

PAM-N Tutorial Material

802.3bj 100 Gb/s Backplane and Copper Cable Task Force

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Outline

- Introduction
- Objectives
- PAM-N Ideal Channel Simulations
- PAM-N Optimum Receiver Analysis
- PAM-N Realizable Receiver Simulations
- Summary
- References

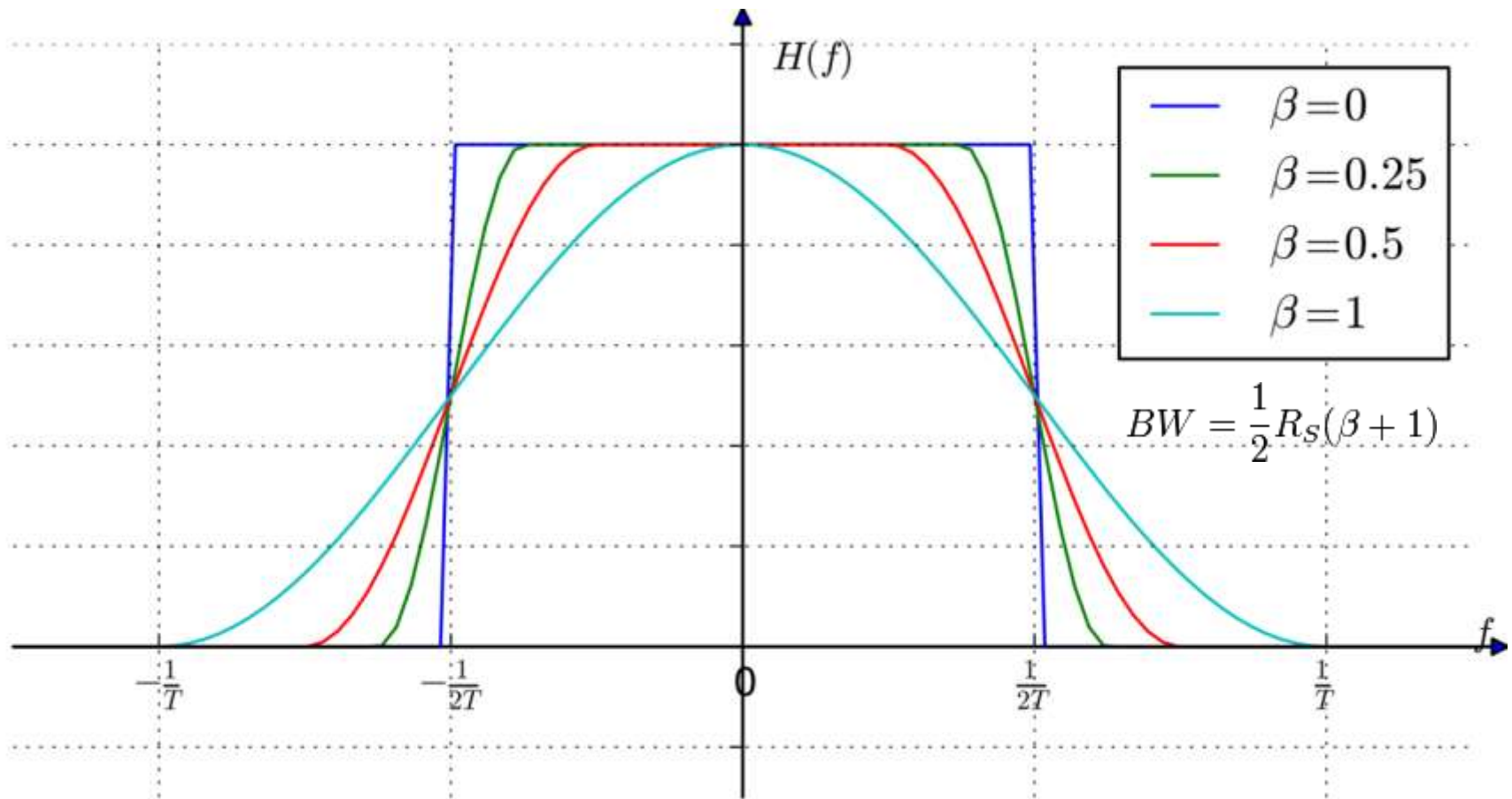
Introduction

- 25Gb/s modulation alternatives are being debated in 802.3bj
- Higher order modulation will be required in future standards to support bandwidth and density growth
- It is critical that there is a broad understanding of PAM-N (amplitude) and more generally QAM (amplitude and phase) modulation to enable informed debate about technology choices for present and future standards

