# 2-D Marker Sequences 

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## Introduction

- Burst Markers (BM) indicate start and end of an upstream OFDMA burst.
- Usage:
- Length of burst
- Number of LDPC codeword and type (long, medium, short)
- Profiles


## Assumptions

- BM are transmitted after ranging and are pre-equalized
- First element of BM is time aligned with RB. BM search is in frequency direction, down to the RB.
- RB are 1,4 or 8 subcarriers by M symbols. $\mathrm{M}>=4$
- BM can span across multiple RB (to allow BM larger than one RB).
- BM can span across OFDMA frame (needed when BM is larger than one RB).
- End and Start BM are usually separated by one or more RB of silence (idle)
- Not for BM detection but to prevent collision from time granularity of the 1-D to 2-D mapping
- BM detection must not be impaired by idle


## 2-D Marker Sequences Properties

- Exploit the 2-D structure of OFDMA
- K subcarriers by L symbols
- Ternary signaling, $\mathrm{P}=-1$ or $1, \mathrm{~N}=0$
- Ease the differentiation of BM from data
$-N$ in the BM allow boosting of $P$ without increasing total output power
- Good auto-correlation and cross-correlation for a large set of sequences


## 2-D Marker Sequences Properties

- Detection is by power averaging of " P " and " N " at the assumed locations
- Additional information can be carried by the BPSK "P" symbols like:
- Start
- End
- Profile
- Idle RB between BM could be used to differentiate between Start and End BM at RX
- Square $B M$ : $K=L$, where $K$ is an even integer
- K/2 Nulls RE in each row and column


## 2-D Marker Sequences Properties

- Non square BM: $\mathrm{K}=\mathrm{L}-1$, where K is an odd integer
- $(K+1) / 2$ Nulls in each row
- (K-1)/2 or ( $\mathrm{K}+1$ )/2 Nulls in each column
- Logical NOT ( $\mathrm{P} \rightarrow \mathrm{N}, \mathrm{N} \rightarrow \mathrm{P}$ ) of a sequence is an orthogonal sequence to the original sequence.
- Many sequences with good auto-correlation to choose from:
$-4 \times 4 \rightarrow 8$ sequences
$-5 \times 6 \rightarrow 10080$ sequences
$-6 x 6 \rightarrow 64$ sequences
$-8 \times 8 \rightarrow 256$ sequences


## Interleaving

- 2-D Burst Marker sequences can be interleaved with the data if the 2-D structure is kept intact
- Examples of $4 \times 4 \mathrm{BM}$ interleaving:

| 0 | $D P$ | 1 | $D P$ | 0 | $D P$ | 1 | $D P$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $D P$ | 1 | $D P$ | 0 | $D P$ | 1 | $D P$ | 0 |
| 0 | $D P$ | 1 | $D P$ | 1 | $D P$ | 0 | $D P$ |
| $D P$ | 1 | $D P$ | 0 | $D P$ | 0 | $D P$ | 1 |
| $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ |
| $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ |
| $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ |
| $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ |

Time

| 0 | $D P$ | 1 | $D P$ | 0 | $D P$ | 1 | $D P$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ |
| $D P$ | 1 | $D P$ | 0 | $D P$ | 1 | $D P$ | 0 |
| $D$ | $D$ | $D$ | $D$ |  | $D$ |  |  |
| $D$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ |  |
| 0 | $D P$ | 1 | $D P$ | 1 | $D P$ | 0 | $D P$ |
| $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ |
| $D P$ | 1 | $D P$ | 0 | $D P$ | 0 | $D P$ | 1 |
| $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ |

Time \& Frequency

| 0 | 1 | 0 | 1 | $D P$ | $D P$ | $D P$ | $D P$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ |
| 1 | 0 | 1 | 0 | $D P$ | $D P$ | $D P$ | $D P$ |
| $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ |
| 0 | 1 | 1 | 0 | $D P$ | $D P$ | $D P$ | $D P$ |
| $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ |
| 1 | 0 | 0 | 1 | $D P$ | $D P$ | $D P$ | $D P$ |
| $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ | $D P$ |

Frequency
" 1 " is location of BPSK ( P ), " 0 " is location of Nulls ( N ), "DP" is Data or Pilot RB are shown with lowest frequency at top, highest at bottom

## 2-D BURST MARKER SEQUENCE EXAMPLES AND CORRELATION

## 2-D 4X4 Sequences

| 0 | 1 | 0 | 1 |
| :--- | :--- | :--- | :--- |
| 1 | 0 | 1 | 0 |
| 0 | 1 | 1 | 0 |
| 1 | 0 | 0 | 1 |

BM4x4_1

| 1 | 0 | 0 | 1 |
| :--- | :--- | :--- | :--- |
| 0 | 1 | 1 | 0 |
| 0 | 1 | 0 | 1 |
| 1 | 0 | 1 | 0 |

