

# Evaluation of Differential Codebooks for IEEE 802.16m Amendment Working Document

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Discussion and approval

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# Background

- This contribution presents the performance evaluation of differential codebooks
- SDD supports a differential feedback mode for codebook based precoding in DL SU and MU-MIMO
- In San Diego meeting, SDD supports “rotation based schemes”.

# 2 kinds of rotation based schemes

[C80216m-09\_0058r4.doc]

- Rotation Scheme 1: right quantization

- Differentiation at SS:  $\mathbf{D} = \mathbf{Q}^H(t-1) \mathbf{V}(t)$

- Quantization at SS:  $\hat{\mathbf{D}} = \arg \max_{\mathbf{D}_i \in C_d} \|\mathbf{D}^H \mathbf{D}_i\|_F$

- Beamforming matrix reconstruction at BS:

$$\hat{\mathbf{V}}(t) = \mathbf{Q}(t-1) \hat{\mathbf{D}}$$

- Beamforming at BS:  $\mathbf{y} = \mathbf{H} \hat{\mathbf{V}}(t) \mathbf{s} + \mathbf{n}$

# Our Proposal

- Rotation Scheme 2: left quantization

- Differentiation at SS:  $\mathbf{D} = \mathbf{V}(t) \mathbf{Q}^H(t-1)$

- Quantization at SS:  $\hat{\mathbf{D}} = \arg \max_{\mathbf{D}_i \in C_d} \|\mathbf{D}^H \mathbf{D}_i\|_F$

- Beamforming matrix reconstruction at BS:

$$\hat{\mathbf{V}}(t) = \hat{\mathbf{D}} \mathbf{Q}(t-1) \quad \mathbf{Q}(t-1) = \hat{\mathbf{V}}(t-1)$$

- Beamforming at BS:  $\mathbf{y} = \mathbf{H} \hat{\mathbf{V}}(t) \mathbf{s} + \mathbf{n}$

	Rotation Scheme 1	Rotation Scheme 2
<b>Design Principle</b>	Quantize the right side combining weight space	Quantize a rotation matrix space
<b>Properties</b>	<b>Difficult to adapt to the time correlation statistics</b> no parameters related to the channel temporal statistics in the codebook design	<b>Function of the temporal correlation statistics</b> Codebook construction is function of the time correlation $\rho$
	<b>High complexity</b> <ul style="list-style-type: none"> <li>• One codebook per rank</li> <li>• <math>\mathbf{Q}(t-1)</math> based on multiple Householder transformation of <math>\hat{\mathbf{V}}(t-1)</math></li> </ul>	<b>Low complexity</b> <ul style="list-style-type: none"> <li>• The same codebook for all ranks</li> <li>• <math>\mathbf{Q}(t-1) = \hat{\mathbf{V}}(t-1)</math></li> </ul>
	<b><math>N_t \times N_s</math> space to quantize</b> <ul style="list-style-type: none"> <li>• no equivalence relation of the codebook <ul style="list-style-type: none"> <li>– No distance measure related to system performance</li> <li>– No guarantee that the Cbk does not overquantize the space</li> </ul> </li> <li>• The quantization error not only depends on the rank of <math>\mathbf{D}</math> but also on the quant. error induced in <math>\mathbf{Q}</math></li> <li>• Some ambiguity when applying HH transformation for generating <math>\mathbf{Q}</math> (for columns from <math>N_t - N_s</math> to <math>N_t</math>)</li> <li>•&gt; <b>sensitivity to quantization error difficult to control and assess</b></li> </ul>	<b><math>N_t</math>-dimensional unitary space</b> <ul style="list-style-type: none"> <li>• Proof of the equivalence relation which decreases the volume of the codebook space</li> <li>• The base differential codebook is in Riemannian manifold -&gt; distance measure can be defined</li> <li>•&gt; <b>Compactly packed rotation codebook</b></li> </ul>

