

Considerations of US Burst Marker Design and Performance

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Summary of Current Burst Marker Proposal

- Power based burst marker detection (T.D. #97)
- Burst Markers baseline proposal
 - [rahman_syed_3bn_01_1113.pdf](#)
- Other burst marker proposal and analysis
 - [montreuil_3bn_02a_0114.pdf](#)
 - [montreuil_3bn_01a_0114.pdf](#)
- This contribution provides more analysis of above proposals and suggest an means of designing the burst marker.

Summary of Requirement for Burst Marker

- Minimum SNR requirement: 10dB
- Target Packet Error Rate (including packet loss rate): $5e-5$
- Miss detection rate: $< 5e-6$
- False Detection Rate: $1/100 \sim 1/1000$ of PER.
- Assume pre-equalized channel
- Other impairments:
 - Narrowband ingress noise

Power Based Detection for 2-D Burst Marker

- Power based detection

$$P = \sum_{i=1}^M P_i \quad N = \sum_{i=1}^K N_i$$

where P_i is the power of each position of '1', and N_i is the power of each position of '0'

- Burst Marker Detected if $P \geq T_{hd}$ and $N < T_{hd}$.

0	1	0	1
1	0	1	0
0	1	1	0
1	0	0	1

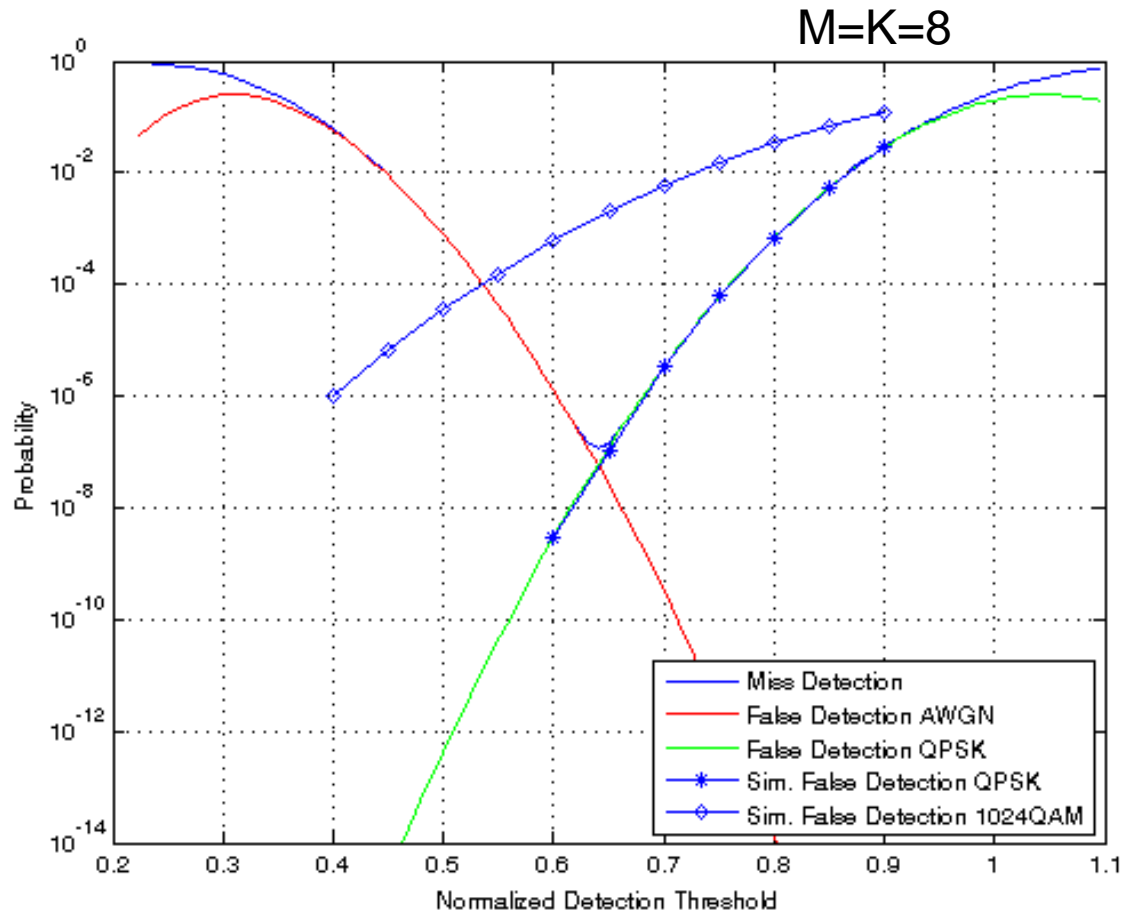
1: BPSK sequence with full power
0: No signal

Detection Error

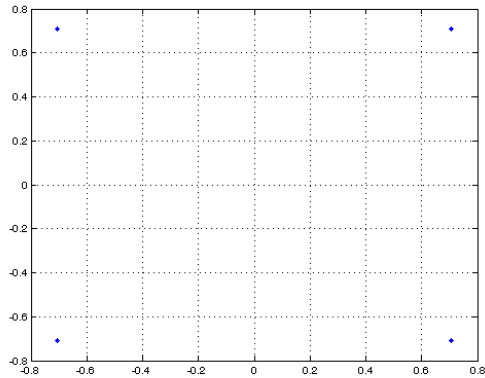
- Miss Detection:
 - Burst Marker present, but undetected
- Two types of false detection:
 - Only white noise present, but detect burst marker
 - US data present, but detect burst marker
- Example: 4x4 burst marker

