Thoughts on Comment 128 (linear fit to ICR curve)

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John D'Ambrosia (dambrosia_02_0905) suggested these equations for fitting ICR:

$$favg = \frac{1}{N} \sum_{n} f_{n}$$

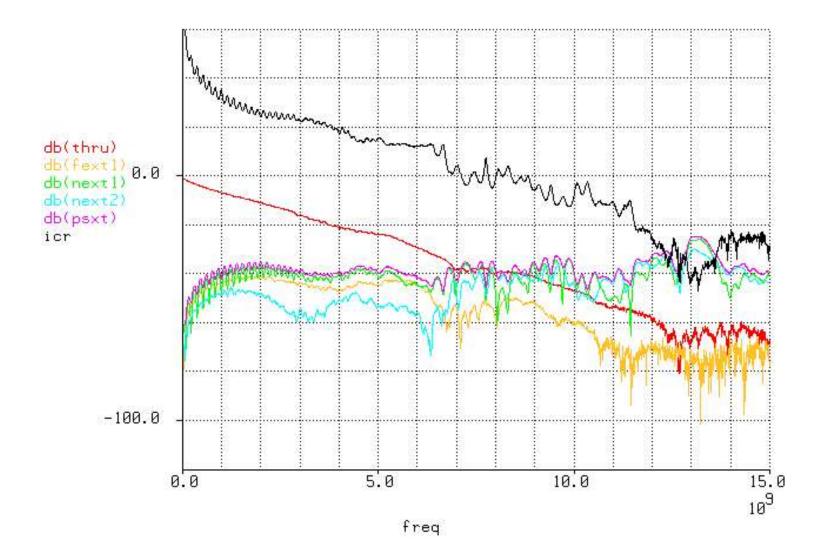
$$ICRavg = \frac{1}{N} \sum_{n} ICR(f_{n})$$

$$m = \frac{\sum_{n} (f_{n} - favg)(ICR(f_{n}) - ICRavg)}{\sum_{n} (f_{n} - favg)^{2}}$$

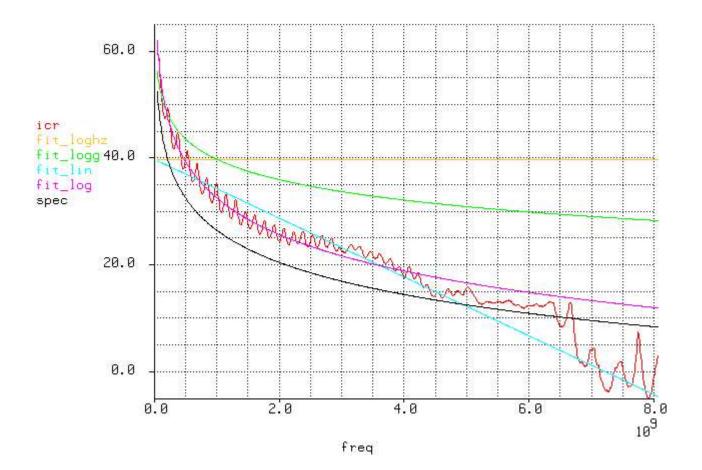
$$b = ICRavg - mfavg$$

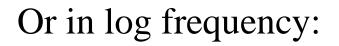
$$ICRLOG(f) = m \ln f - b$$

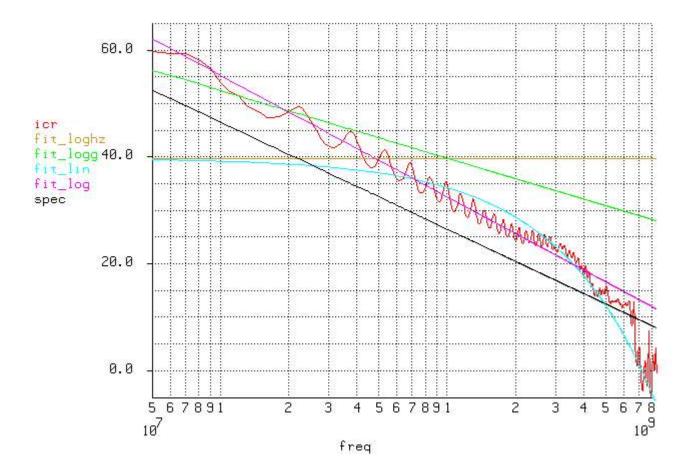
To test these equations I used the following curves from D'Ambrosia Case2 channel model.



I tried 4 ways of fitting the ICR curve: In linear frequency:







On these plots: The Red curve is ICR The Brownish curve is a literal following of the D'Ambrosia equations. The Green Curve is the D'Ambrosia equations assuming frequency is in GHz rather than Hz The Light Blue curve is a linear frequency fit The Magenta curve is a log fit using equations given below The Black curve is the ICR spec.

All fits were done over the frequency range 100MHz-5GHz

I think that the magenta curve is the best fit and recommend that we use it.

Equations for performing log fit:

$$log favg = \frac{1}{N} \sum_{n} log(f_n)$$

$$ICRavg = \frac{1}{N} \sum_{n} ICR(f_n)$$

$$m = \frac{\sum_{n} (log(f_n) - log favg)(ICR(f_n) - ICRavg)}{\sum_{n} (log(f_n) - log favg)^2}$$

$$b = ICRavg - m \cdot log favg$$

 $ICRLOG(f) {=} m {\cdot} log(f) {-} b$

I recommend that we propose acceptance of comment 128 in principal with recommended verbiage:

The ICRLOG is defined to be the least mean square fit of the ICR with frequency plotted on a log scale, and is defined by Equations (69-20) through (69-24). The sums in these equations are to be performed over the range of values such that f_n is in the range of frequencies for which IRC is specified.

$$\begin{split} &\log favg = \frac{1}{N} \sum_{n} \log(f_{n}) & \text{Equation69-20} \\ & \text{ICRavg} = \frac{1}{N} \sum_{n} \text{ICR}(f_{n}) & \text{Equation69-21} \\ & m = \frac{\sum_{n} (\log(f_{n}) - \log favg)(\text{ICR}(f_{n}) - \text{ICRavg})}{\sum_{n} (\log(f_{n}) - \log favg)^{2}} & \text{Equation69-22} \\ & \text{b} = \text{ICRavg} - m \cdot \log favg & \text{Equation69-23} \\ & \text{ICRLOG}(f) = m \cdot \log(f) - b & \text{Equation69-24} \end{split}$$

The ICRLOG(*f*) at the receiver is recommended to be at least:

 $ICRLOG(f) > 12.5 - 20 \cdot log(\frac{f}{5 GHz})$ Equation 69-25