# Rotation schemes 1: a smaller quantization error ?

- C80216m-09\_0058r4.doc claim that Rotation schemes 1 “quantizes a smaller dimension, hence resulting in denser codebook and smaller quantization errors” is questionable

$$\hat{\mathbf{V}}(t) = \hat{\mathbf{Q}}(t-1) \hat{\mathbf{D}}(t)$$

Build based on

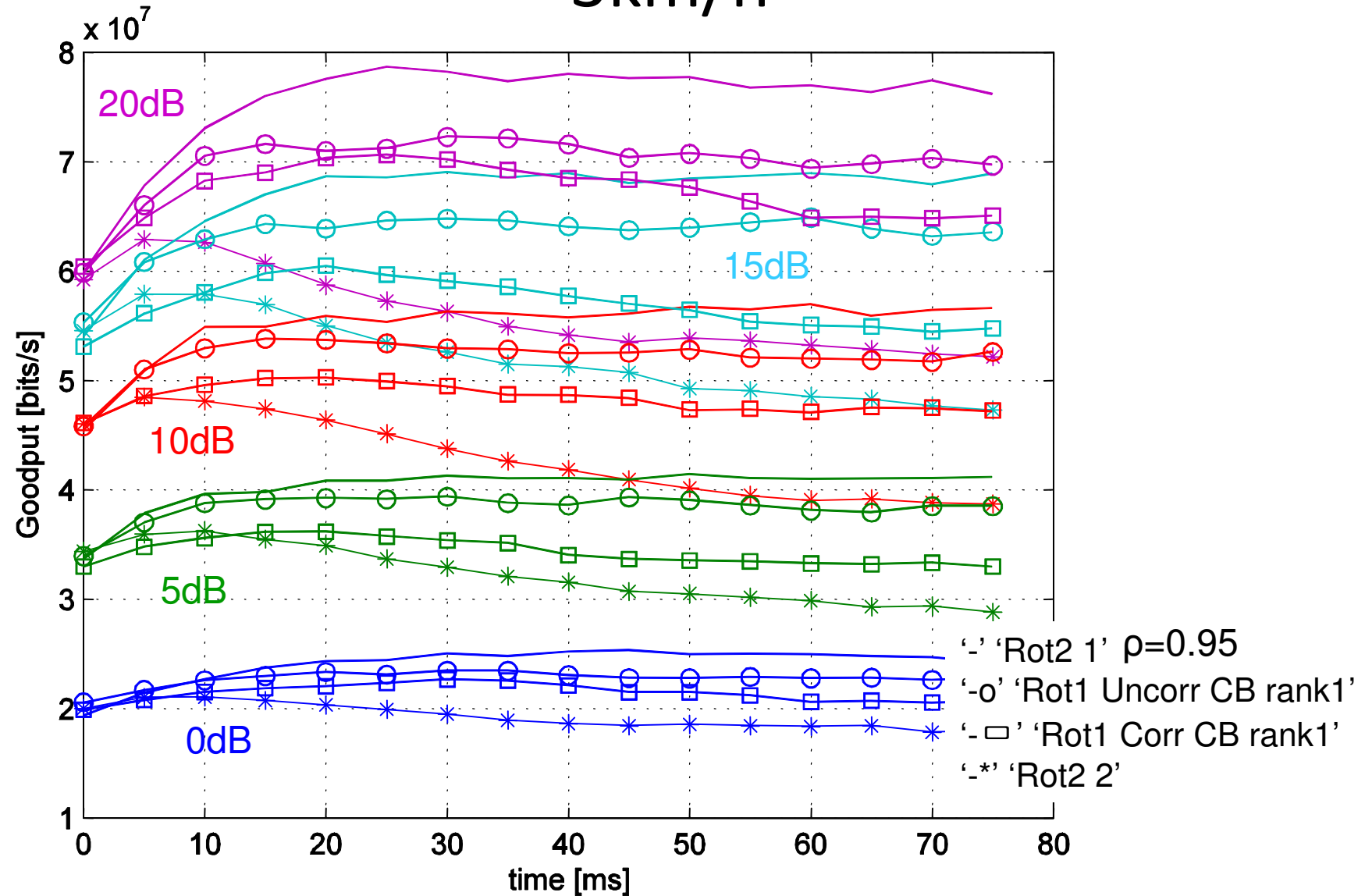
$$\hat{\mathbf{V}}(t-1) = \hat{\mathbf{Q}}(t-2) \hat{\mathbf{D}}(t-1)$$