0	1	0	1
1	0	1	0
0	1	1	0
1	0	0	1

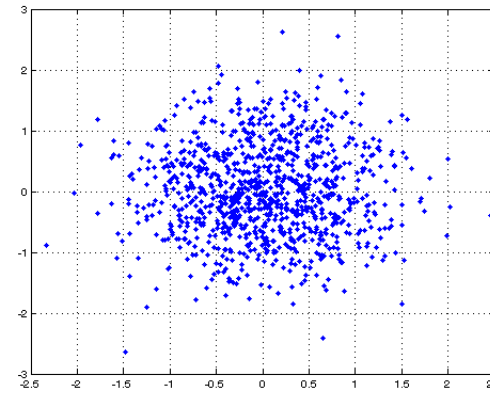
Error Probability



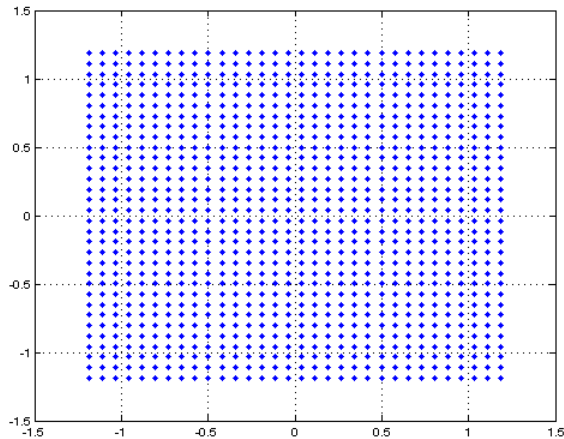
Different Data Symbol Statistics



QPSK



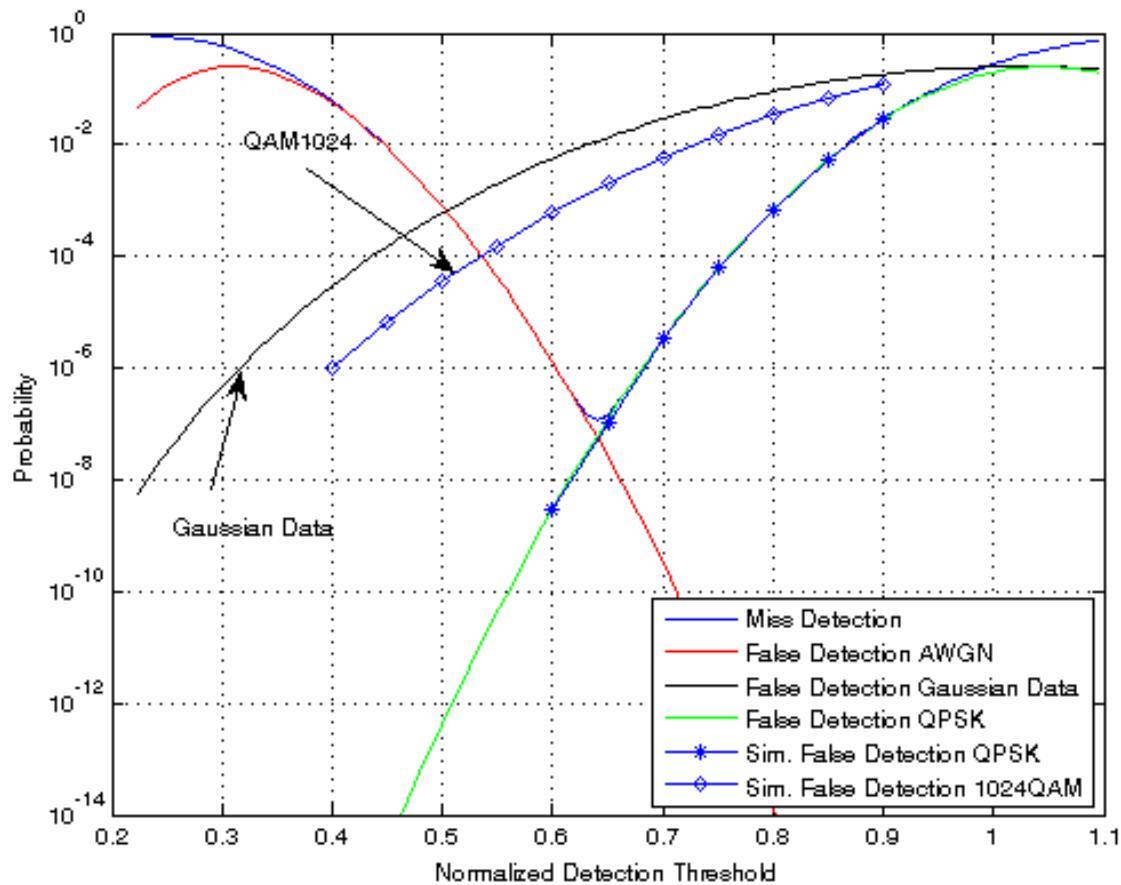
Gaussian



1024QAM

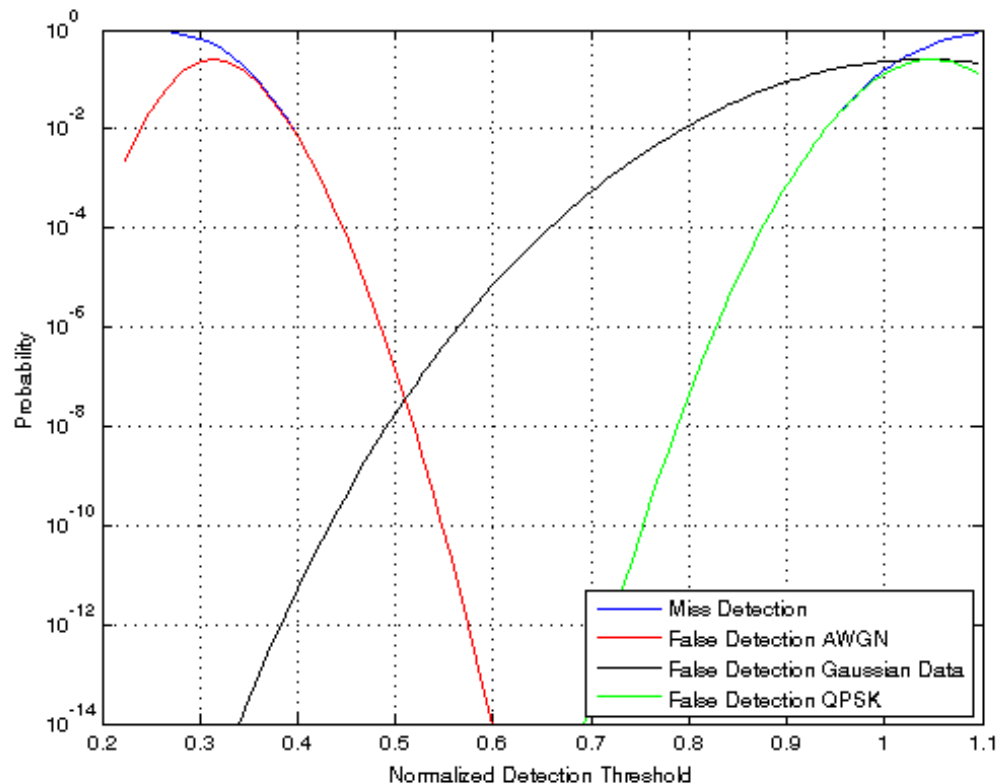
Use Gaussian Constellation
well approximate worst case

Error Probability---Gaussian Approximation



