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Dk & Df ALGEBRAIC MODEL v2.01

Let's take a look...

WHAT YOU WILL SEE

NOTE: The Change Parameter window is a visual basic macro.
If you save the file to your computer, be sure to select the Maco-Enabled file type.

LOOK & FEEL

Quick preview of select frequencies

CHANGE PARAMETERS

Click to change the input parameters

See the connector & channel loss at specific frequencies

Fitted equation(s):
 $Dk(f) = c2*f^2 + c1*f + b$

Version 2.01 LOSS SNAPSHOT: Loss at 5GHz: 23.79 dB			Loss at 12.75GHz: 56.54 dB			Loss at 14GHz: 61.66 dB		
Backplane/Trace Material			Linecard A Material			Linecard B Material		
Length (inch)	20		Length (inch)	2		Length (inch)	18	
Trace Width (mil)	8		Trace Width (mil)	6		Trace Width (mil)	5	
Cu Thickness (mil)	0.6		Cu Thickness (mil)	0.6		Cu Thickness (mil)	0.6	
Diel. Thickness (mil)	16		Diel. Thickness (mil)	12.9		Diel. Thickness (mil)	11.1	
Freq	Dk	Df	Freq	Dk	Df	Freq	Dk	Df
1.00E+08	3.67	0.0039	1.00E+08	3.6	0.0092	1.00E+08	3.6	0.0092
1.00E+09	3.65	0.004	1.00E+09	3.6	0.0092	1.00E+09	3.52	0.0115
2.00E+09	3.59	0.0043	2.00E+09	3.5	0.0115	2.00E+09	3.49	0.0108
5.00E+09	3.576	0.0049	5.00E+09	3.5	0.0115	5.00E+09	3.46	0.011
1.00E+10	3.3494	0.0055	1.00E+10	3.4	0.0125	1.00E+10	3.44	0.0112
2.00E+10	3	0.0065	2.00E+10	3.2	0.014	2.00E+10	3.43	0.0114
Low Roughness	20	6.0E-07	High Roughness	65	6.0E-07	High Roughness	65	6.0E-07

Version 2.01	Frequency (GHz)	Dielectric Constant	Loss Tangent
0	0	2.2	0.004
0	1	2.3	0.0045
0	2	2.4	0.005
0	3	2.5	0.0055
0	4	2.6	0.006
0	5	2.7	0.0065
0	10	3.1	0.008
0	20	3.5	0.011

Version 2.01	Frequency (GHz)	Dielectric Constant	Loss Tangent
0	0	3.45	0.008
0	1	3.5	0.009
0	2	3.55	0.01
0	3	3.5	0.011
0	4	3.45	0.012
0	5	3.4	0.013
0	10	3.5	0.014
0	20	3.6	0.015

Version 2.01	Frequency (GHz)	Dielectric Constant	Loss Tangent
0	0	3.55	0.008
0	1	3.5	0.009
0	2	3.45	0.01
0	3	3.4	0.011
0	4	3.45	0.012
0	5	3.5	0.013
0	10	3.6	0.014
0	20	3.6	0.015

DK fit to Second Order Equation	c2	c1	b
DK fit to Second Order Equation	3.672198659	-3.82611E-24	2.075E-13
Df fit to Second Order Equation	0.003870352	0.003870352	0.003870352

DK fit to Second Order Equation	c2	c1	b
DK fit to Second Order Equation	3.64774E-23	-2.02392E-11	3.591963577
Df fit to Second Order Equation	0.009448676	-1.15209E-23	4.54439E-13

DK fit to Second Order Equation	c2	c1	b
DK fit to Second Order Equation	0.0102537	0.0102537	0.0102537

Zo	Conn. Loss	A _{tot} (dB)
48.06984334	0.0283	0.8099
48.07668132	0.0630	0.8454

NOTE: The Change Parameter window is a visual basic macro. If you are having issues opening this window, consider Microsoft button > Excel Options > Trust Center > Trust Center Settings > Macro Settings

Enter Parameters for the Material

Setup | Backplane | Line Card

Single Trace Only

Backplane w/ 2 Connectors, 1 Material

Backplane w/ 2 Connectors, Different Materials

First select your configuration

Enter Parameters for the Material

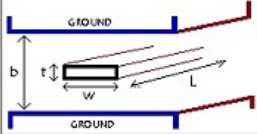
Setup | Backplane | Line Card

All fields must be completed. Backplane/Trace Material:

	Dk (real)	Df
100M	3.67	0.0039
1G	3.65	0.004
2G	3.59	0.0043
5G	3.576	0.0049
10G	3.3494	0.0055
20G	3	0.0065

CU Roughness: Low Med High

Want to auto-fill? Meg6, -135I, Imp FR4, Copy Mat. to Linecard



If applicable, the same b, and t form used for line material ent

b, Dielectric Thickness (mils): 16 w, Trace Width (mils):
L, Trace Length (inches): 20 t, Cu Thickness (mils):

Include 2 connectors

Since you selected Trace Only, please select OK to get your loss calculator

OK Clear

The appropriate tabs will become live.

Enter Parameters for the Material

Setup | Backplane | Line Card

All fields must be completed. Line/Daughter Card #1 Material:

	Dk (real)	Df
100M	3.6	0.0092
1G	3.6	0.0092
2G	3.5	0.0115
5G	3.5	0.0115
10G	3.4	0.0125
20G	3.2	0.014

CU Roughness: Low Med High

Want to auto-fill? Meg6, -135I, Imp FR4

b, Dielectric Thickness (mils): 12.9 w, Trace Width (mils): 6
L, Trace Length (inches): 2 t, Cu Thickness (mils): 0.6

Line/Daughter Card #2 Material: Use same as LC #1

	Dk (real)	Df
100M		
1G		
2G		
5G		
10G		
20G		

CU Roughness: Low Med High

b, Dielectric Thickness (mils): w, Trace Width (mils): 6
L, Trace Length (inches): 2 t, Cu Thickness (mils): 0.6

OK Clear

Shortcut if you want both daughter cards of the same material.

All values must be filled in before you press OK.

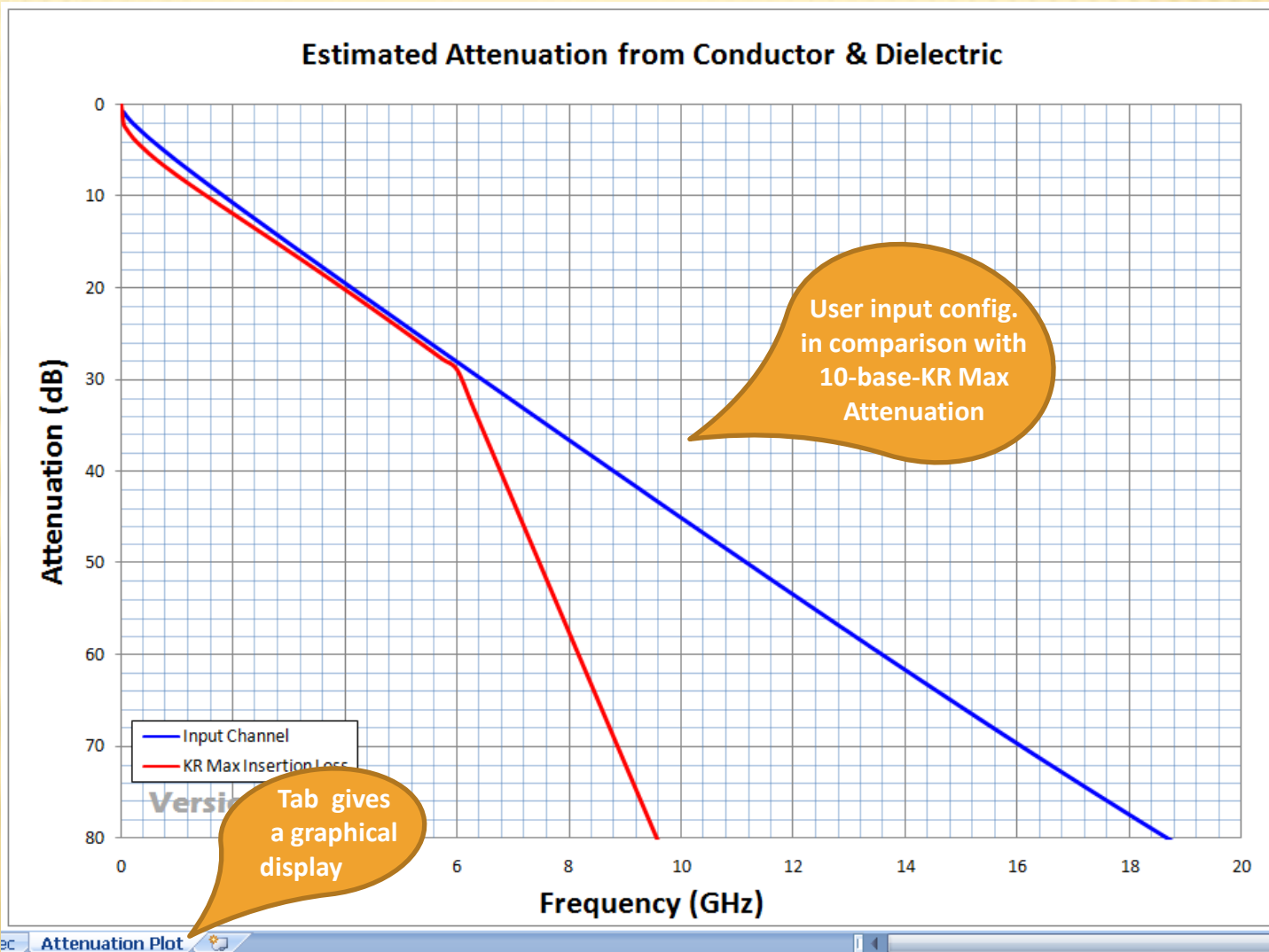
Order Equation	b	3.67219659	2 conn	Order Equation	b	3.591963577
Df fit to Second	d	-3.62611E-24		Df fit to Second	d	-1.15209E-23
Order Equation	d	2.075E-13		Order Equation	d	4.54438E-13
	b	0.003870952			b	0.009448676