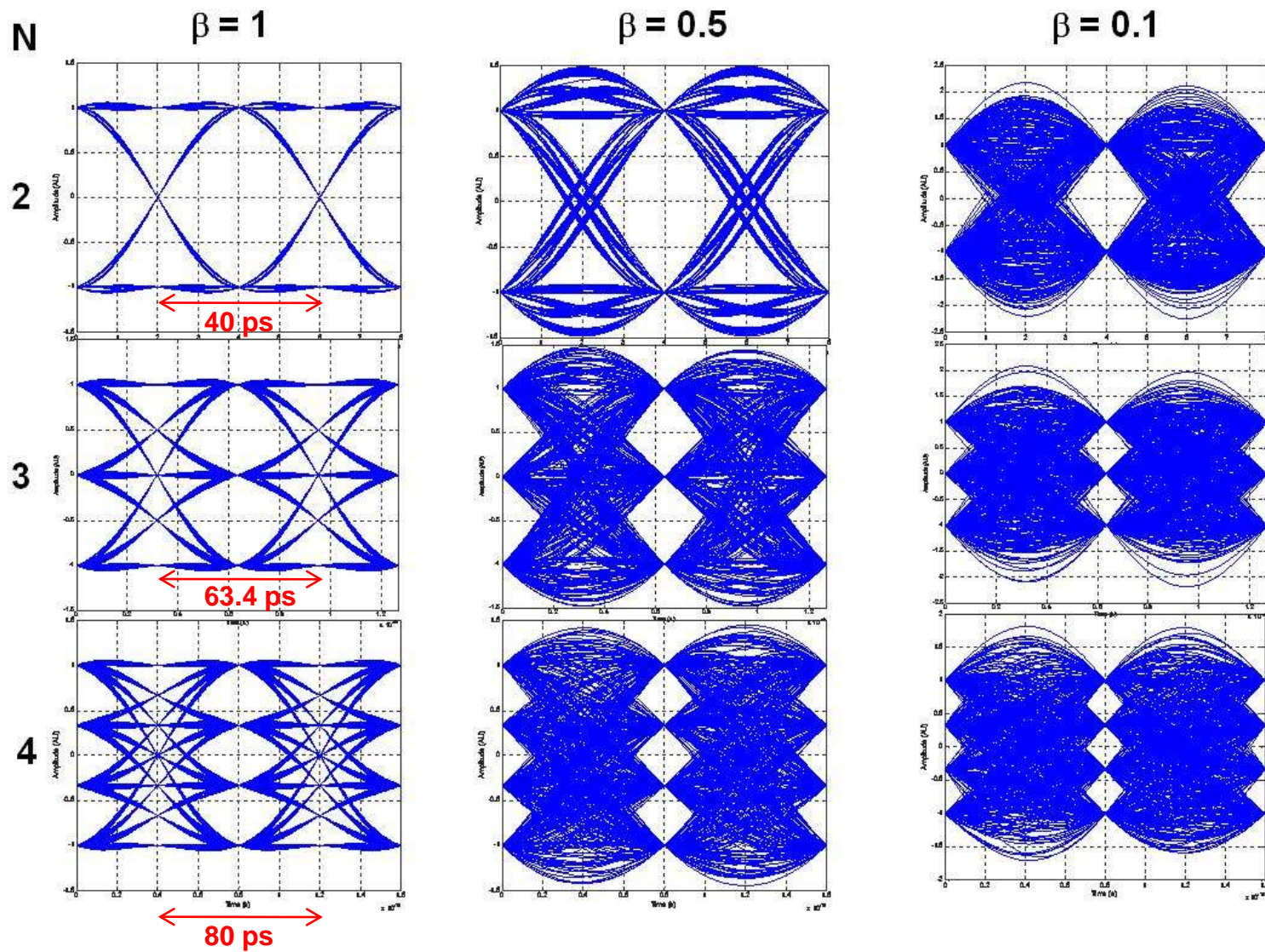
Objectives

- Develop PAM-N modulation tutorial material
- Solicit PAM-N modulation tutorial contributions
- Develop PAM-N performance understanding from:
 - Ideal channel models
 - Fundamental theory
- Compare PAM-2 (NRZ) & PAM-4 performance