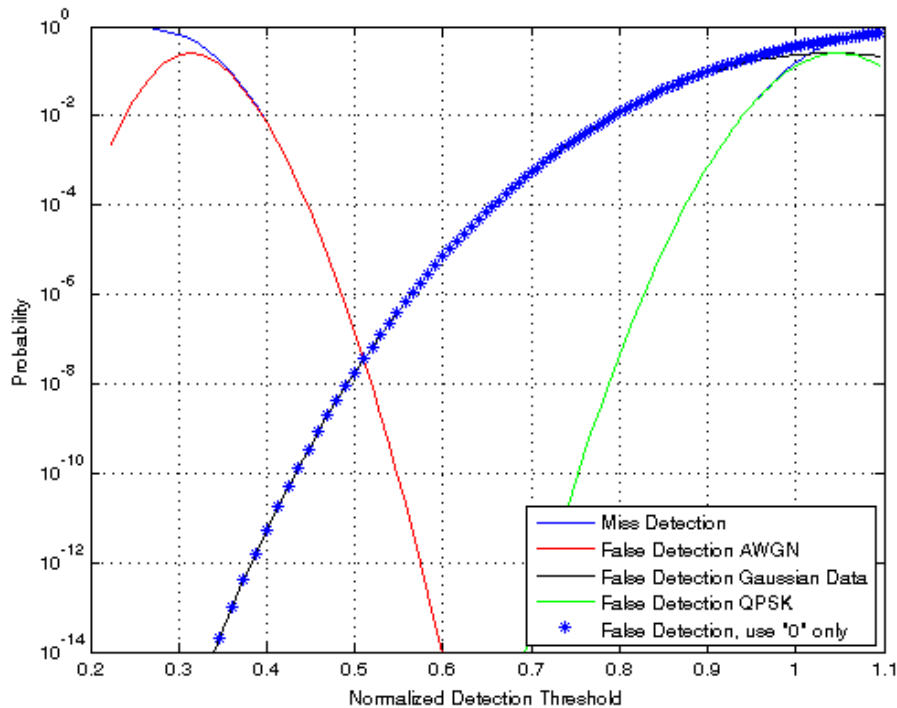
How Large Does the Burst Marker Need To Be for Current Proposal

- False Probability $< 1e-8$, and Miss probability $< 1e-6$
- $M=K=22$,
i.e. 22 “1”s and
22 “0”s



“1”s In the Burst Marker Does Not Help on False Probability of Data

- In case of false probability of data
 $\text{Prob}\{P \geq \text{Thd}\} \sim 1$
- $\text{Prob_false} = \text{Prob}\{N < \text{Thd}\}$