Zo

43.06984334 43.55672188

43.07668132 43.56230717

LOOK & FEEL



Behind the Scenes...

EQUATIONS AND REFERENCES OF MODEL

FREQUENCY DEPENDENCE

- ✘ 6 input frequency points for D_k and D_f
- ✘ Fit D_k and D_f to second order equations
 - + Coefficients shown on sheet
 - + Graphical representation shown on sheet
- ✘ Note that frequency dependence fit is only approximated to 20G, therefore, loss approximations should only be considered to 20G
- ✘ Z_0 is calculated with D_k (or ϵ_r) at a given frequency; a similar technique is used in loss calculations

DK & DF SECOND ORDER EQUATIONS

- ✘ Second order approximation is created using the LINEST function. This function essentially fits a 2nd order polynomial to the 6 frequency points given; resulting in

$$D_k = c_2 * f^2 + c_1 * f + b$$

- ✘ Function as implemented in the spreadsheet:

LINEST(C8:C13,B8:B13^[1,2])

Y Values
(Dk entered points)

X Values
(Freq. associated
w/ entered points)

Exponents of X;
Creating a second
order equation.

- ✘ See Excel HELP for more details on LINEST function. Methodology verified against “add trend line” within plot.

CHARACTERISTIC IMPEDANCE [2, EQU 4-5]

$$Z_0 = \frac{94.15}{\sqrt{\epsilon_r} \left(\frac{\frac{w}{b}}{1-t} + \frac{c'_f}{0.0885\epsilon_r} \right)} \text{ ohms}$$

$$c'_f = \frac{0.0885\epsilon_r}{\pi} \left\{ \frac{2}{1-\frac{t}{b}} \log_e \left(\frac{1}{1-\frac{t}{b}} + 1 \right) - \left(\frac{1}{1-\frac{t}{b}} - 1 \right) \log_e \left(\frac{1}{\left(1-\frac{t}{b}\right)^2} - 1 \right) \right\}$$

ϵ_r = relative dielectric constant (at a given frequency)

b = platespacing (mil)

w = trace width (mil)

t = trace thickness (mil)

c'_f = fringing capacitance ($\mu\text{f}/\text{cm}$) * assuming semi - infinite plate between two infinite ground planes, but good approximation for $w/(b - t) \geq 0.35$