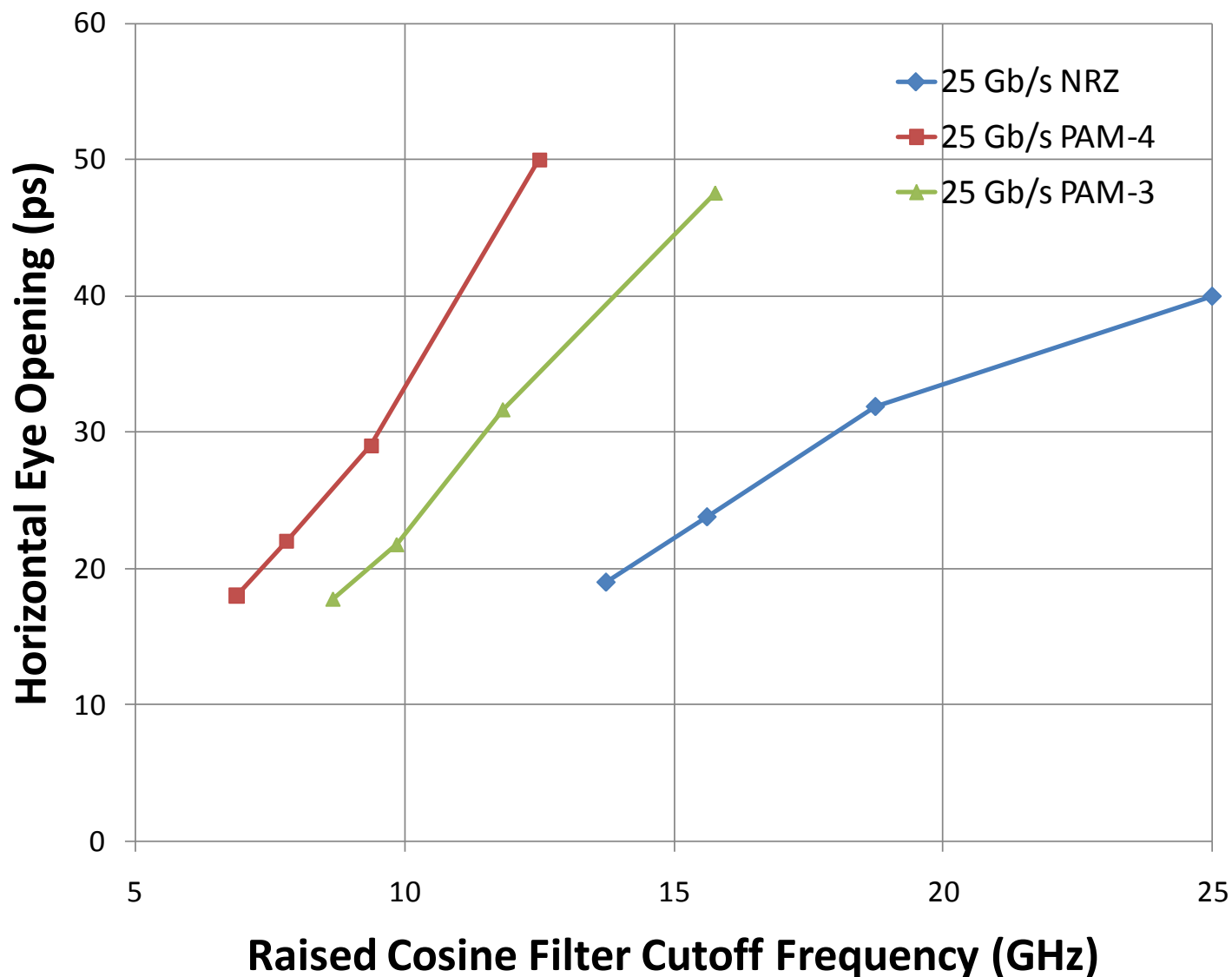
Matlab Model 1: Raised Cosine Channel



PAM-N Eye Diagrams



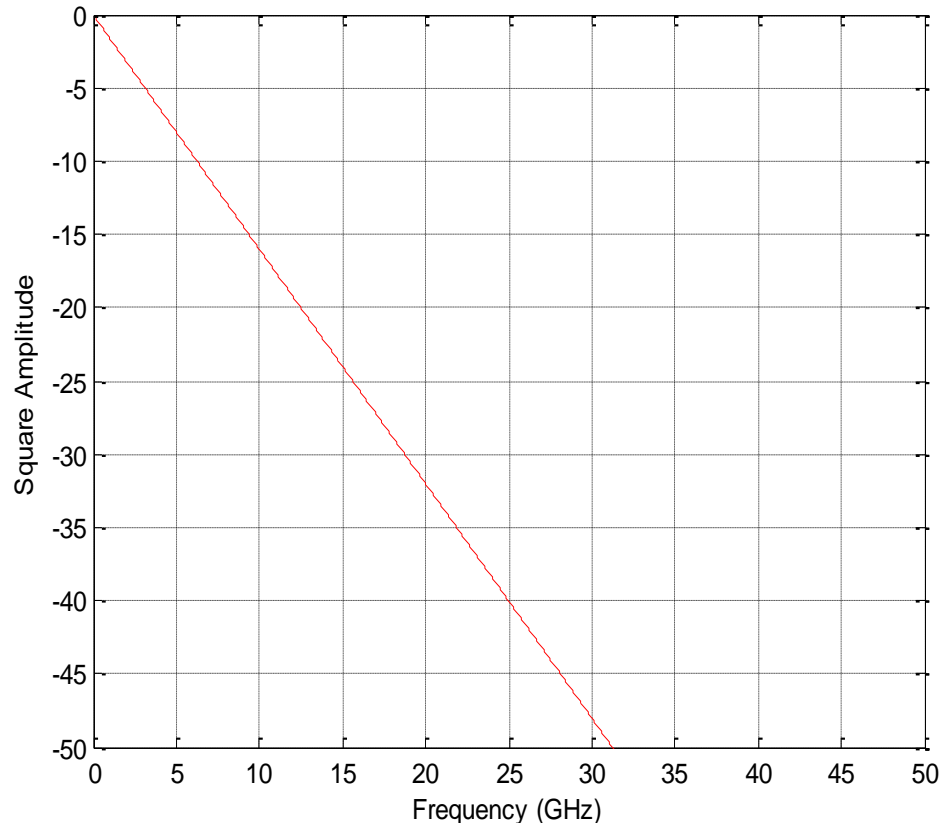
PAM-N Horizontal Eye Opening



Matlab Model 2: Exponential Loss Channel

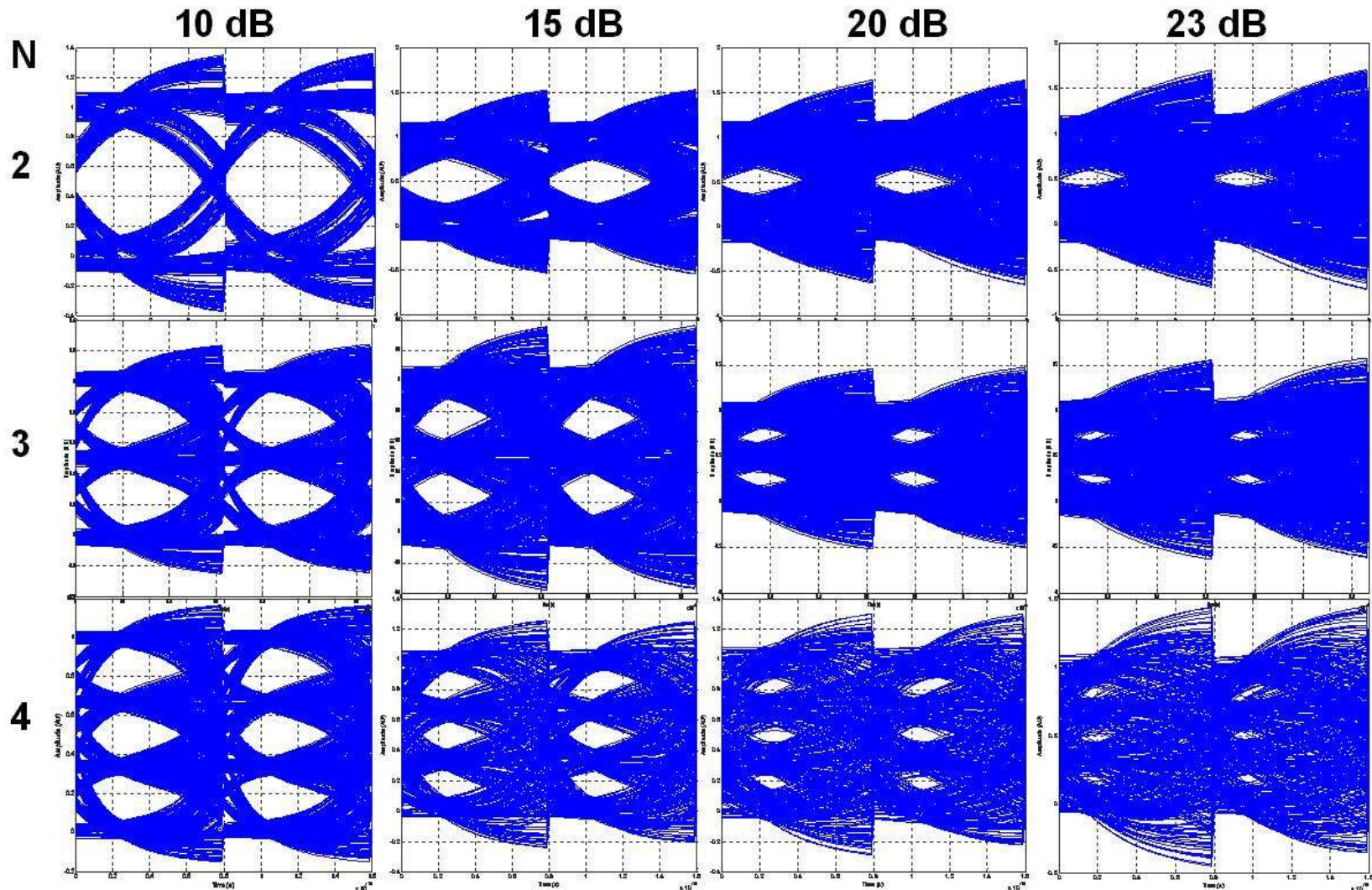


Channel Model



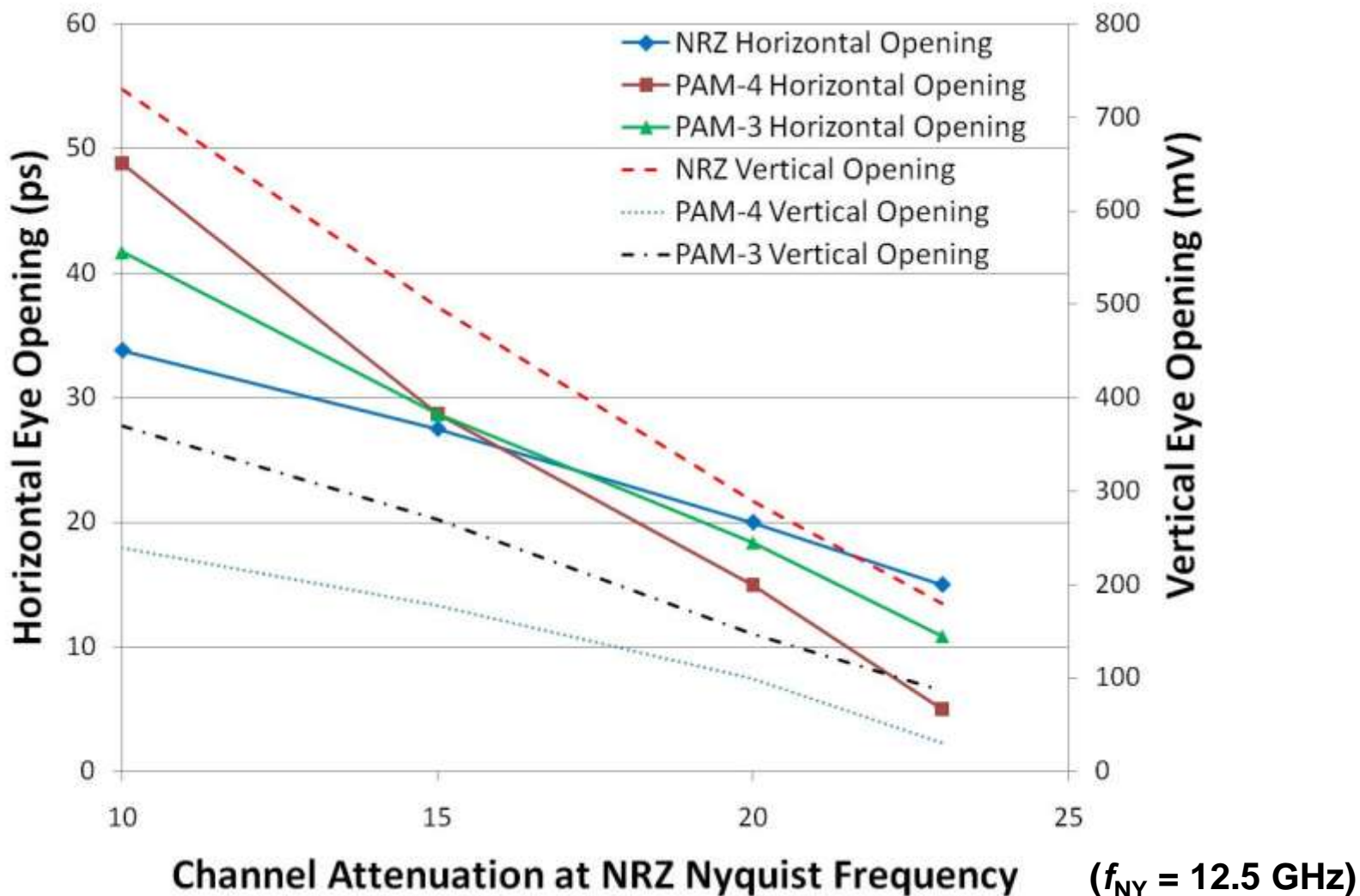
- Ideal Linear Phase Channel
- 20dB loss @ 12.5GHz
- FFE equalizer not included to gain PAM-N performance understanding from DFE only equalizer output

PAM-N Eye Diagrams after DFE



Addition of FFE equalizer will significantly increase the vertical eye opening

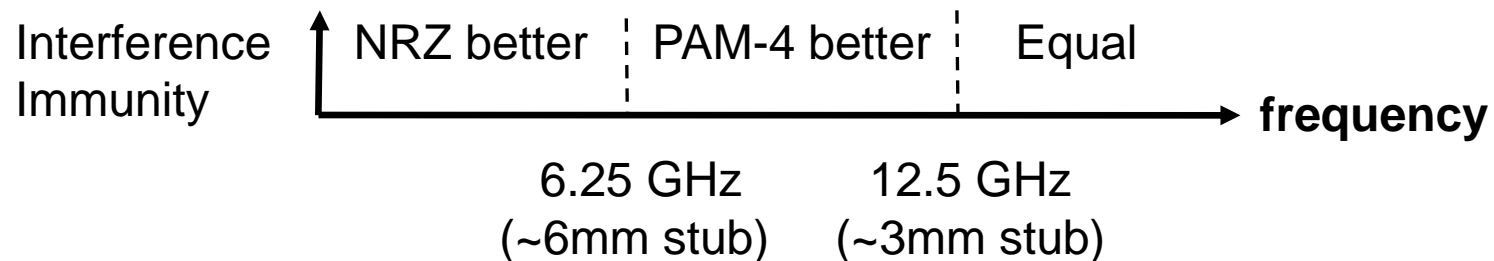
PAM-N Eye Opening



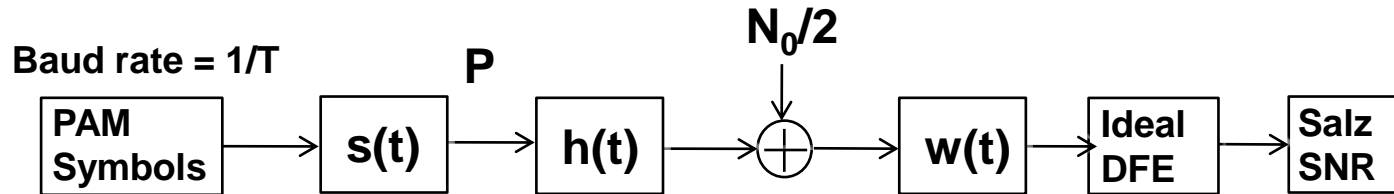
Horizontal and vertical eye openings defined as “inner eye opening”

PAM-N Eye Diagram Observations

- PAM-N has zero ISI at the ideal sampling point with a raised cosine channel response