Power Ratio Detector

- Compute the power of “1”s and “0”s as P and N

$$P = \sum_{i=1}^M P_i \quad N = \sum_{i=1}^K N_i$$

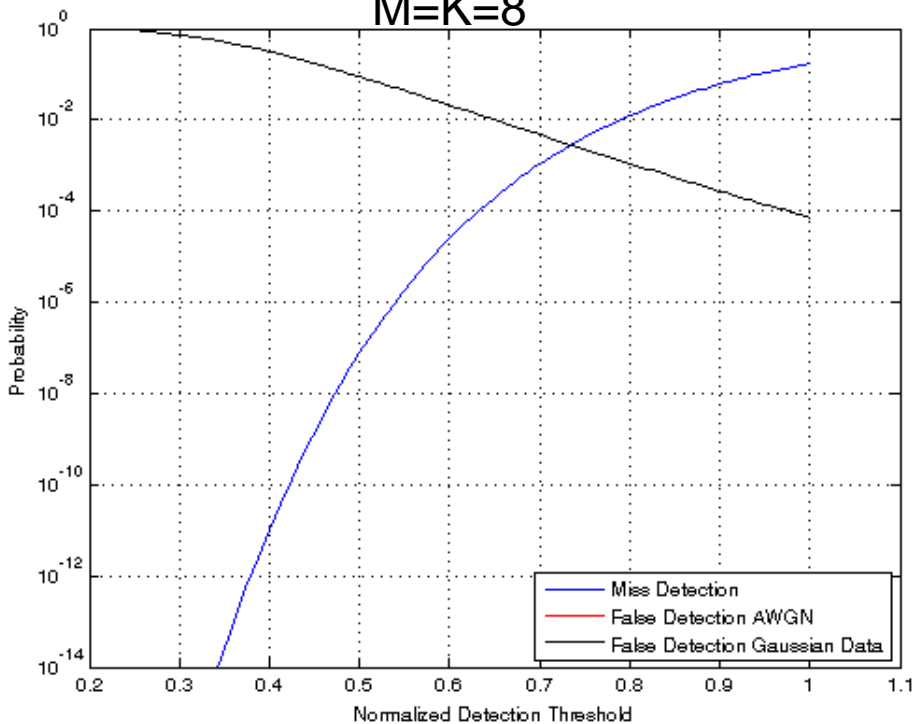
- Radio Detector
 - Burst Detect: $P/N > Th$
- Error Performance
 - Miss Detection: Burst Marker present, but not detect
 - $P \sim$ noncentral chi-square of $2M$ degree of freedom
noncentral parameter = $2M * SNR$
 - $N \sim$ chi-square of $2K$ degree of freedom
 - P/N : non-central F distribution

Power Ratio Detector

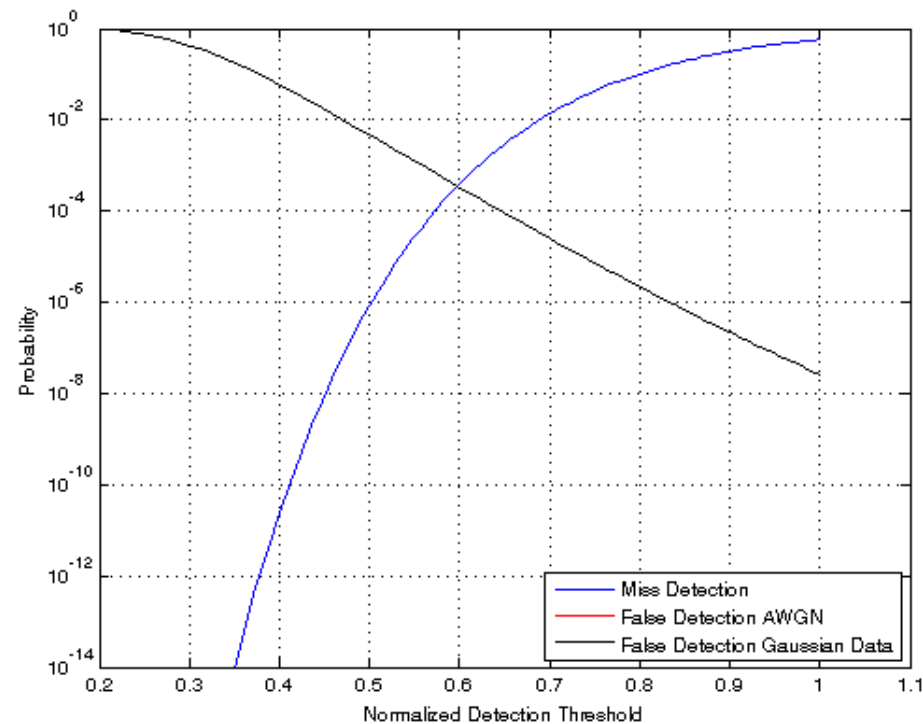
- False Detection due to AWGN
P and N are both chi-square of $2K$ degree of freedom
- False Detection due to Gaussian Data
P and N are both chi-square of $2K$ degree of freedom
- For power ratio detector, the false detection rate due to AWGN is the same as that due to Gaussian data.

Error Performance of Power Ratio Detector

M=K=8



M=K=12



Considerations

- Consider the power threshold detector
- In the proposed burst marker, false probability of data is dominant of false probability.
- '1's in the burst marker do not help on the false probability of data. Only '0's can help.
- '1's in the burst marker only help in the detection over AWGN.
- Decouple the detection of "0"s and "1"s
 - Provide flexibility of burst marker design
 - The number of "0"s and "1"s can be designed separately.
- Propose two-step detection
 - First step: detect "0"s within burst marker
 - Second Step: detect "1"s within the burst marker