- Quantization error in D appears at 2 levels
- Householder operation in Q boosts and spreads the quantization error

# Differential codebooks

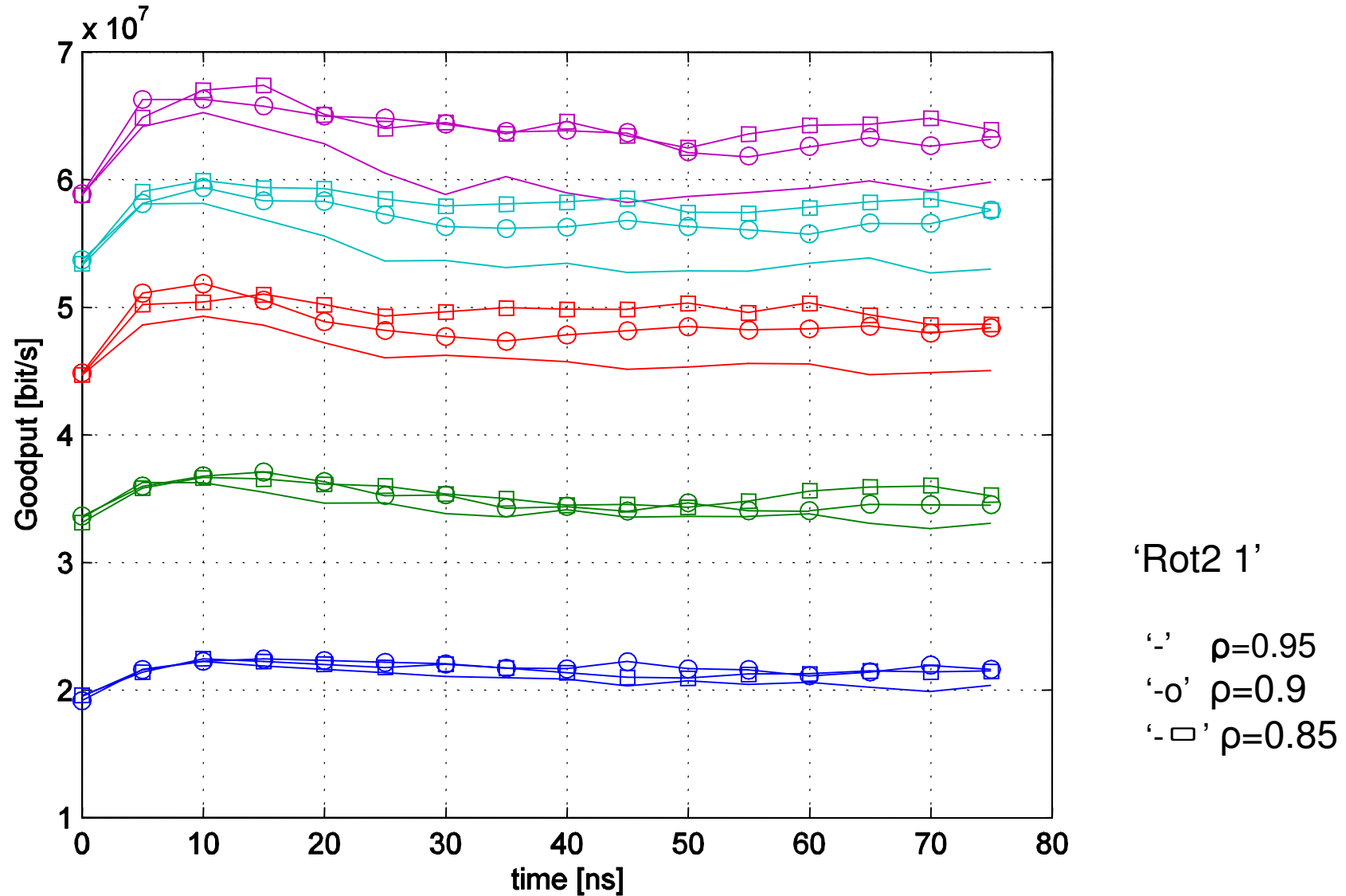
	rank	label	Codebook size	reference
Rotation scheme 1	Rank 1	'Rot1 Uncorr CB rank1'	3 bit	C80216m-09_0528.ppt (Guangjie Li et al.)
		'Rot1 Corr CB rank1'	3 bit	
	Rank 2	'Rot1 Uncorr CB rank2'	3 bit	
Rotation scheme 2	For all Ranks	'Rot2 1'	4 bit	C80216m-09_0677.doc (David Mazzaresse et al.)
	For all Ranks	'Rot2 2'	4 bit	C80216m-09_038r1_LGE_r1.doc (WookBong Lee et al.)