- For an ideal Nyquist channel, PAM-4 has twice the horizontal eye opening versus NRZ
- In practice ideal sampling never happens; performance is limited by horizontal eye closure due to ISI
- Horizontal eye closure rate with increasing channel loss is faster for PAM-4 than NRZ; ~15dB crossover w/ 3-Tap DFE
- For an ideal Nyquist channel, PAM-4 has better immunity to interferers, like suck-outs and crosstalk, from $F_{\text{PAM-4_Nyquist}}$ to $F_{\text{NRZ_Nyquist}}$



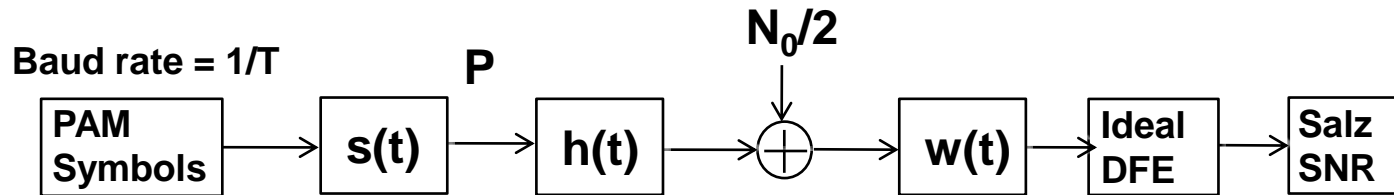
Salz Model



Model Assumptions:

1. Ideal DFE (infinite taps)
2. Matched filter $W(t)$ using ideal FFE (infinite taps)
3. DFE decision errors ignored (i.e. SNR is high enough)
4. Noise is AWGN
5. Nyquist pulse shaping TX filter $S(t)$
6. Exponential loss channel modeled as $H(f) = \exp(-\alpha f)$

Salz Model, cont.