First Detector

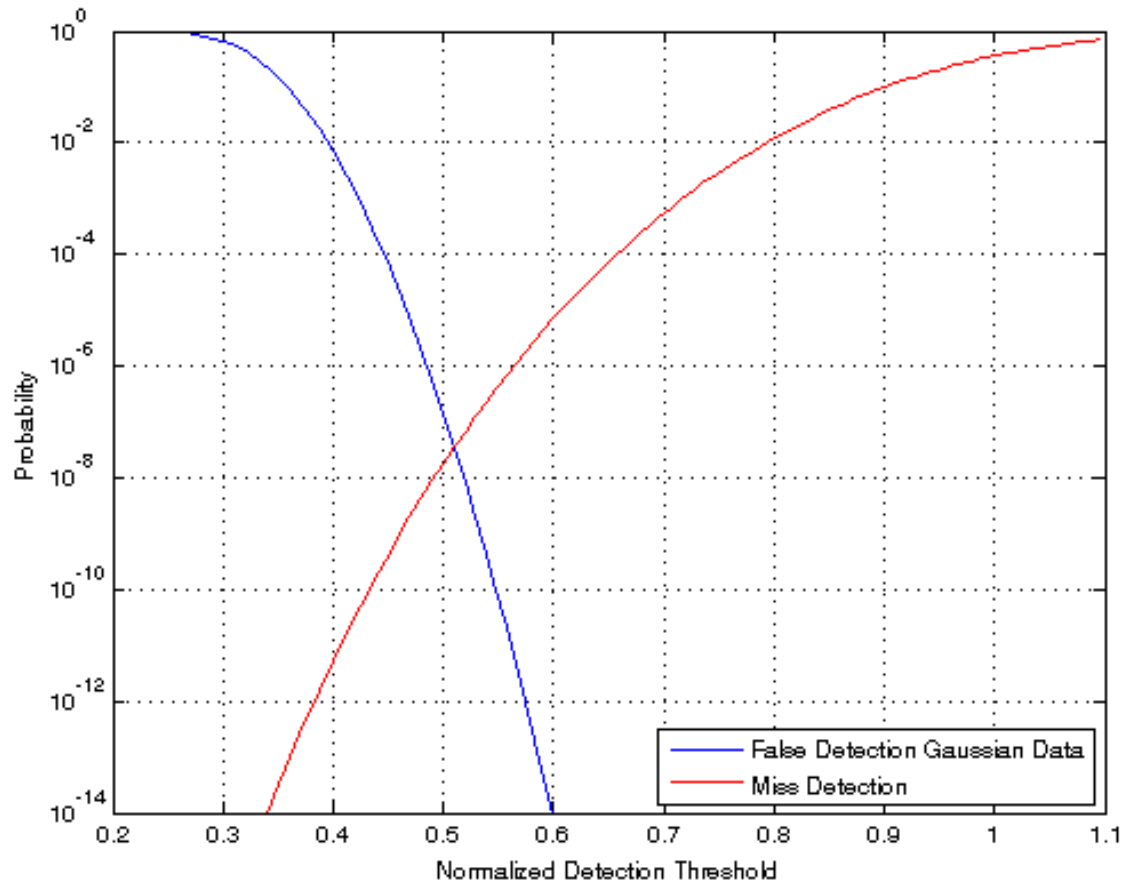
- Assume K zeros are defined in the burst marker, N_i , $i=1, \dots, K$, as power of each “0”

$$N = \sum_{i=1}^K N_i$$

- Detect: $N < \text{Thd}$
- Error Event:
 - False probability due to data: P_{f1}
 - Miss detection probability: P_{m1}

Error Performance of First Detector

K=22



Second Detector

- Assume M “1”s in the burst marker.
- $p_i, i=1, \dots, M$ is taken from $\{-1, 1\}$ as PRBS sequence.
- $r_i, i=1, \dots, M$ as the received value at the output of FFT.
- Coherent correlator

