

PAM-N Tutorial Material

802.3bj 100 Gb/s Backplane and Copper Cable Task Force

IEEE 802.3 Plenary Session

Waikoloa, HI

12-15 March 2012

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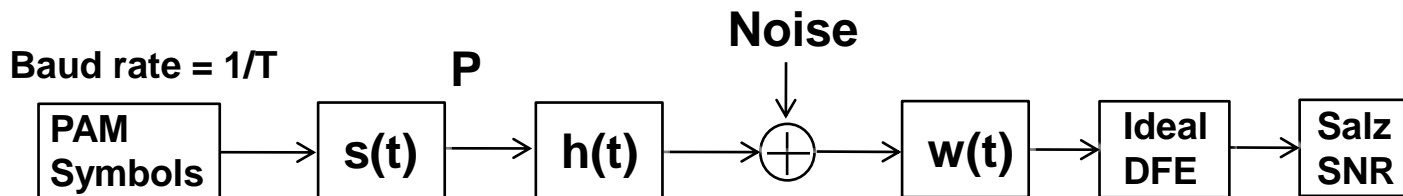
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Outline

- Salz SNR Formula for AWGN Channel
- Salz SNR Formula for Xtalk Channel
- Summary Results
- Conclusions

Salz SNR Model for AWGN Channel



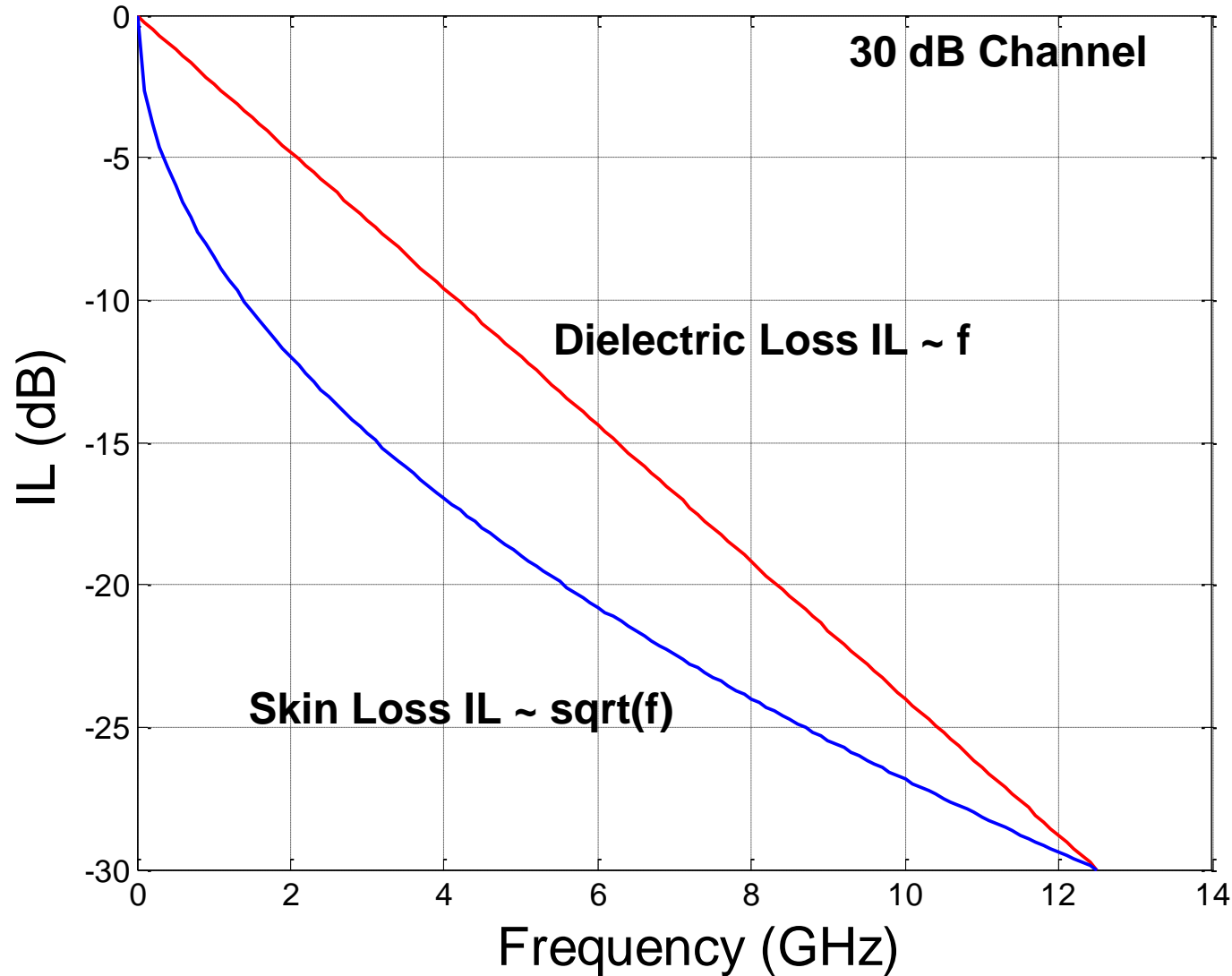
$$SNR = e^{\left[\frac{1}{2T} \int_0^{f_{NY}} \ln(Y(f)+1) df \right]} = e^{\frac{1}{f_{NY}} \int_0^{f_{NY}} \ln(Y(f)+1) df}$$