# MU MIMO: uncorrelated ( $4 \lambda$ , $15^\circ$ AS), 3km/h





# MU MIMO: uncorrelated ( $4 \lambda$ , $15^\circ$ AS), 6km/h



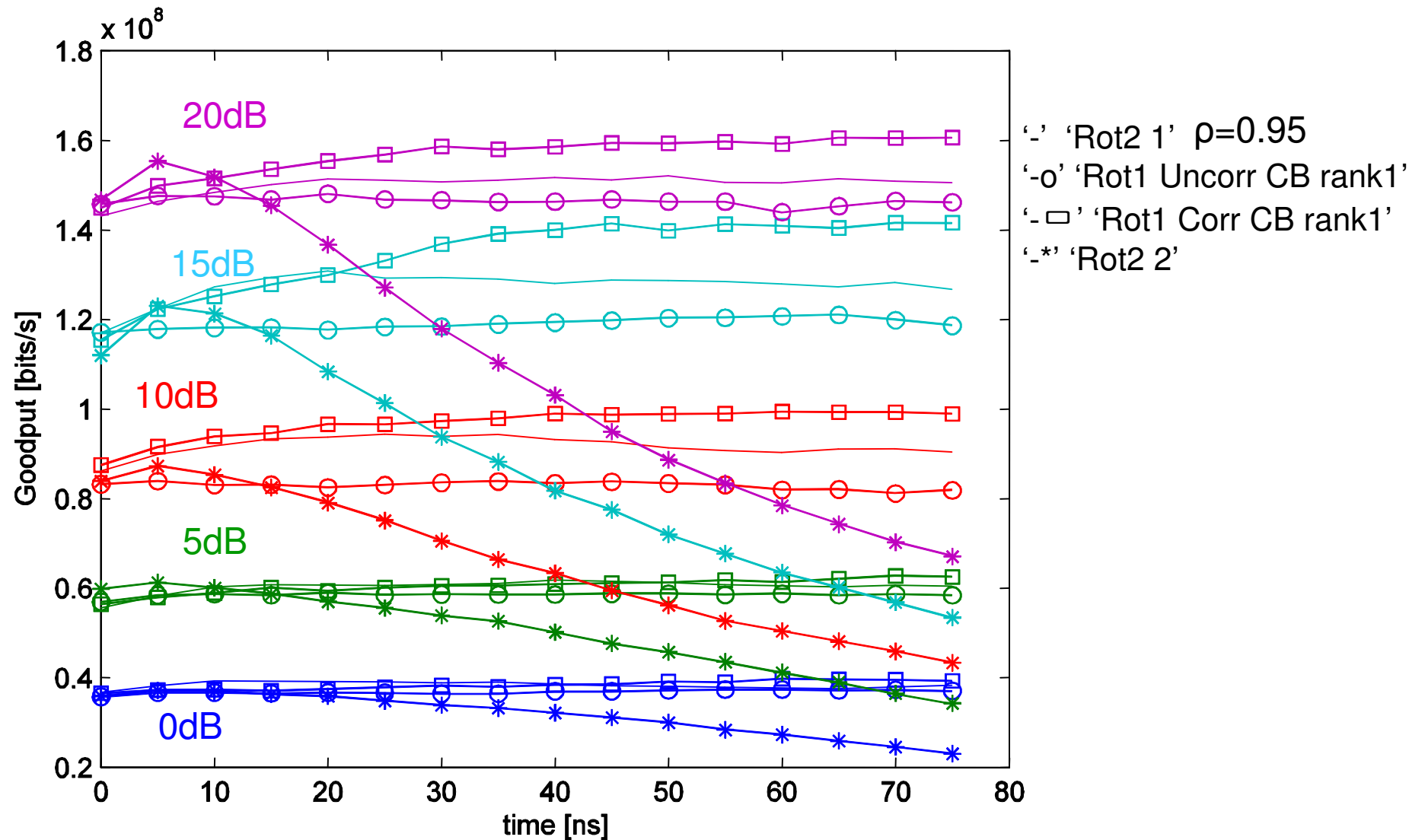
# observations

- Good refinement for 'Rot2 1' and 'Rot1 Uncorr CB rank1'
- 'Rot1 Corr CB rank1' optimized for small spacing shows loss or weak refinement in uncorrelated channels
- 'Rot2 2' shows significant loss due to small distance on the Riemannian manifold

	Distance on Riemannian manifold	properties
'Rot2 1'	0.9822	<b>Equally spaced</b> codebook
'Rot2 2'	0.0266	<b>Not equally spaced</b> codebook

- 'Rot2 1' easily adapts to mobile speed (i.e. parameter  $\rho$ )
- **Overall: 'Rot2 1' shows the best performance and flexibility**