$$P = \sum_{i=1}^M r_i p_i$$

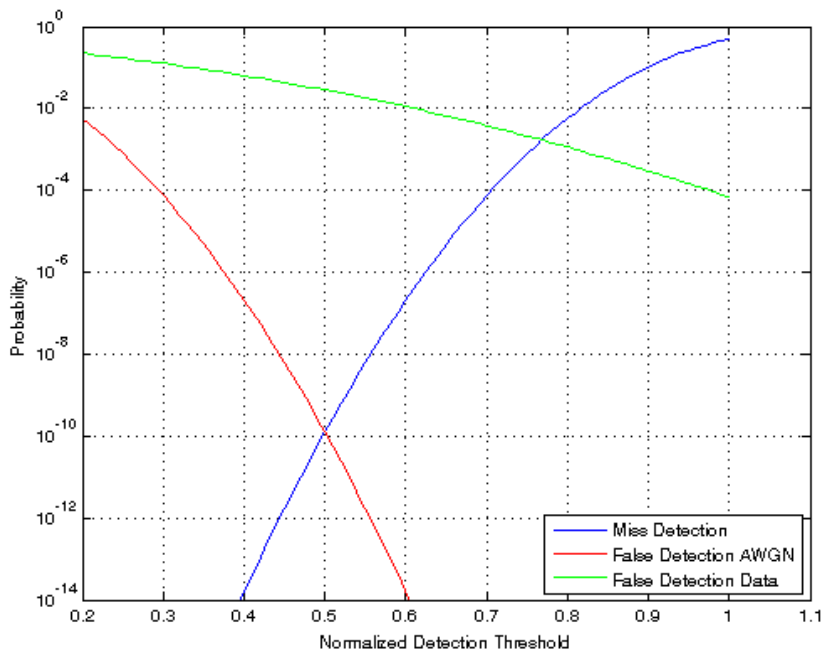
- Non-coherent correlator

$$P = \left| \sum_{i=1}^M r_i p_i \right|$$

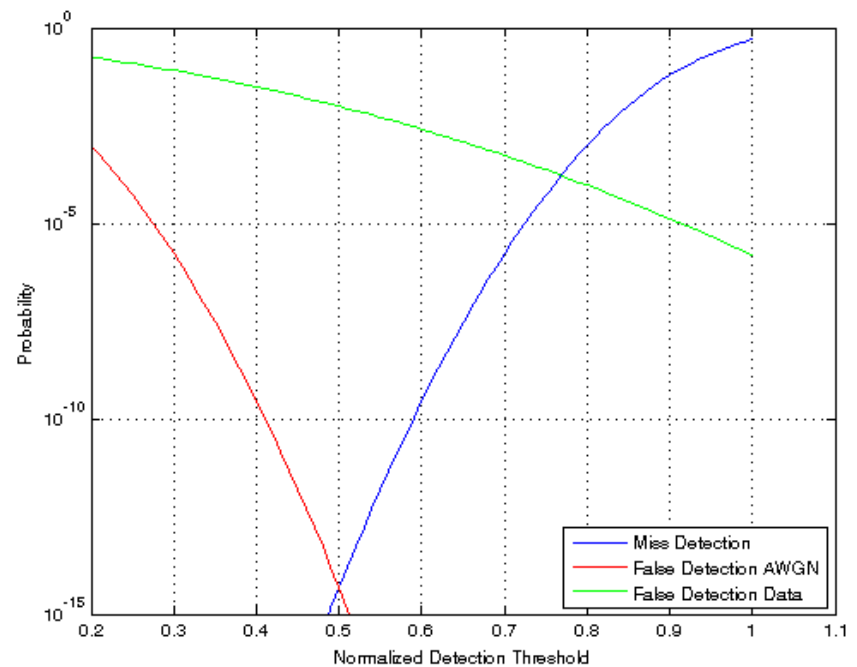
- Detect: $P > \text{Thd}$
- Error Event
 - Miss detection P_{m2}
 - False detection due to noise P_{f2}
 - False detection due to data: P_{f2_data}