$$Y(f) = \rho |H(f)|^2$$

$$\rho = \text{Tx SNR}$$

$$IL(f) = 10 \text{Log}_{10}(|H(f)|^2)$$

Channel Insertion Loss Models



SNR Formula

In the limit of high TX SNR, Taylor series expansion results in a simple Salz SNR Formula.

Dielectric loss:
$$SNR_{dB} = \rho_{dB} - \frac{1}{2} (IL_{f_{NY}})$$

Skin loss:
$$SNR_{dB} = \rho_{dB} - \frac{2}{3} (IL_{f_{NY}})$$

IL is evaluated at the Nyquist frequency of each modulation format.

SNR Formula cont.

Salz SNR Formula as a function of IL at NRZ Nyquist:

Dielectric loss:

$$SNR_{dB}^{NRZ} = \rho_{dB} - \frac{1}{2} IL$$

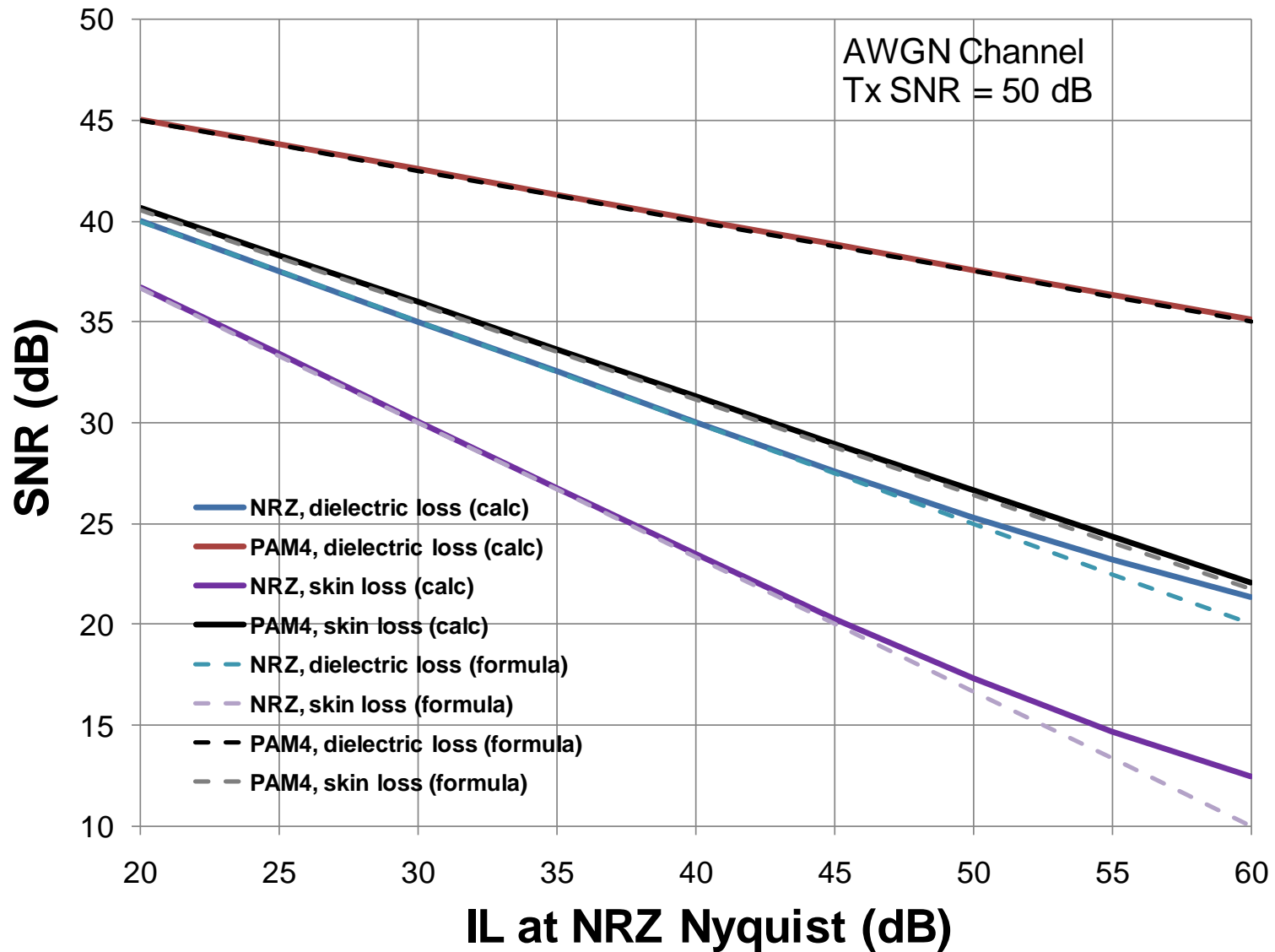
$$SNR_{dB}^{PAM4} = \rho_{dB} - \frac{1}{4} IL$$