# MU MIMO: correlated ( $0.5 \lambda$ , $3^\circ$ AS), 3km/h



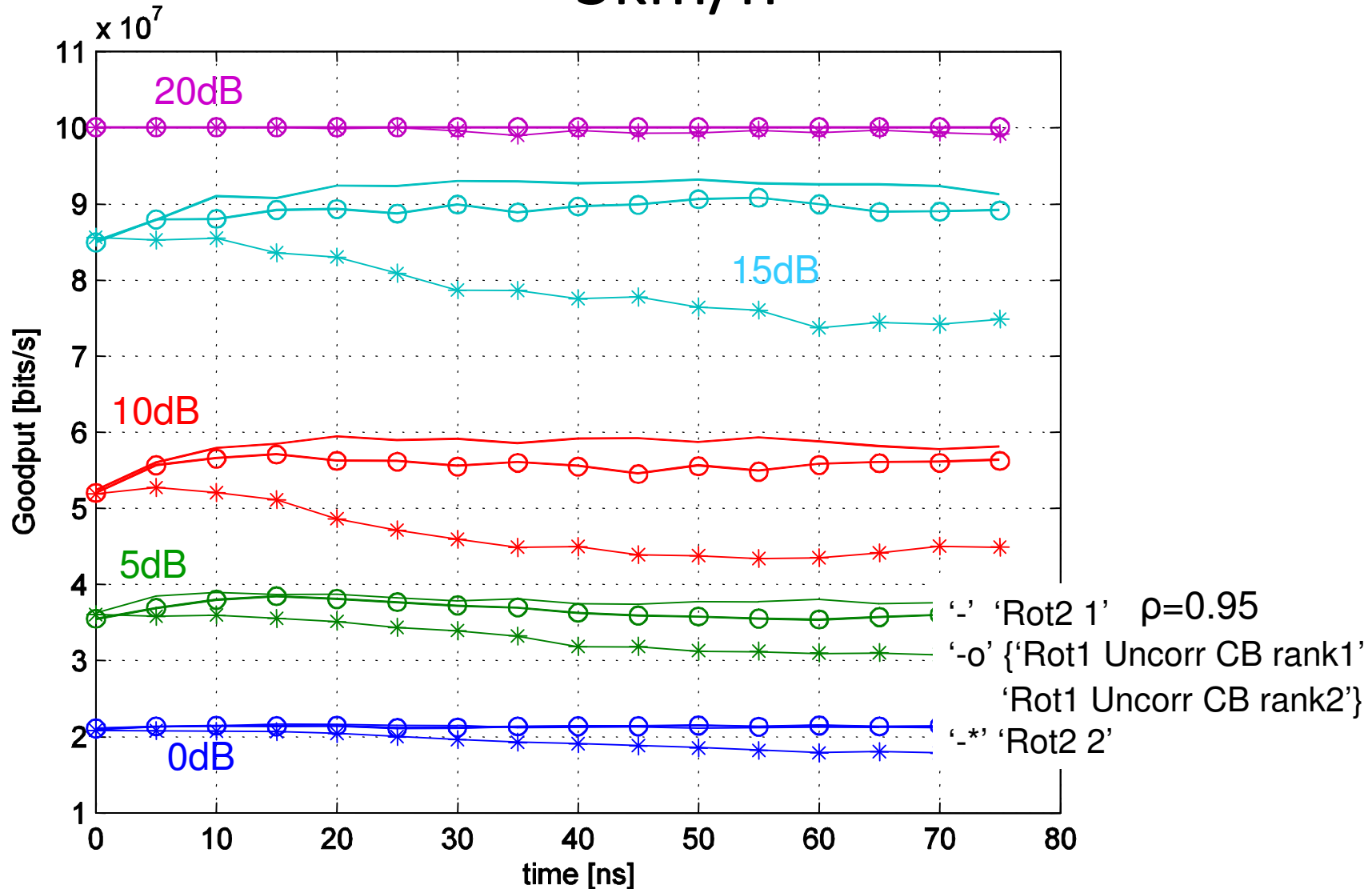
# observations

- Differential codebook less beneficial in correlated channels than in uncorrelated channels
- Good refinement for 'Rot1 Corr CB rank1'
- Good Robustness for 'Rot2 1'
  - Moderate refinement in correlated channels
- 'Rot1 Uncorr CB rank1' shows no throughput improvement compared to base codebook
- **Overall: 'Rot1 Corr CB rank1' shows the best performance**

# MU-MIMO: summary

	Uncorrelated	Correlated
'Rot1 Uncorr CB rank1'	good refinement	No refinement
'Rot1 Corr CB rank1'	Not robust enough	The best: excellent refinement
'Rot2 1'	The best: excellent refinement	Robust: moderate refinement
'Rot2 2'	Loss	Loss

# CL SU MIMO: uncorrelated ( $4 \lambda$ , $15^\circ$ AS), 3km/h



# SU-MIMO: summary

	Uncorrelated
{'Rot1 Uncorr CB rank1', 'Rot1 Uncorr CB rank2'}	moderate refinement
'Rot2 1'	The best: excellent refinement
'Rot2 2'	Loss

# Conclusions

- We propose to adopt 'Rot2 1' as the differential feedback mode for codebook based feedback