Unchanged from v1.01

ATTENUATION IN LOSSY LINES

Unchanged
from v1.01

- ✘ Attenuation per length^[1, EQN 9-54]:

$$\alpha_n = \sqrt{\frac{1}{2} \left[\sqrt{(R_L^2 + \omega^2 L_L^2)(G_L^2 + \omega^2 C_L^2)} - \omega^2 L_L C_L + R_L G_L \right]} \text{ nepers/length}$$

- ✘ Using a low-loss approximation^[1, EQN 9-55]: (surface roughness ignored)

$$\alpha_n = \frac{1}{2} \left(\frac{R_L}{Z_0} + G_L Z_0 \right) \text{ nepers/length}$$

- ✘ But we don't typically discuss in nepers...^[1, EQN 9-57]

$$10^{\frac{\alpha_{dB}}{20}} = e^{\alpha_n} \quad \therefore \alpha_{dB} = 20 \log_{10} e \times \alpha_n$$

for ease of notation: $Y_{n \rightarrow dB} = 20 \log_{10} e$

CONDUCTOR LOSS (per inch)

$$\alpha_{cond} = (Y_{n \rightarrow dB}) \times \frac{R_L}{Z_0} \quad \begin{cases} \alpha_{cond} = \text{attenuation of amplitude due to conductor loss, in dB/length}^{[1, EQN 9-59]} \\ Y_{n \rightarrow dB} = \text{conversion from nepers to dB} \\ R_L = \text{resistance per length of conductor} \\ Z_0 = \text{characteristic impedance} \end{cases}$$

- ✘ Skin effect, ground resistance, and stripline effect are accounted for in resistance^[3, EQNs 4.3a-4.10]:

- R of signal trace & return path (w/skin effect)

$$R_{signalCu \text{ skin effect}} = \frac{\sqrt{\pi \mu \rho f}}{w} \quad R_{groundCu \text{ skin effect}} = \frac{\sqrt{\pi \mu \rho f}}{6H}$$

- AC surface resistance for microstrip (or 1 side of a stripline trace)

$$R_{ac \text{ microstrip}} = R_{signal} + R_{ground}$$

CONDUCTOR LOSS (per inch)

- Stripline approximation assumes parallel resistance of top and bottom microstrip approximations

$$R_L = \frac{\left[\sqrt{\pi\mu\rho f} * \left(\frac{1}{w} + \frac{1}{6H} \right) \right]^2}{2 * \left[\sqrt{\pi\mu\rho f} * \left(\frac{1}{w} + \frac{1}{6H} \right) \right]}$$

}

R_L = stripline surface resistance (Ω/inch)

w = width of trace (inch)

H = height dielectric from ground to signal (inch)

μ = permeability of Cu $\approx 4\pi \times 10^{-7} \times 0.999994 \frac{\text{H}}{\text{m}}$

ρ = resistivity of Cu = $\frac{1}{\sigma} = \frac{1}{5.96 \times 10^7} \Omega \text{ m}$

f = frequency (hertz)

- ✘ Conductor loss per inch as entered in the model:

$$\alpha_{cond} = \frac{1}{2} \times (20 \log_{10} e) \times \left(\frac{\left[\sqrt{\pi\mu\rho f} * \left(\frac{1}{w} + \frac{1}{6H} \right) \right]}{2} \right) \times \frac{1}{Z_0}$$

DIELECTRIC LOSS (per inch)

$$\alpha_{diel} = (Y_{n \rightarrow dB}) \times G_L Z_0$$

$$\left\{ \begin{array}{l} \alpha_{cond} = \text{attenuation of amplitude due to dielectric loss, in dB/length}^{[1, EQN 9-60]} \\ Y_{n \rightarrow dB} = \text{conversion from nepers to dB} \\ G_L = \text{shunt conductance per length from dielectric} \\ Z_0 = \text{characteristic impedance} \end{array} \right.$$

**Unchanged
from v1.01**

✘ As developed by Bogatin...