BM4x4_5

| 0 | 1 | 0 | 1 |
| :--- | :--- | :--- | :--- |
| 1 | 0 | 1 | 0 |
| 1 | 0 | 0 | 1 |
| 0 | 1 | 1 | 0 |

BM4x4_2


| 0 | 1 | 1 | 0 |
| :--- | :--- | :--- | :--- |
| 1 | 0 | 0 | 1 |
| 0 | 1 | 0 | 1 |
| 1 | 0 | 1 | 0 |

BM4x4_3

| 0 | 1 | 1 | 0 |
| :--- | :--- | :--- | :--- |
| 1 | 0 | 0 | 1 |
| 1 | 0 | 1 | 0 |
| 0 | 1 | 0 | 1 |

BM4x4_4

| 1 | 0 | 1 | 0 |
| :--- | :--- | :--- | :--- |
| 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | 0 |
| 1 | 0 | 0 | 1 |
| BM4x4_7 |  |  |  |


| 1 | 0 | 1 | 0 |  |
| :--- | :--- | :--- | :--- | :---: |
| 0 | 1 | 0 | 1 |  |
| 1 | 0 | 0 | 1 |  |
| 0 | 1 | 1 | 0 |  |
| BM4x4_8 |  |  |  |  |

" 1 " is location of BPSK (P), " 0 " is location of Nulls ( $N$ )

## 2-D 4x4 Sequence Correlation





## Mis and False Detection vs Threshold, BM $4 \times 4(8 N, 8 P), S N R=10 d B$



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## 2-D 6X6 Sequences (5 out of 64)

| 0 | 0 | 1 | 1 | 1 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | 0 | 0 | 0 | 1 |
| 0 | 1 | 0 | 1 | 0 | 1 |
| 1 | 0 | 1 | 0 | 0 | 1 |
| 0 | 1 | 1 | 0 | 1 | 0 |
| 1 | 0 | 0 | 1 | 1 | 0 |
| BM6x6_1 |  |  |  |  |  |


| 1 | 1 | 0 | 0 | 0 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 1 | 1 | 1 | 0 |
| 1 | 0 | 1 | 0 | 1 | 0 |
| 0 | 1 | 0 | 1 | 1 | 0 |
| 1 | 0 | 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | 0 | 0 | 1 |
| BM6x6_64 |  |  |  |  |  |


| 0 | 1 | 1 | 1 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 0 | 0 | 0 | 1 | 1 |
| 1 | 0 | 0 | 1 | 0 | 1 |
| 1 | 0 | 1 | 0 | 1 | 0 |
| 0 | 1 | 0 | 1 | 1 | 0 |
| 0 | 1 | 1 | 0 | 0 | 1 |
| BM6x6_25 |  |  |  |  |  |


| 1 | 0 | 0 | 0 | 1 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 1 | 1 | 1 | 0 | 0 |
| 0 | 1 | 1 | 0 | 0 | 1 |
| 0 | 1 | 0 | 1 | 1 | 0 |
| 1 | 0 | 1 | 0 | 1 | 0 |
| 1 | 0 | 0 | 1 | 0 | 1 |
| BM6x6_38 |  |  |  |  |  |


| 1 | 1 | 0 | 0 | 0 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 1 | 1 | 1 | 0 |
| 0 | 1 | 0 | 1 | 1 | 0 |
| 1 | 0 | 1 | 0 | 1 | 0 |
| 0 | 1 | 1 | 0 | 0 | 1 |
| 1 | 0 | 0 | 1 | 0 | 1 |
| BM6x6_57 |  |  |  |  |  |

" 1 " is location of BPSK ( P ), " 0 " is location of Nulls ( N )

## 2-D 6x6 Sequence Correlation




BM6x6_1 to BM6x6_25


## BM 4x3

## Data and Idle prior and after BM



## Mis and False Detection vs Threshold, BM 6x6 (18N,18P), SNR=10dB



## 2-D 8X8 Sequences (5 out of 256)

| 0 | 0 | 1 | 1 | 1 | 0 | 1 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | 0 | 0 | 0 | 0 | 1 | 1 |
| 0 | 1 | 0 | 1 | 1 | 1 | 0 | 0 |
| 1 | 0 | 1 | 0 | 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | 0 | 0 | 1 | 0 | 1 |
| 1 | 0 | 0 | 1 | 0 | 1 | 1 | 0 |
| 1 | 0 | 0 | 1 | 1 | 0 | 0 | 1 |
| 0 | 1 | 1 | 0 | 1 | 0 | 1 | 0 |
| BM8x8_1 |  |  |  |  |  |  |  |