Analytical solution for normalized Mean Square Error (MSE) at output of DFE (Salz SNR bound):

$$SNR = e^{\left[\frac{T}{\pi} \int_0^{\frac{\pi}{T}} \ln \left(\rho e^{-\frac{\alpha \omega}{\pi}} + 1 \right) d\omega \right]}$$

$$\rho = P \cdot T / (N_0/2) = \text{TX SNR}$$

Salz Model, cont.

In the limit of high TX SNR, Taylor series expansion can be used to obtain a remarkably simple formula for Salz SNR:

$$SNR_{dB} = \rho_{dB} - \frac{1}{2} (IL_{f_{NY}})$$

The effective SNR at DFE output is approximately the TX SNR decreased by $\frac{1}{2}$ the IL (channel insertion loss) in dB at the Nyquist frequency.

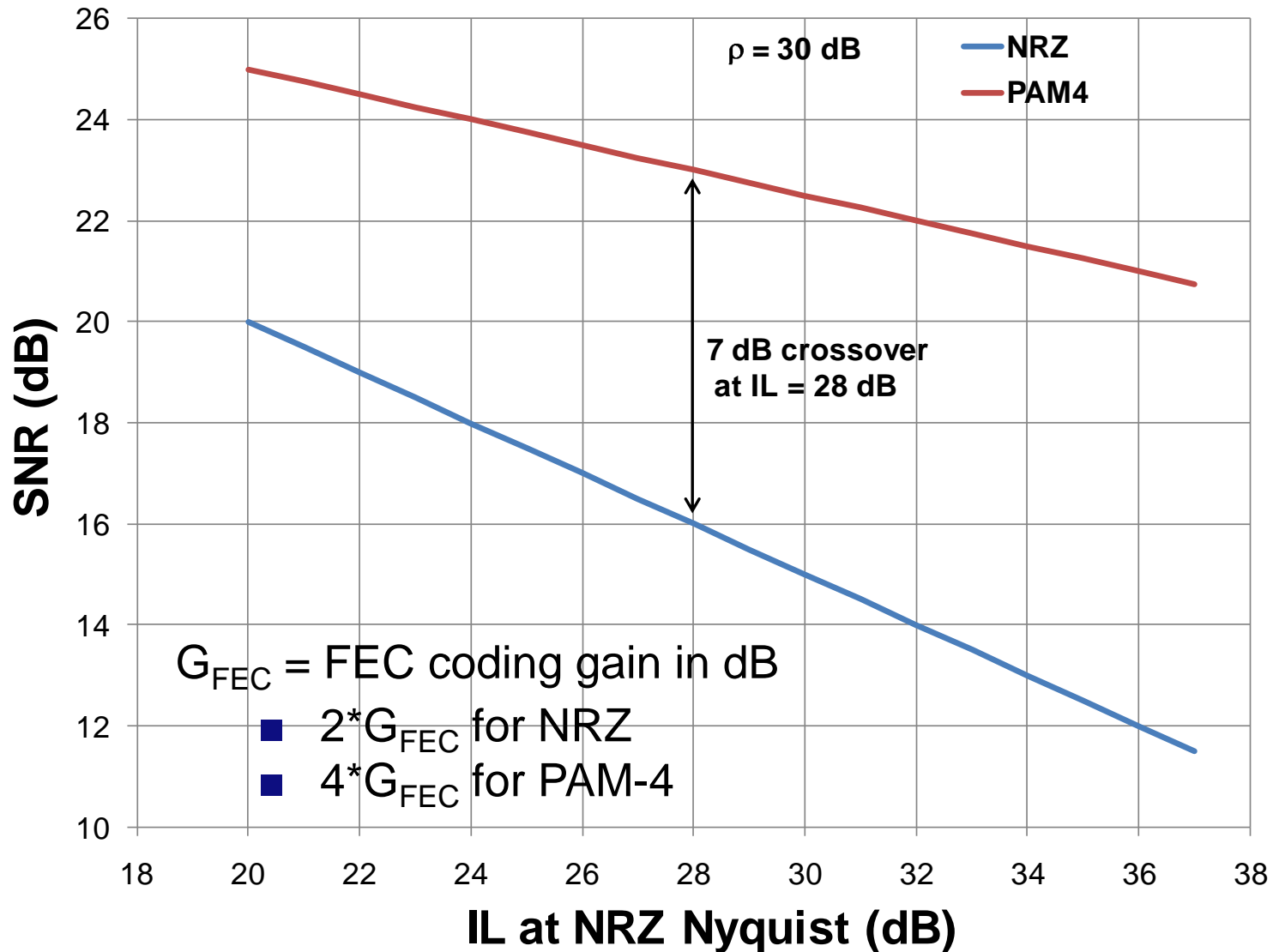
$$f_{NY} = 1 / 2T$$