Skin loss:

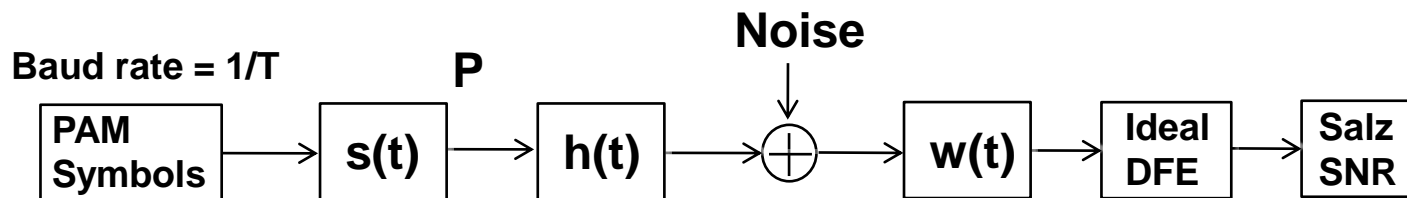
$$SNR_{dB}^{NRZ} = \rho_{dB} - \frac{2}{3} IL$$

$$SNR_{dB}^{PAM4} = \rho_{dB} - \frac{\sqrt{2}}{3} IL$$

SNR Formula & Numeric Calc Comparison



Salz SNR Model for Colored Noise



$$SNR = e^{\left[\frac{1}{2T} \int_0^{f_{NY}} \ln(Y(f)+1) df \right]} = e^{\frac{1}{f_{NY}} \int_0^{f_{NY}} \ln(Y(f)+1) df}$$