Error Performance-Coherent Correlator

M=8

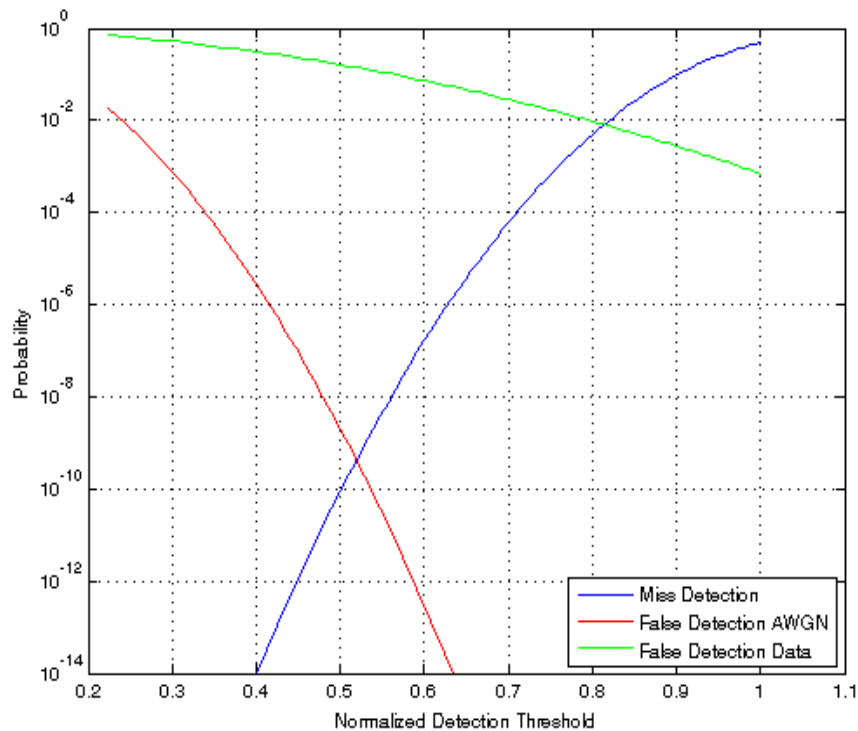


M=12

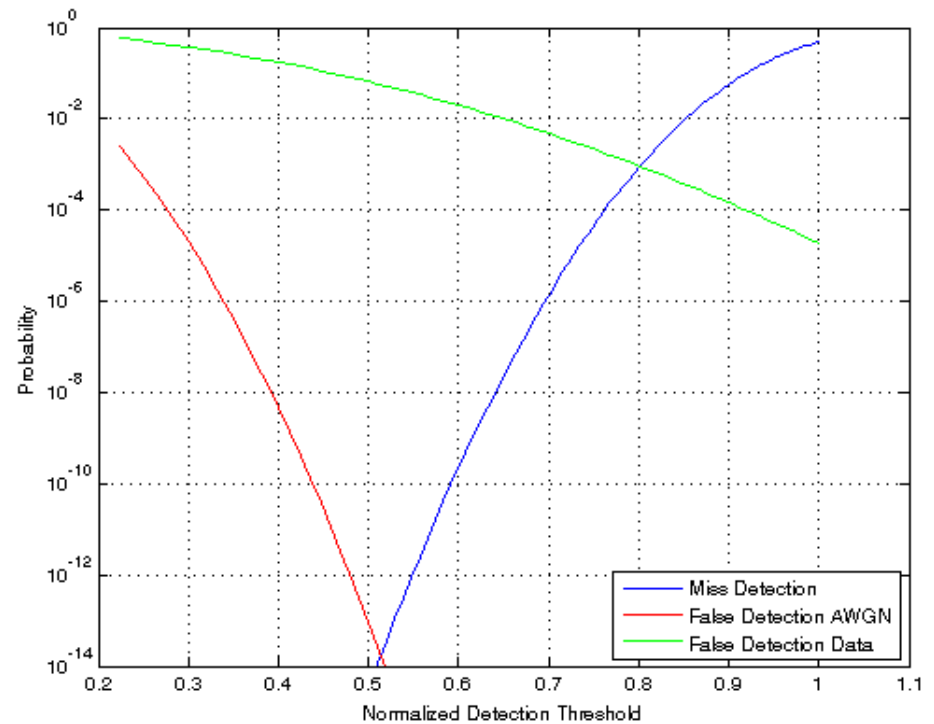


Error Performance - Noncoherent

M=8



M=12



Combined Error Performance for two Detectors

- Miss Detection
 - First detector miss, OR, second detector miss
 $P_m = P_{m1} + (1 - P_{m1}) * P_{m2} \approx P_{m1} + P_{m2} \approx P_{m1}$
($P_{m2} \ll P_{m1}$)
- False Detection due to AWGN
 - First detector detect, AND second detector false detect
 $P_{fawgn} = (1 - P_{m1}) * P_{f2} \approx P_{f2}$
- False Detection due to Data
 - First detector false detect AND Second detector false detect due to data
 $P_{fdata} = P_{f1} * P_{f2_data}$

Selection Rule for Burst Marker Length based on Two Step Detector

1. Select the number of “1”s M , such that miss detection $< 1e-8$, and false detection due to noise is less than $1e-10$

$$M \geq 8$$

2. Obtain $Pf2_data$ given M and miss detection rate $1e-8$.

3. Calculate the required $Pf1$ for first detector

$$Pf1 = 1e-8 / Pf2_data$$

4. Find the number of “0”s K , such that it meets $Pm1 < 1e-6$ given $Pf1$ obtained in step 3

Example

- $M=8$, when $P_{m2}=1e-8$, $P_{f2_data}\sim 0.1$, the required $P_{f1}=1e-8/0.1=1e-7$.
Find K such at $P_{m1}<1e-6$ when $P_{f1}\leq 1e-7$,
 $K=20$.
- $M=12$, when $P_{m2}=1e-8$, $P_{f2_data}\sim 1e-2$, then, the required $P_{f1}=1e-6$
Find K such that $P_{m1}<1e-6$ when $P_{f1}\leq 1e-6$,
 $K=18$.

Summary

- Two-step detection allows to choose M , K independently given false detection and miss detection requirement.
- The burst marker designed by the two-step detector has same error performance as square 2-D markers, but with reduced number of “1”s.
- The assumption of Gaussian constellation is only the worst case. Actual number K may be less if using the real constellation in simulation.

2-D Structure of Burst Marker(M,K)

- Current proposal uses scattered 2-D burst marker
- Resist narrowband interference??
(Need to verify this)
- Sensitive to Inter-carrier Interference
 - AM hum 60Hz or 120Hz
 - Frequency offset (when search for burst marker, there may be uncorrected frequency offset.)
- Need to design 2-D structure to have good auto-correlation for both 0 and 1 positions.

0	1	0	1
1	0	1	0
0	1	1	0
1	0	0	1

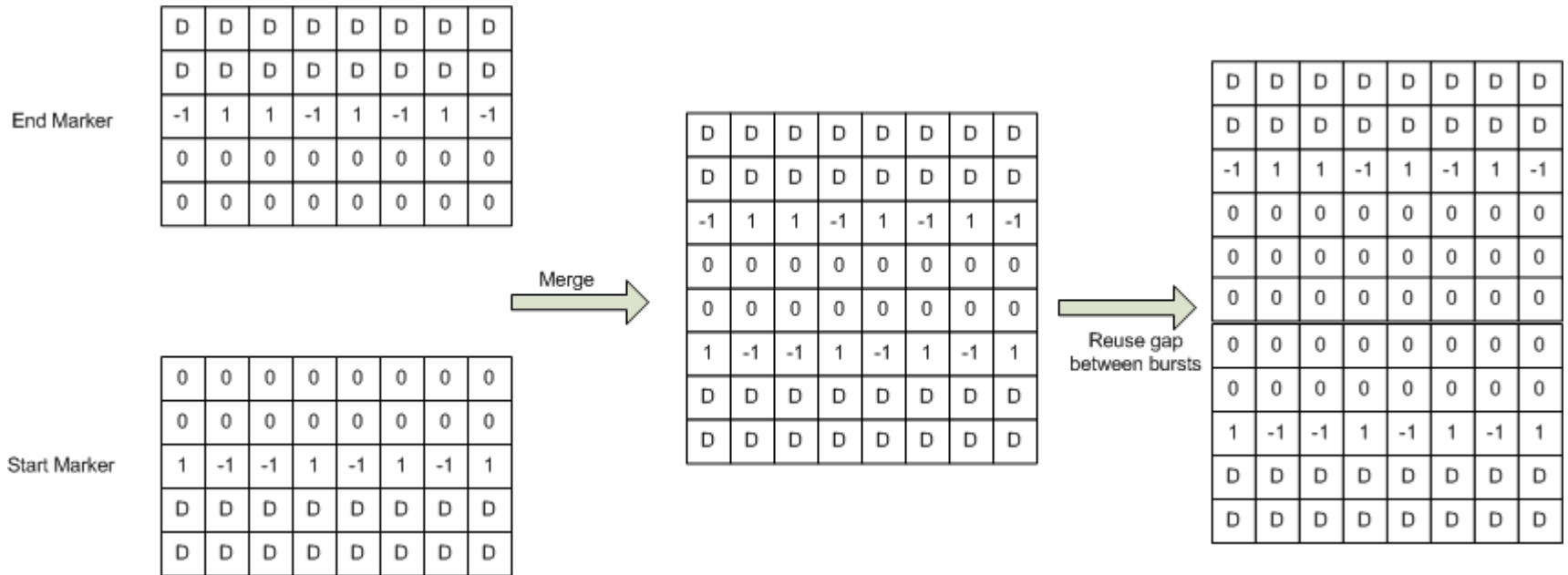
Alternative Structure with Isolated '0's and '1's