Salz Model NRZ & PAM-4 Comparison

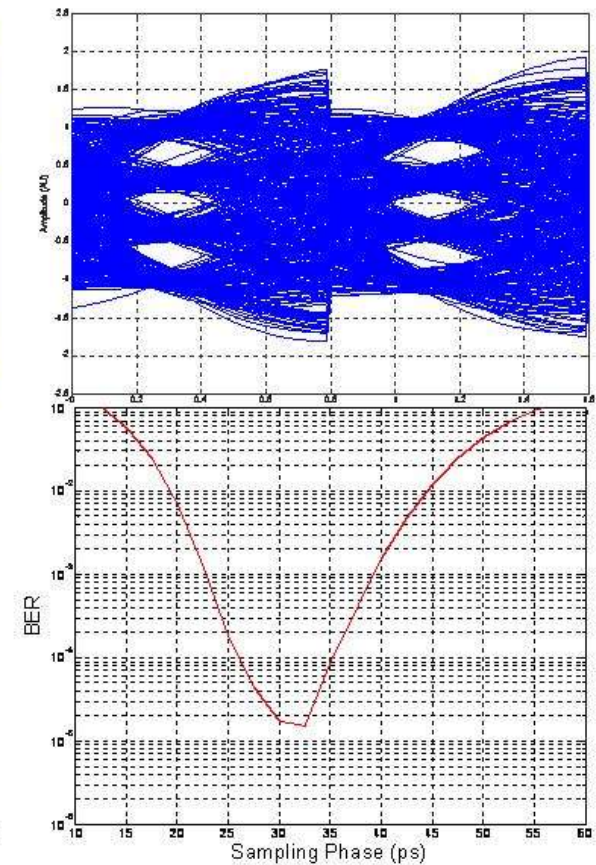
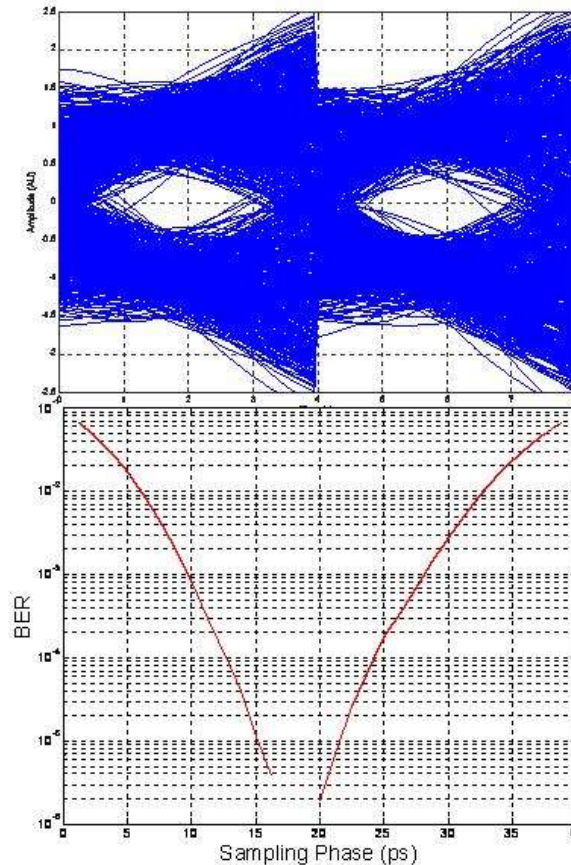
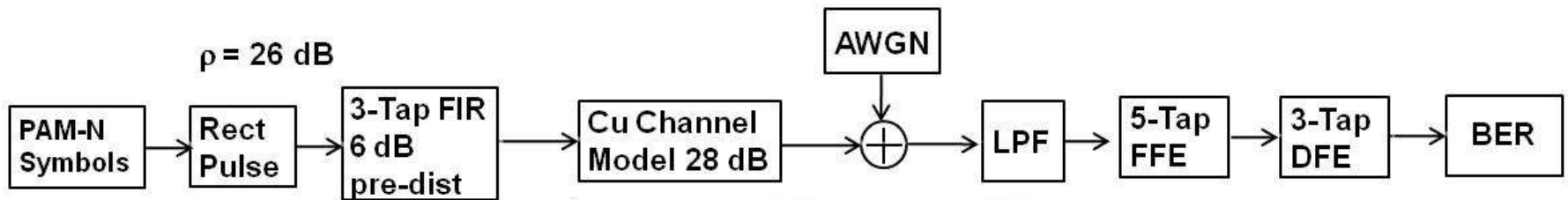
$$SNR_{dB} = \rho_{dB} - \frac{1}{2} (IL_{f_{NY}})$$

- PAM-4 $f_{NY} = \frac{1}{2}$ NRZ f_{NY}
- PAM-4 IL = $\frac{1}{2}$ NRZ IL
- Theoretical NRZ SNR in dB at equal TX SNR:
NRZ SNR = $\frac{1}{4}$ PAM-4 SNR (4x PAM-4 advantage)
- To achieve the same BER:
NRZ SNR = PAM-4 SNR - 7dB (7dB NRZ advantage)
- Therefore PAM-4 is better than NRZ for:
IL > 28dB (i.e. NRZ is better for IL < 28dB)

Salz Model NRZ & PAM-4 Comparison

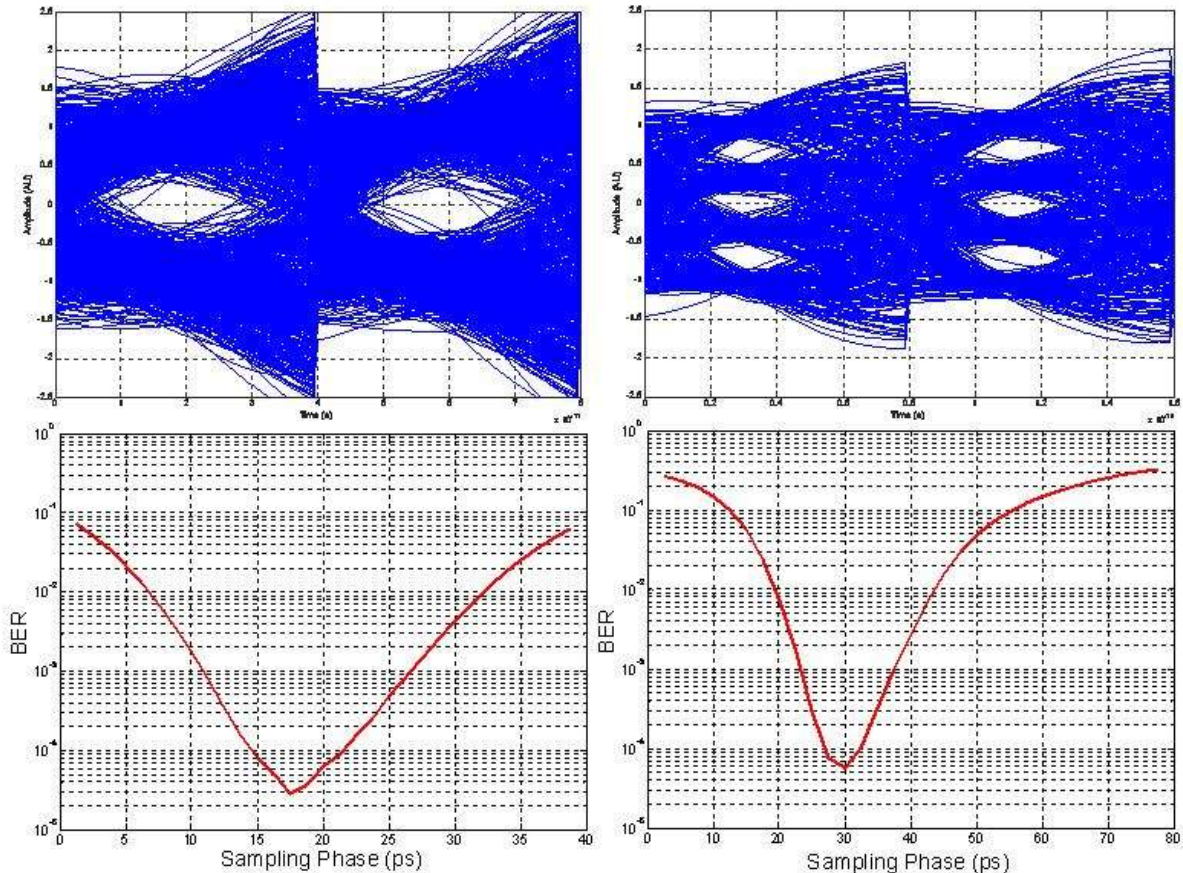
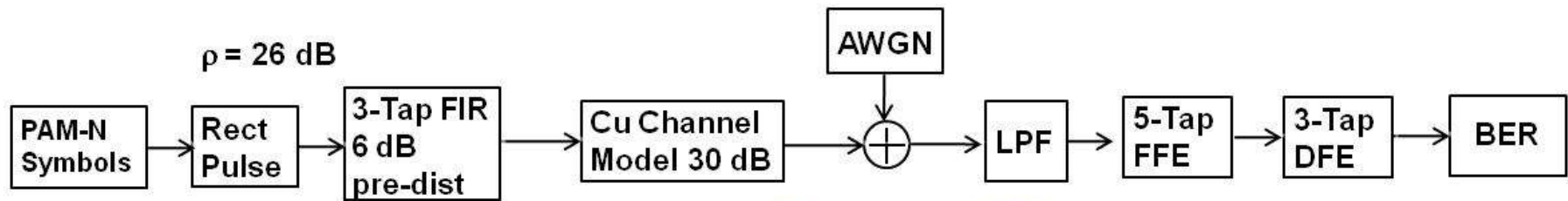