$$G_L = \omega \tan(\delta) C_L$$

$$Z_0 = \frac{\sqrt{\epsilon_r}}{c C_L}$$

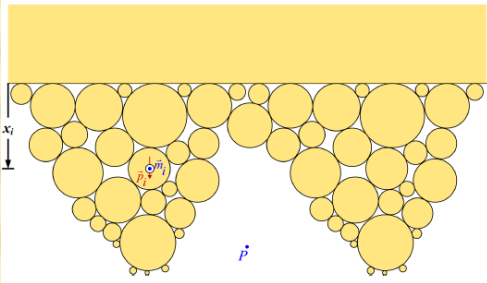
$$\left\{ \begin{array}{l} G_L \text{ equation}^{[1, EQN 9-19, EQN 9-60]} \\ Z_0 \text{ equation}^{[1, EQN 9-67]} \text{ is used to cancel the capacitance value,} \\ \text{the } Z_0 \text{ value for a given frequency is NOT used} \\ c = \text{speed of light m/s} \therefore \text{conversion m} \rightarrow \text{in. is needed} \end{array} \right.$$

✘ Dielectric loss per inch as entered in the model:

$$\alpha_{diel} = \frac{1}{2} \times (20 \log_{10} e) \times (2\pi f \times D_f) \times \frac{\sqrt{\epsilon_r}}{299792458 * 39.37}$$

SURFACE ROUGHNESS (multiplier)

- ✘ Through the snowball method (Huray Model^[4, CHAP 6]), surface roughness is approximated as a collection of smaller spheres. *Note image shows non-uniform “snowballs”... model approximates using uniform spheres.



- ✘ Applied to trace: $\alpha_{total} = \alpha_{diel} + k_{snowball} \alpha_{cond(smooth)}$
- ✘ Surface roughness multiplier as entered in the model:

$$k_{snowball} \approx 1 + \frac{3}{2} \sum_{i=1}^j \frac{\left(\frac{N_i 4\pi a_i^2}{A_{flat}} \right)}{\left(1 + \frac{\delta}{a_i} + \frac{\delta^2}{2a_i^2} \right)}$$

$$\left\{ \begin{array}{l} a_i = \text{radius of spheres (m)} \\ N_i = \text{number of snowballs of size } a_i \text{ per } A_{flat} \\ A_{flat} = \text{total area containing stacked snowballs} \\ \delta = \text{skin depth (m)} \quad \dots \text{ recall : } \delta = \frac{1}{\sqrt{\pi \mu \sigma f}} \end{array} \right.$$

CONNECTOR LOSS & CHANNEL LOSS

- ✘ Attempting to base on 25G technology connectors
- ✘ Used connector models from multiple vendors to draw this max* connector loss... used in model:

$$IL_{conn} = 9 * 10^{-6} * \sqrt{f} - 1.2 * 10^{-12} * f + 1.6 * 10^{-21} f^2$$

* Max loss when ignoring majority of ILD. Idea was to create equation that production connectors can beat. Note that this creates additional error in comparing model to measured, however, model should error in pessimistic direction. Connector implementation likely to be changed in future versions.

- ✘ Equation gives loss of: 0.6164dB @5G; 1.133dB @12.89G; 1.21dB @14G
- ✘ **OVERALL CHANNEL LOSS EQUATION:** (simple enough, right?)

$$A_{total} = a_{LCA_total} * L_{LCA} + IL_{conn} + a_{BP_total} * L_{BP} + IL_{conn} + L_{LCB_total} * L_{LCB}$$

REFERENCES

- [1] E. Bogatin. *Signal Integrity – Simplified*. Pearson Education, Inc., 2004. ISBN 0-13-066946-6.
- [2] S. B. Cohn. “Problems in Strop Transmission Lines.” *IRE Trans. Microwave Theory and Techniques*, Vol. MTT-3, March, 1955, pp 119-126.
- [3] S. H. Hall, G.W.Hall, J. A. McCall. *High-Speed Digital System Design: A Handbook of Interconnect Theory and Design Practices*. John Wiley & Sons, Inc., 2000. ISBN-10 0471360902.
- [4] P. G. Huray. *The Foundations of Signal Integrity*. John Wiley & Sons, Inc., 2010. ISBN-978-0-470-34360-9

TRACKING THE CHANGES

Version	Change
1.01	9/26/2011 – Initial release – second order Dk & Df approximation, track user input channel along with Meg-6 & Improved FR-4 for given length/width/thickness, 3 materials compared to KR limit line.
2.01	12/15/2011 – surface resistance updated to include return path resistance and stripline approximation, Huray model for surface roughness added, “worst-case” connector added, partitioning option added (backplane w/2 daughter cards), KR limit comparison made to attenuation max (instead of IL)