- Same Performance
- Less sensitive to ICI, esp. for start marker
- Narrow-band interference?
- Only need good auto-correlation for '1'.
 - Can use orthogonal sequence, such as walsh sequence

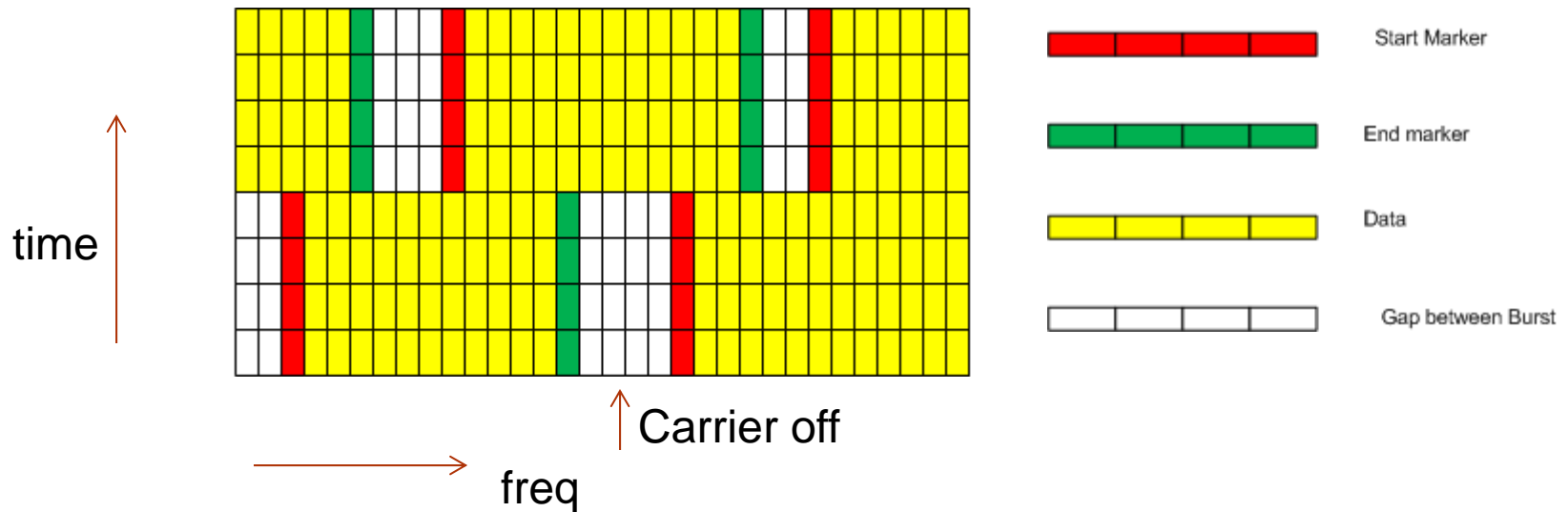
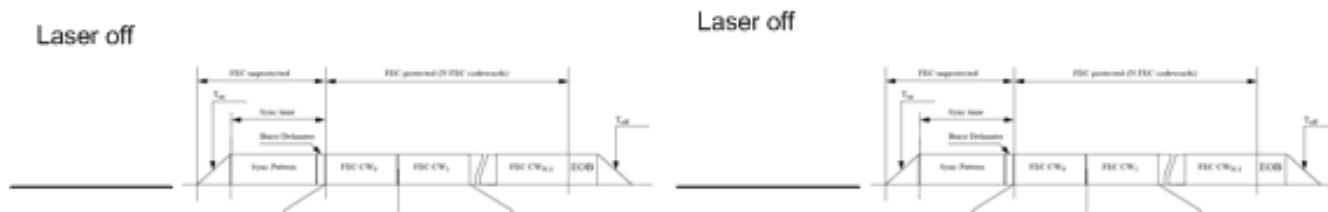
0	0	0	0
0	0	0	0
1	1	1	1
1	1	1	1

Example

- M=8, K=16



Similarity between EPON and EPoC Burst



Summary

- With the isolated '0's and '1's, the start marker and end marker can share same '0's, improve the efficiency.
- Any gap between bursts naturally becomes part of the '0's and increase the reliability of detection.
- The two-step detector turns out to merely be a frequency domain "AGC", i.e. first detect the power-off reset AGC and detection state machine, then detect the BPSK marker, similar to what EPON and other packet based systems do.

Consideration for Narrow Band Interference

- Narrow-band interference generates power leakage because of rectangle windowing at RX
- If a strong NBI strikes start or end marker, it will most likely corrupt the detection any way.
- Narrow band interference is quasi-static.
- A better solution is to avoid the interfering subcarriers in the US bit-loading profile.
- When doing 1D-2D mapping, those subcarriers of poor C/I should be excluded.
- Quantitative requirement for rejection of narrow band interference needs to be established.

Leakage