Matlab Model 3: FFE+DFE RX w/ 28dB IL



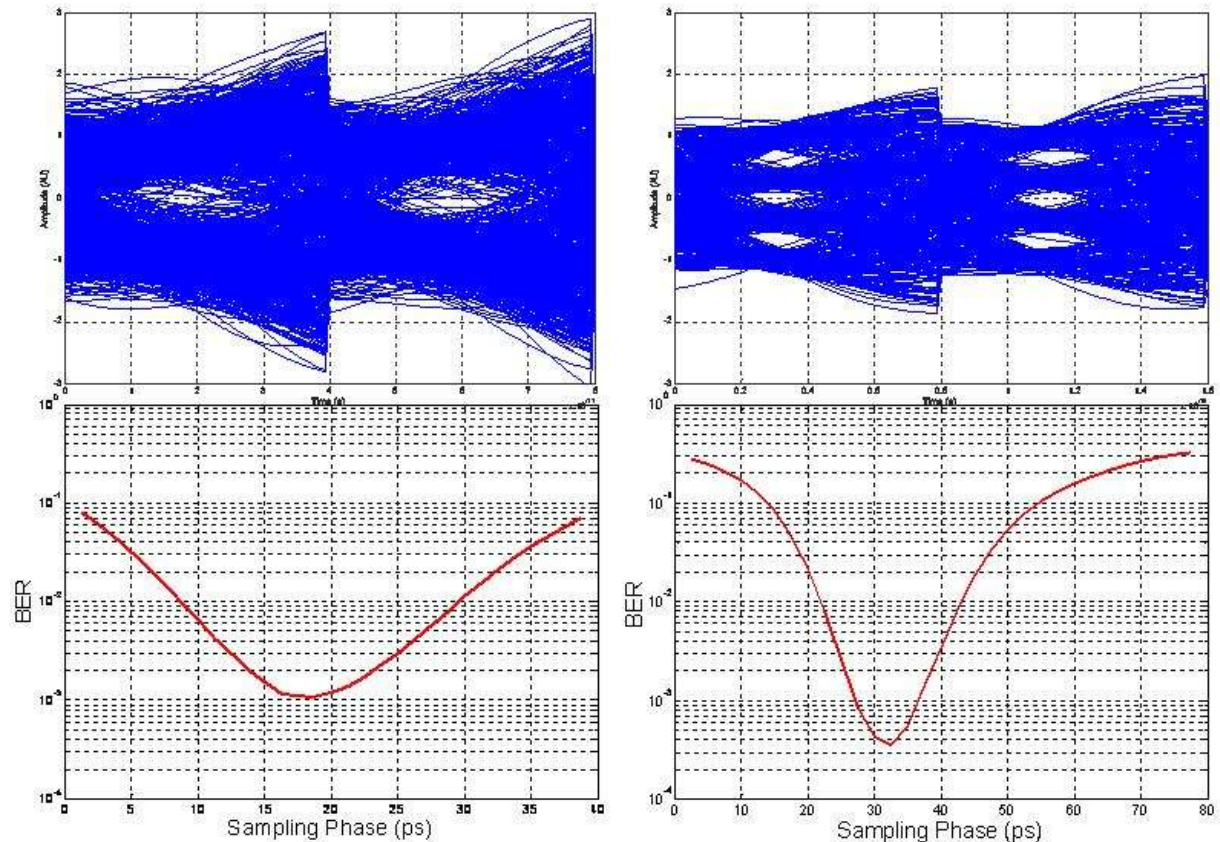
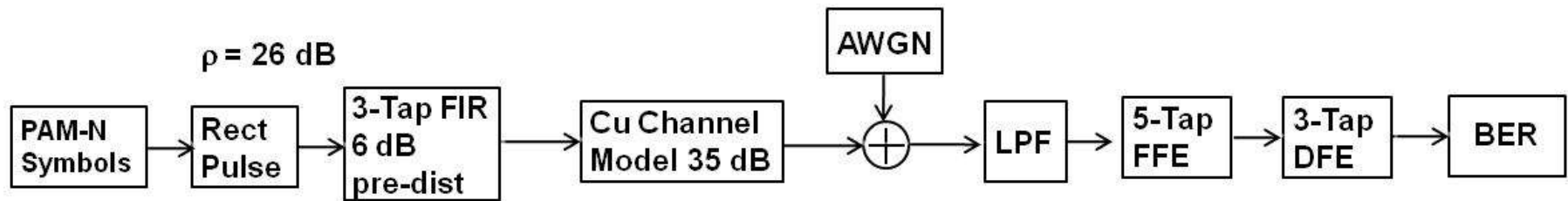
Use of T/2 FFE with higher number of taps will increase the horizontal eye opening.