  - the best performance in SU and MU MIMO uncorrelated channels and robust in correlated channels
  - Lower complexity compared to rotation schemes 1
  - Easily adaptable to various environment and mobile speed
- Adopt text proposal #12 in C80216m-09\_0677.doc



# Appendix: Simulation Assumptions

- Channel model: Pedestrian B channel model, 3km/h, linear array
  - Uncorrelated:  $AS= 15$ ,  $d/\lambda=4$
  - Correlated:  $AS= 3$ ,  $d/\lambda=0.5$
- 10 MHz
- HARQ (Chase Combining, non-adaptive) with 3 retransmissions
  - Delay first transmission: 6 subframes
  - Delay between re-transmissions: 1 frame (8 subframes)
  - Delay between 2 midamble (update of the differential precoder): 1 frame (8 subframes)
- CQI, PMI feedback period: every frame (5 ms)
- Link Adaptation (PHY abstraction): QPSK 1/2 with repetition 1/2/4/6, QPSK 3/4, 16QAM 1/2, 16QAM 3/4, 64QAM 1/2, 64QAM 2/3, 64QAM 3/4, 64QAM 5/6
- Ideal channel estimation
- MMSE receiver
- No CQI transmission errors
- ZFBF, CL SU MIMO with SCW and rank adaptation
- LLRU (4 PRUs)
- Base codebook: 4bit subset C80216m-08/577
- Ideal antenna calibration
- No constraint on PAPR