# SJTP: Pattern Characteristics 

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## Disparity Probability

- N -bit sequence
- \# of ones = X
- \# of zeros $=\mathrm{N}$ - X
- $\Delta \mathrm{RD}=$ disparity of the sequence

$$
\Delta R D=X-(N-X)=2 X-N
$$

- $\mathrm{p}(\mathrm{X}, \mathrm{N})=$ probability that X ones occur in N "trials"
- Assume ones \& zeros are equally likely

$$
p(X, N)=\binom{N}{X}\left(\frac{1}{2}\right)^{N} \quad \text { where }\binom{N}{X}=\frac{N!}{X!(N-X)!}
$$

- Probability that $\leq \mathrm{X}$ ones occur in the sequence

$$
\operatorname{Pr}\{\# \text { of ones } \leq X \mid N\}=\sum_{i=1}^{X} p(i, N)
$$

- Probability that magnitude of the disparity is $>R D_{0}$

$$
\operatorname{Pr}\left\{|\Delta R D|>R D_{0} \mid N\right\}=2 \sum_{i=1}^{\left(R D_{0}+N\right) / 2} p(i, N)
$$

## Disparity Probability



## Transition Density Probability

- N -bit sequence
- $X$ transitions within sequence
- Transition density $=\mathrm{X} / \mathrm{N}$
- $p(X, N)=$ probability that $X$ transitions occur in $N$ "trials"
- Assume ones \& zeros are equally likely

$$
\operatorname{Pr}\{X \mid N\}=\binom{N-1}{X}\left(\frac{1}{2}\right)^{N-1}=p(X, N-1)
$$

- Probability that transition density $\leq \mathrm{TD}_{0}$

$$
\operatorname{Pr}\left\{X \leq T D_{0} N \mid N\right\}=\sum_{i=1}^{T D_{0} N} p(i, N-1)
$$

## Transition Density Probability



## Pattern Selection Criteria?

- Looking for events that occur "once per day"
- Probability ~ $1 \times 10^{-15}$
- Need to choose sequence length (N)
- Following examples:
- Transition density calculations
- $\mathrm{N}=1000 \rightarrow$ transition density $\sim 0.37$ at $10^{-15}$ probability
- Baseline wander calculations
- Pole corner frequency $=f_{c}=B / 5000$ ( $\sim 2.5 \%$ RMS wander)
- 10-15 probability $\rightarrow \sim 8 \sigma=0.2$ peak baseline wander


## Pattern Characteristics

- Procedure
- Seed PRBS generator with max run-length
- adjust so max RL occurs in the middle of the sequence
- Generate 128 block PRBS
- Compute statistics
- Parameters
- Max runs of ones or zeros
- Data is all zeros or LF
- Search all seeds that generate given max run-length


## Pattern Characteristics (cont.)



- Weak trends based on maximum run-length


## Pattern Characteristics



- Pattern characteristics depend dramatically on:
-LF vs. Zero data input
-Runs of zeros vs. ones