Matlab Model 4: FFE+DFE RX w/ 30dB IL



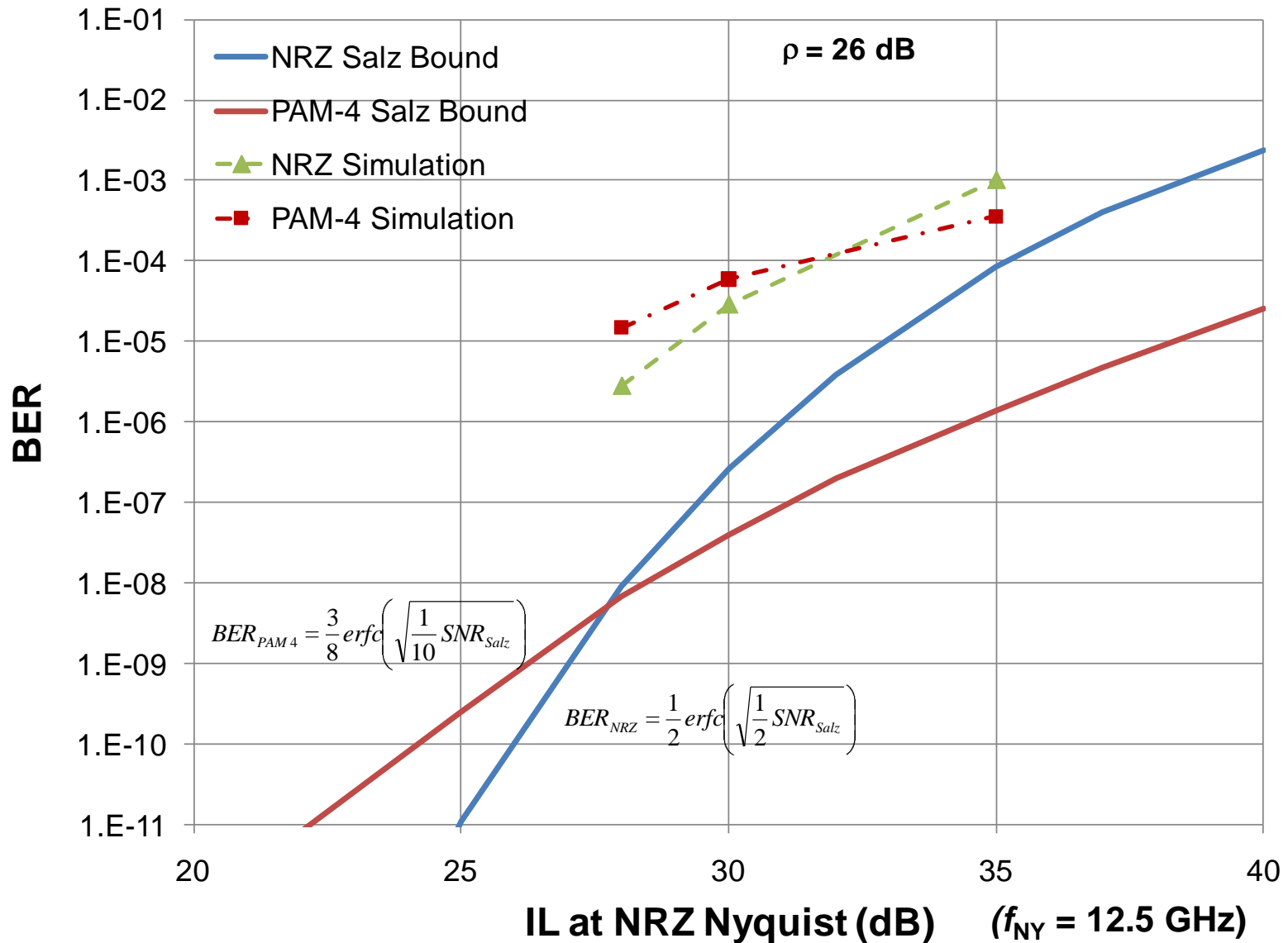
Use of T/2 FFE with higher number of taps will increase the horizontal eye opening.

Matlab Model 5: FFE+DFE RX w/ 35dB IL



Use of T/2 FFE with higher number of taps will increase the horizontal eye opening.

Salz RX & FFE+DFE RX Comparison



Summary Results

- Salz Model over an exponential loss channel shows better PAM-4 versus NRZ performance for:
 - $IL_{12.5\text{GHz}} > 28\text{dB}$ (i.e. NRZ is better for $IL_{12.5\text{GHz}} < 28\text{dB}$)
 - $IL_{12.5\text{GHz}} > 32\text{dB}$ (for moderate FFE+DFE RX Model)
- For $IL \sim 30\text{dB}$, small implementation differences can shift the crossover, explaining conflicting Task Force results
- Salz Model does not include random jitter and timing errors
- PAM-N differences in sensitivity to timing jitter and errors may substantially change the IL crossover value

The timing penalty will be quantified in future work

References

- J. Salz, “Optimum Mean-Square Decision Feedback Equalization,” BSTJ, Vol. 52, No. 8, pp. 1341-1370, April 1973.
- B.L. Kaspar, “Equalization of Multimode Optical Fiber Systems”, BSTJ, Vol. 61, No. 7, pp.1367-1388, Sept. 1982.
- G. Thompson, “How 1000BASE-T Works”, P802.3ab 1000BASE-T Task Force, Nov. 1997,
<http://www.ieee802.org/3/ab/public/nov97/geoff1.pdf>
- C. Mick, et al., “A Tutorial Presentation”, P802.3ab 1000BASE-T Task Force, March 1998,
http://www.ieee802.org/3/tutorial/march98/mick_170398.pdf
- Abler, et al., “PAM-4 versus NRZ Signaling: Basic Theory”, P802.3 Backplane Ethernet Task Force, July 2004,
http://www.ieee802.org/3/ap/public/jul04/abler_01_0704.pdf
- D.G. Kam et al., “Multi-level Signaling in High Density, High Speed Electrical Links”, DesignCon 2008.

References

- D.G. Kam et al. "Is 25 Gb/s On-Board Signaling Viable?," IEEE Trans. Advanced Packaging, vol. 32, no 2, May 2009, pp. 328-344.
- W. Bliss, "Sensitivity to Timing Error Jitter for NRZ and PAM-4", P802.3bj Backplane and Copper Cable Task Force, Nov. 2011, http://www.ieee802.org/3/bj/public/nov11/bliss_01a_1111.pdf
- Q. Gua, et al., "20-Gb/s Single-Feeder WDM-PON Using Partial-Response Maximum Likelihood Equalizer", IEEE Photonics Technology Letters, Vol. 23, No. 23, Dec. 2011, pp. 1802-1804
- References without url are available for download at:
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