| 1 | 1 | 0 | 0 | 0 | 1 | 0 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 1 | 1 | 1 | 1 | 0 | 0 |
| 1 | 0 | 1 | 0 | 0 | 0 | 1 | 1 |
| 0 | 1 | 0 | 1 | 1 | 0 | 1 | 0 |
| 1 | 0 | 0 | 1 | 1 | 0 | 1 | 0 |
| 0 | 1 | 1 | 0 | 1 | 0 | 0 | 1 |
| 0 | 1 | 1 | 0 | 0 | 1 | 1 | 0 |
| 1 | 0 | 0 | 1 | 0 | 1 | 0 | 1 |
| BM8x8_64 |  |  |  |  |  |  |  |


| 0 | 1 | 0 | 1 | 1 | 0 | 1 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 0 | 1 | 0 | 0 | 0 | 1 | 1 |
| 0 | 0 | 1 | 1 | 1 | 1 | 0 | 0 |
| 1 | 1 | 0 | 0 | 0 | 1 | 0 | 1 |
| 1 | 0 | 0 | 1 | 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | 0 | 1 | 0 | 0 | 1 |
| 0 | 1 | 1 | 0 | 0 | 1 | 1 | 0 |
| 1 | 0 | 0 | 1 | 1 | 0 | 1 | 0 |
| BM8x8_16 |  |  |  |  |  |  |  |


| 0 | 1 | 1 | 0 | 0 | 1 | 0 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 0 | 0 | 1 | 1 | 0 | 0 | 1 |
| 1 | 0 | 0 | 1 | 0 | 1 | 1 | 0 |
| 0 | 1 | 1 | 0 | 1 | 0 | 1 | 0 |
| 0 | 1 | 0 | 1 | 1 | 0 | 1 | 0 |
| 1 | 0 | 1 | 0 | 0 | 0 | 1 | 1 |
| 0 | 0 | 1 | 1 | 1 | 1 | 0 | 0 |
| 1 | 1 | 0 | 0 | 0 | 1 | 0 | 1 |

BM8x9_28

| 1 | 0 | 0 | 1 | 0 | 1 | 0 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 1 | 1 | 0 | 0 | 1 | 1 | 0 |
| 0 | 1 | 1 | 0 | 1 | 0 | 0 | 1 |
| 1 | 0 | 0 | 1 | 1 | 0 | 1 | 0 |
| 0 | 0 | 1 | 1 | 1 | 0 | 1 | 0 |
| 1 | 1 | 0 | 0 | 0 | 0 | 1 | 1 |
| 0 | 1 | 0 | 1 | 1 | 1 | 0 | 0 |
| 1 | 0 | 1 | 0 | 0 | 1 | 0 | 1 |

BM8x8_33

## 2-D 6x6 Sequence Correlation





## 8x8 2-D Auto-Correlation



## Mis and False Detection vs Threshold, BM 8x8 (32N,32P), SNR=10dB



## 2-D 5X6 Sequences (4 out of 10080)

| 1 | 0 | 0 | 1 | 0 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | 0 | 0 | 1 | 0 |
| 0 | 1 | 1 | 0 | 0 | 1 |
| 0 | 1 | 1 | 1 | 0 | 0 |
| 1 | 0 | 0 | 0 | 1 | 1 |
| BM5x6_6004 |  |  |  |  |  |


| 0 | 0 | 1 | 1 | 1 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 1 | 0 | 1 | 1 | 0 |
| 1 | 0 | 1 | 0 | 0 | 1 |
| 1 | 0 | 0 | 0 | 1 | 1 |
| 0 | 1 | 1 | 1 | 0 | 0 |
| BM5x6_1590 |  |  |  |  |  |


| 0 | 0 | 1 | 0 | 1 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | 0 | 0 | 0 | 1 |
| 1 | 0 | 0 | 1 | 1 | 0 |
| 1 | 0 | 1 | 1 | 0 | 0 |
| 0 | 1 | 0 | 0 | 1 | 1 |
| BM5x6_757 |  |  |  |  |  |


| 0 | 1 | 0 | 1 | 0 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | 1 | 0 | 0 | 0 |
| 0 | 0 | 1 | 1 | 1 | 0 |
| 0 | 0 | 1 | 0 | 1 | 1 |
| 1 | 1 | 0 | 1 | 0 | 0 |
| BM5x6_3004 |  |  |  |  |  |

## 2-D 5x6 Sequence Correlation



## Conclusion

- 2-D BM sequences exploit the 2-D OFDMA modulation structure to improve contrast for search of BM
- Equal number of $P$ and $N$ is optimal to minimize misdetection and false detection rate
- Equal number of P and N allow 3 dB boosting to further improve robustness
- 2-D BM sequences are suitable for RB of 1 subcarrier RB