$$Y(f) = \frac{P(f)}{N(f)} |H(f)|^2$$

$P(f)$ = signal power spectral density

$N(f)$ = noise power spectral density

Note when $N(f)$ is due to Xtalk, then $Y(f)=ICR(f)$

Salz SNR Model for Xtalk Channel

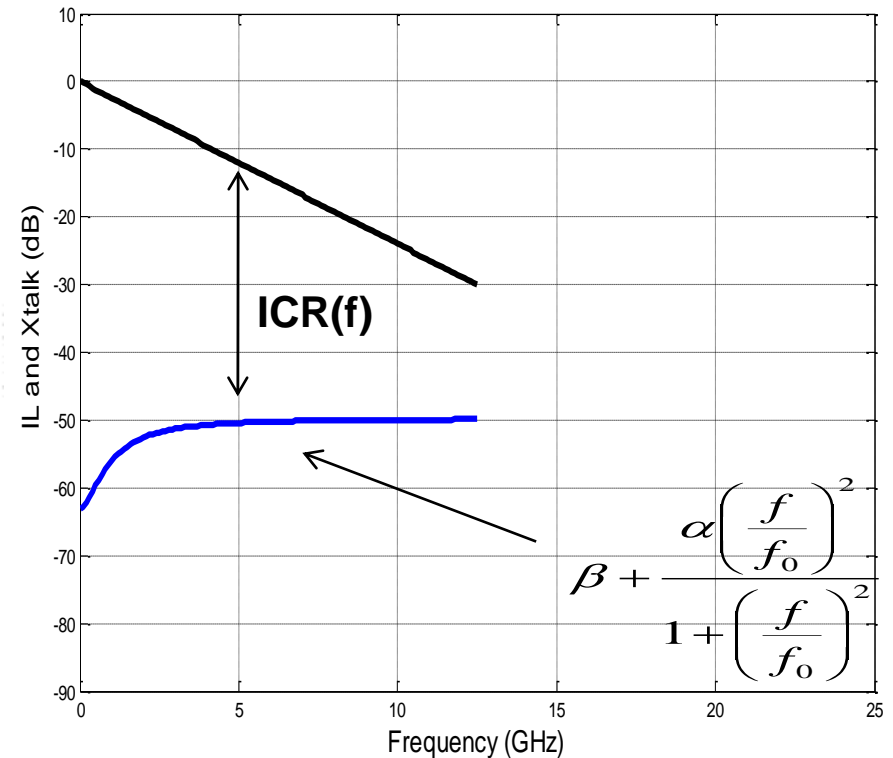
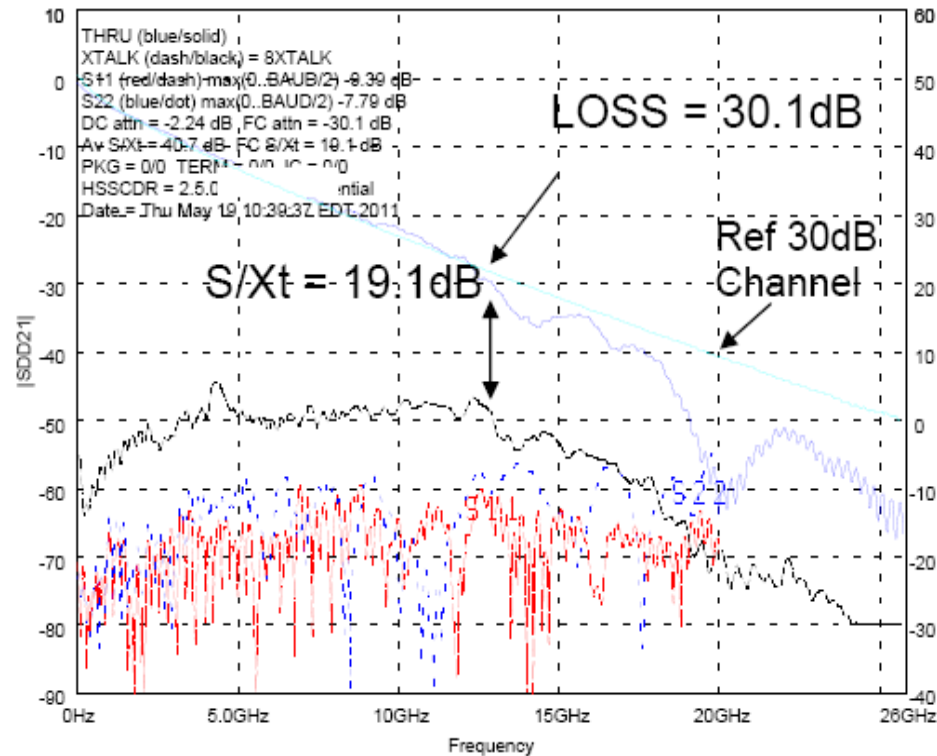
$$SNR_{dB} = \frac{1}{f_{NY}} \int_0^{f_{NY}} 10 \log 10(Y(f) + 1) df = \langle (Y(f) + 1)_{dB} \rangle$$

$$Y(f) = \frac{P(f)}{N(f)} |H(f)|^2 = ICR(f)$$

Xtalk Model Example

IBM measured 30 dB channel (beukema_01a_0911)

