

A look at the tolerance stackup of the Avaya resistive method of discovery  
 In this case, V2 is exactly equal to  $(V1 \cdot (1 \pm \text{src\_tol})) / 2 \cdot (1 \pm \text{src\_rel\_tol})$

The given Inputs:

res\_tol := 1%      src\_tol := 1%      src\_rel\_tol := 1%  
 R1 := 75000      V1 := 24      Rsigmax := 26500      Rsigmin := 19000

The calculations, Vomin and Vmax are the required detector windows to acquire the desired range of signature resistor

$$\text{Vomax}(a, b, c) := \left[ \text{Rsigmax} \cdot \frac{(V1) \cdot (1 + a \cdot \text{src\_tol}) - \left[ \frac{V1 \cdot (1 + a \cdot \text{src\_tol})}{2} \right] \cdot (1 + c \cdot \text{src\_rel\_tol})}{R1 \cdot (1 + b \cdot \text{res\_tol}) + \text{Rsigmax}} \right]$$

$$\text{Vomin}(a, b, c) := \left[ \text{Rsigmin} \cdot \frac{(V1) \cdot (1 + a \cdot \text{src\_tol}) - \left[ \frac{V1 \cdot (1 + a \cdot \text{src\_tol})}{2} \right] \cdot (1 + c \cdot \text{src\_rel\_tol})}{R1 \cdot (1 + b \cdot \text{res\_tol}) + \text{Rsigmin}} \right]$$

all the possible cases of tolerance stackup:

|                           |                           |
|---------------------------|---------------------------|
| Vomax(-1, -1, -1) = 3.156 | Vomin(-1, -1, -1) = 2.445 |
| Vomax(-1, -1, 1) = 3.094  | Vomin(-1, -1, 1) = 2.396  |
| Vomax(-1, 1, -1) = 3.11   | Vomin(-1, 1, -1) = 2.406  |
| Vomax(-1, 1, 1) = 3.048   | Vomin(-1, 1, 1) = 2.358   |
| Vomax(1, -1, -1) = 3.22   | Vomin(1, -1, -1) = 2.494  |
| Vomax(1, -1, 1) = 3.156   | Vomin(1, -1, 1) = 2.445   |
| Vomax(1, 1, -1) = 3.173   | Vomin(1, 1, -1) = 2.455   |
| Vomax(1, 1, 1) = 3.11     | Vomin(1, 1, 1) = 2.406    |

VMAX := max(Vomax(-1, -1, -1), Vomax(-1, -1, 1), Vomax(-1, 1, -1), Vomax(-1, 1, 1), Vomax(1, -1, -1), Vomax(1, -1, 1), Vomax(1, 1, -1), Vomax(1, 1, 1))  
 VMIN := min(Vomin(-1, -1, -1), Vomin(-1, -1, 1), Vomin(-1, 1, -1), Vomin(-1, 1, 1), Vomin(1, -1, -1), Vomin(1, -1, 1), Vomin(1, 1, -1), Vomin(1, 1, 1))

Here are the extreme maximum and minimum Detector Voltages

the highest

the lowest

$$V_{MAX} = 3.22$$

$$V_{MIN} = 2.358$$

Now add in a little margin to obtain the equiv worst case detector thresholds

$$\text{ref\_marg} := 0.001\%$$

$$V_{rejmax} := V_{MAX} \cdot (1 + \text{ref\_marg})$$

$$V_{rejmin} := V_{MIN} \cdot (1 - \text{ref\_marg})$$

$$V_{rejmax} = 3.22$$

$$V_{rejmin} = 2.358$$

Now, let's calculate the resistance range that is guaranteed to be rejected

$$R_{rejmax}(a, b, c) := \frac{V_{rejmax} \cdot R1 \cdot (1 + b \cdot \text{res\_tol})}{(V1) \cdot (1 + a \cdot \text{src\_tol}) - \left[ \frac{V1 \cdot (1 + a \cdot \text{src\_tol})}{2} \right] \cdot (1 + c \cdot \text{src\_rel\_tol}) - V_{rejmax}}$$

$$R_{rejmin}(a, b, c) := \frac{V_{rejmin} \cdot R1 \cdot (1 + b \cdot \text{res\_tol})}{(V1) \cdot (1 + a \cdot \text{src\_tol}) - \left[ \frac{V1 \cdot (1 + a \cdot \text{src\_tol})}{2} \right] \cdot (1 + c \cdot \text{src\_rel\_tol}) - V_{rejmin}}$$

$$R_{rejmax}(-1, -1, -1) = 27232.07$$

$$R_{rejmin}(-1, -1, -1) = 18164.53$$

$$R_{rejmax}(-1, -1, 1) = 27989.597$$

$$R_{rejmin}(-1, -1, 1) = 18623.529$$

$$R_{rejmax}(-1, 1, -1) = 27782.213$$

$$R_{rejmin}(-1, 1, -1) = 18531.488$$

$$R_{rejmax}(-1, 1, 1) = 28555.044$$

$$R_{rejmin}(-1, 1, 1) = 18999.762$$

$$R_{rejmax}(1, -1, -1) = 26500.36$$

$$R_{rejmin}(1, -1, -1) = 17719$$

$$R_{rejmax}(1, -1, 1) = 27232.07$$

$$R_{rejmin}(1, -1, 1) = 18164.528$$

$$R_{rejmax}(1, 1, -1) = 27035.72$$

$$R_{rejmin}(1, 1, -1) = 18076.956$$

$$R_{rejmax}(1, 1, 1) = 27782.213$$

$$R_{rejmin}(1, 1, 1) = 18531.488$$

$$R_{MIN} := \min(R_{rejmin}(-1, -1, -1), R_{rejmin}(-1, -1, 1), R_{rejmin}(-1, 1, -1), R_{rejmin}(-1, 1, 1), R_{rejmin}(1, -1, -1), R_{rejmin}(1, -1, 1), R_{rejmin}(1, 1, -1), R_{rejmin}(1, 1, 1))$$

$$R_{MAX} := \max(R_{rejmax}(-1, -1, -1), R_{rejmax}(-1, -1, 1), R_{rejmax}(-1, 1, -1), R_{rejmax}(-1, 1, 1), R_{rejmax}(1, -1, -1), R_{rejmax}(1, -1, 1), R_{rejmax}(1, 1, -1), R_{rejmax}(1, 1, 1))$$

Summary:

If the minimum and maximum Signature Resistor Values are given as:

$$R_{\text{sigmin}} = 19000$$

$$R_{\text{sigmax}} = 26500$$

And if the 75K resistor tolerance ( $\text{res\_tol}$ ), and the source voltage tolerances ( $\text{src\_tol}$ ) are:

$$\text{res\_tol} = 1 \%$$

$$\text{src\_tol} = 1 \%$$

$$\text{src\_rel\_tol} = 1 \%$$

Then

Any signature resistor above this value will be rejected:

$$R_{\text{MAX}} = 28555.044$$

Any signature resistor below this value will be rejected:

$$R_{\text{MIN}} = 17718.997$$