SJTP: Pattern Characteristics

6/18/2001

Disparity Probability

- N-bit sequence
 - # of ones = X
 - # of zeros = N X
- ΔRD = disparity of the sequence

 $\Delta RD = X - (N - X) = 2X - N$

- p(X,N) = probability that X ones occur in N "trials"
 - Assume ones & zeros are equally likely

$$p(X,N) = \binom{N}{X} \left(\frac{1}{2}\right)^N$$
 where $\binom{N}{X} = \frac{N!}{X!(N-X)!}$

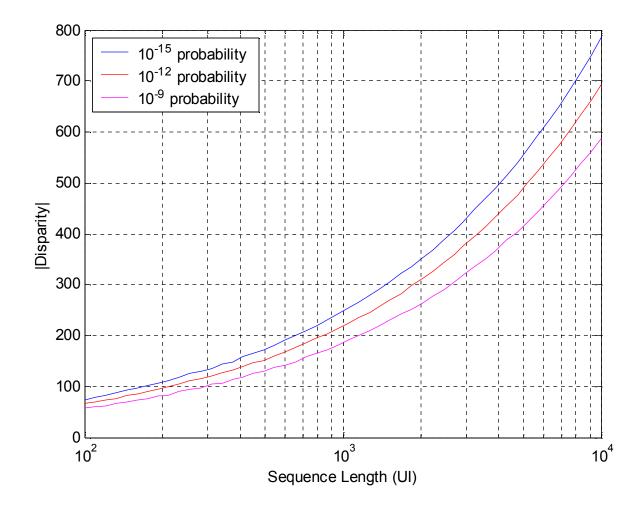
- Probability that $\leq X$ ones occur in the sequence

$$\Pr\{\# \text{ of ones } \le X \mid N\} = \sum_{i=1}^{X} p(i, N)$$

• Probability that magnitude of the disparity is > RD₀

$$\Pr\{|\Delta RD| > RD_0 | N\} = 2 \sum_{i=1}^{(RD_0 + N)/2} p(i, N)$$

Disparity Probability



Transition Density Probability

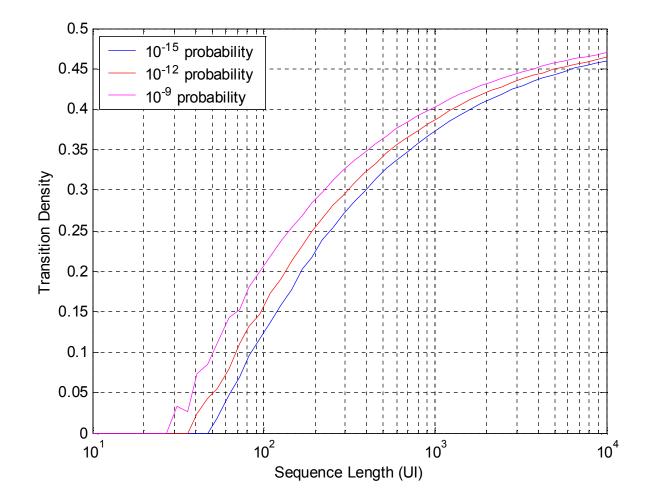
- N-bit sequence
 - X transitions within sequence
- Transition density = X/N
- p(X,N) = probability that X transitions occur in N "trials"
 - Assume ones & zeros are equally likely

$$\Pr\{X \mid N\} = \binom{N-1}{X} \left(\frac{1}{2}\right)^{N-1} = p(X, N-1)$$

• Probability that transition density $\leq TD_0$

$$\Pr\{X \le TD_0 N \mid N\} = \sum_{i=1}^{TD_0 N} p(i, N-1)$$

Transition Density Probability



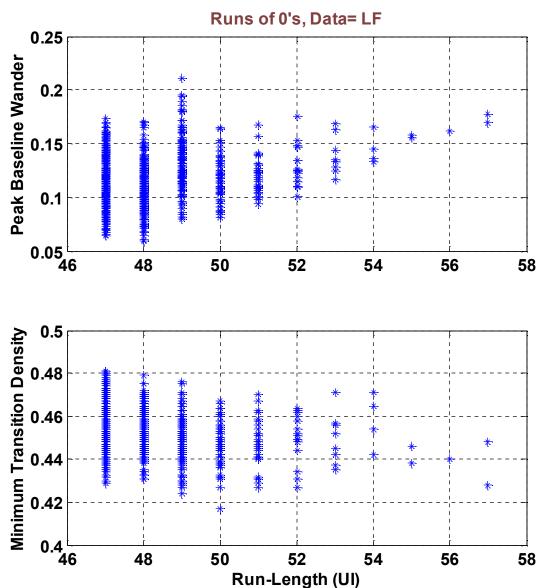
Pattern Selection Criteria?

- Looking for events that occur "once per day"
 - Probability ~ 1×10^{-15}
- Need to choose sequence length (N)
- Following examples:
 - Transition density calculations
 - N= 1000 \rightarrow transition density ~ 0.37 at 10⁻¹⁵ probability
 - Baseline wander calculations
 - Pole corner frequency = $f_c = B/5000$ (~2.5% RMS wander)
 - 10^{-15} probability $\rightarrow \sim 8\sigma = 0.2$ peak baseline wander

Pattern Characteristics

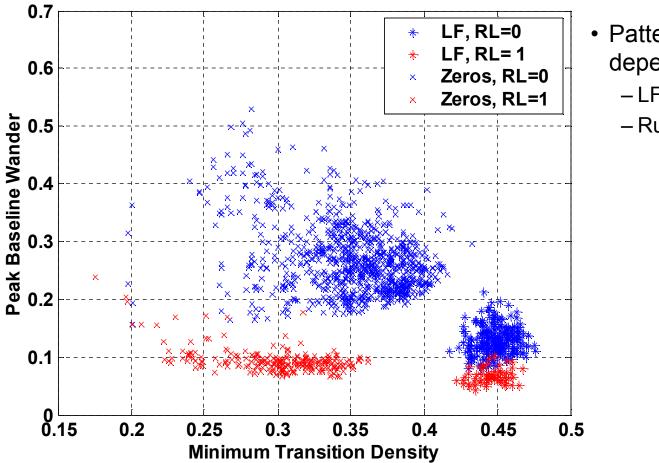
- Procedure
 - Seed PRBS generator with max run-length
 - adjust so max RL occurs in the middle of the sequence
 - Generate 128 block PRBS
 - Compute statistics
- Parameters
 - Max runs of ones or zeros
 - Data is all zeros or LF
 - Search all seeds that generate given max run-length

Pattern Characteristics (cont.)



 Weak trends based on maximum run-length

Pattern Characteristics



- Pattern characteristics depend dramatically on:
 - LF vs. Zero data input
 - Runs of zeros vs. ones