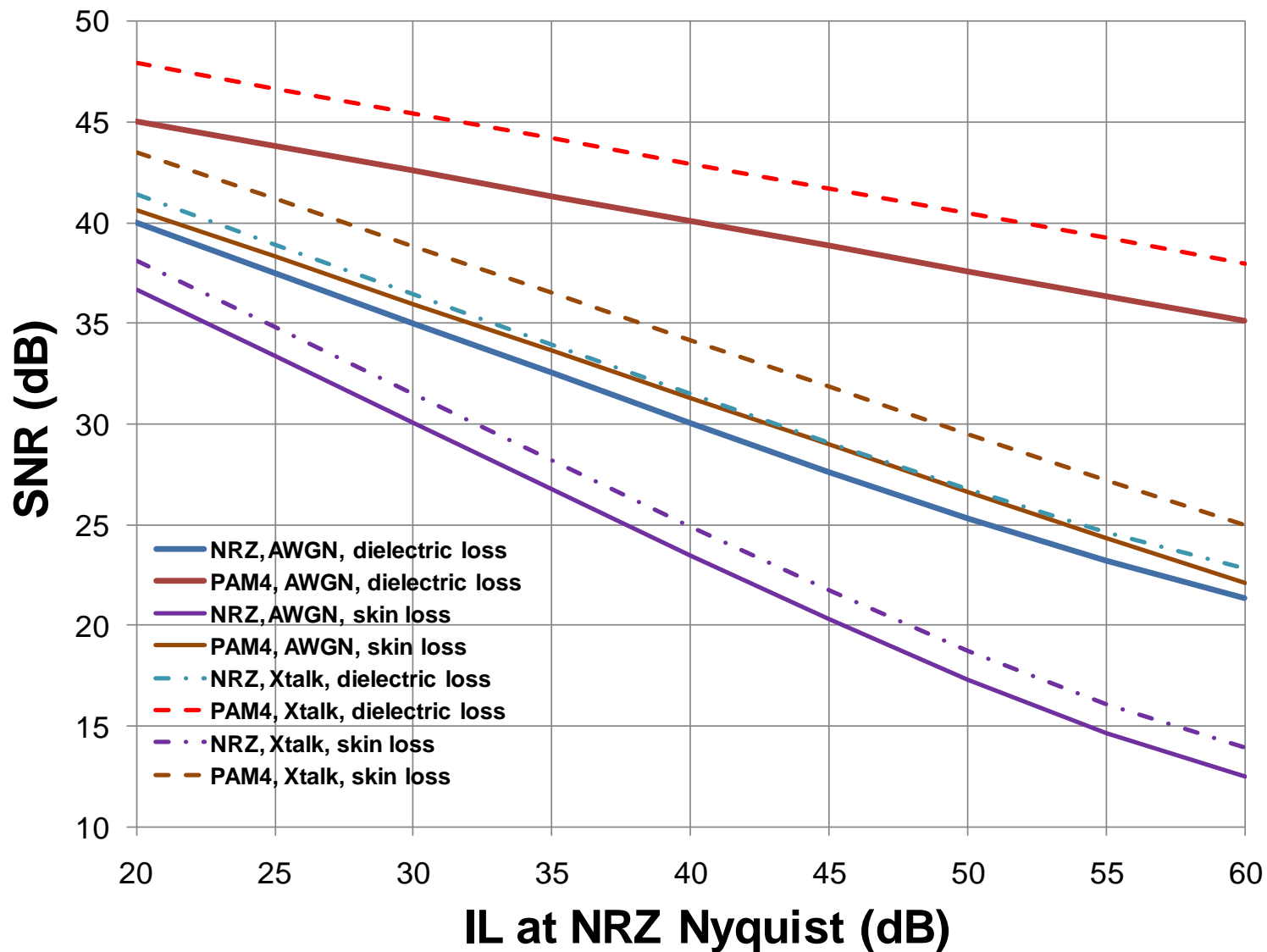
Xtalk Model



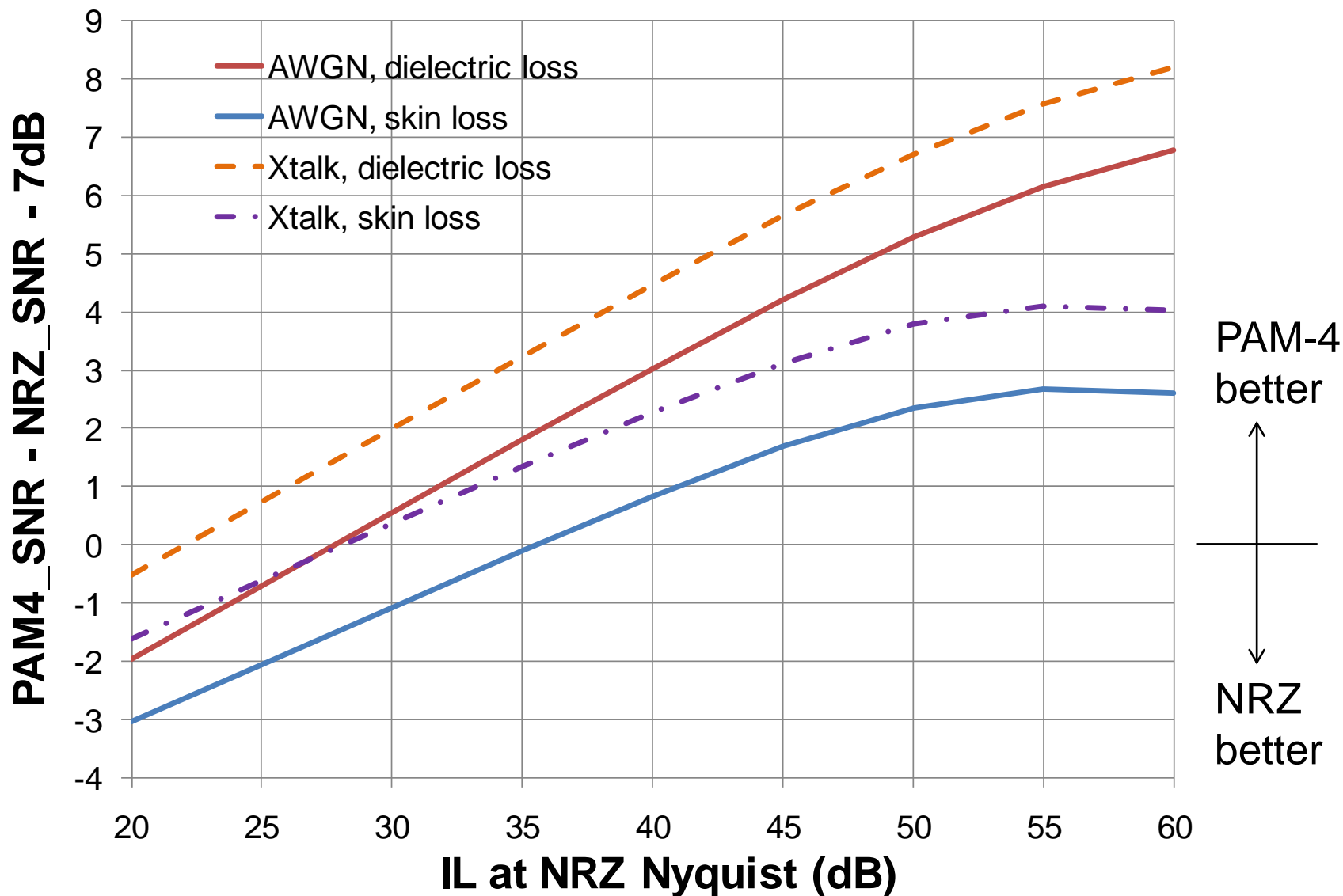
Model Parameters:

$f_0=2\text{GHz}$, $\alpha=1.e-5$, $\beta=5.e-7$

SNR Formula for AWGN & Xtalk Channels



Δ SNR Formula Comparing NRZ & PAM-4



Conclusions

- Salz Formula for AWGN channel predicts better PAM-4 versus NRZ performance for:
 - $IL_{12.5\text{GHz}} > 28\text{dB}$ (dielectric loss limited channel)
 - $IL_{12.5\text{GHz}} > 35\text{dB}$ (skin loss limited channel)
- Salz Formula for Xtalk example channel predicts better PAM-4 versus NRZ performance for:
 - $IL_{12.5\text{GHz}} > 22\text{dB}$ (dielectric loss limited channel)
 - $IL_{12.5\text{GHz}} > 28\text{dB}$ (skin loss limited channel)