

# Problems of high DFE coefficients

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- If we allow high DFE coefficients, we cannot meet MTTFPA (Mean Time to False Packet Acceptance) requirements at  $BER=1E-12$  due to burst errors
  - Hence,  $b_{max}$  (max magnitude of relative DFE coefficient) is proposed to be 0.35
  
- There are some serious problems with  $b_{max} = 0.35$  or 0.5
  - Problem 1: COM is not accurate when  $b_{max} < 1$
  - Problem 2: BER (and COM) may be drastically degraded when  $b_{max}$  is 0.35 or 0.5
  
- COM should not be used with  $b_{max} < 1$ , because
  - COM is not accurate when  $b_{max} < 1$  (Problem 1)
    - This may be fixed in the future
  - $b_{max} = 0.35$  rejects sufficiently good channels (Problem 2)
    - $b_{max} = 0.35$  is not necessary to meet the MTTFPA requirement
  
- We have two other options to satisfy the MTTFPA requirement:
  - Option 1:
    - Revise COM criteria so that we get  $BER < 1E-15$ , if we pass COM test with  $DER_0=1E-12$ , and
    - Test Rx for  $BER < 1E-12$  with restricted DFE coefficients, or for  $BER < 1E-15$  with no restriction
  - Option 2:
    - Use precoding to *eliminate* burst errors due to DFE error propagation

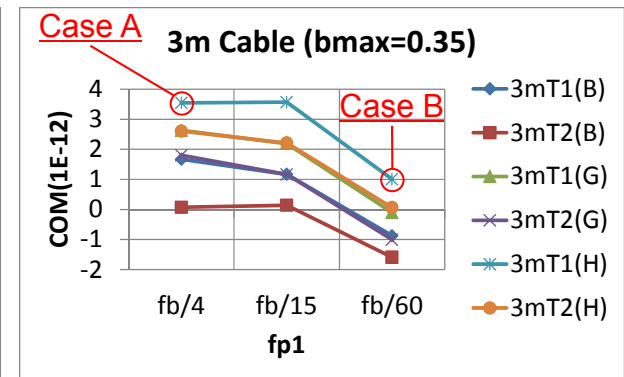
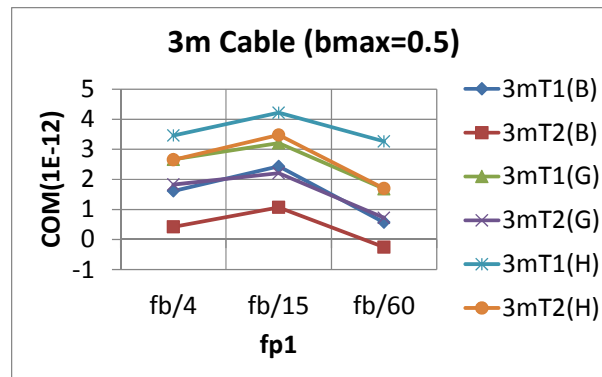
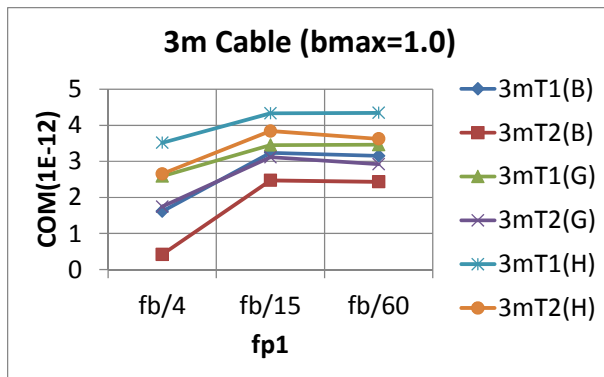
# Study of bmax Effect on COM and BER



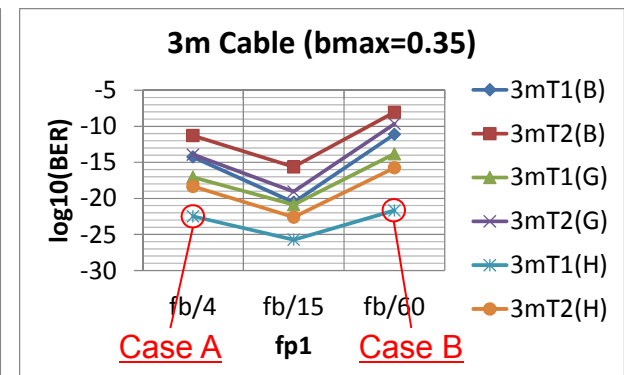
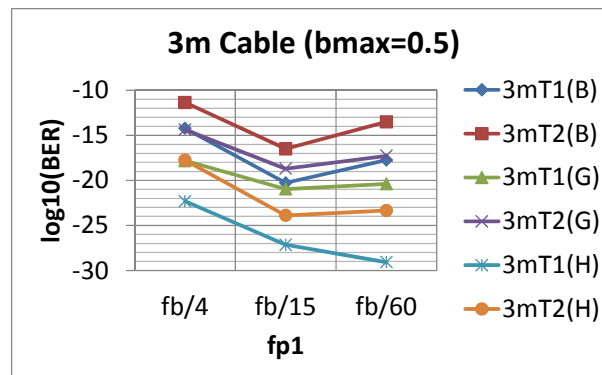
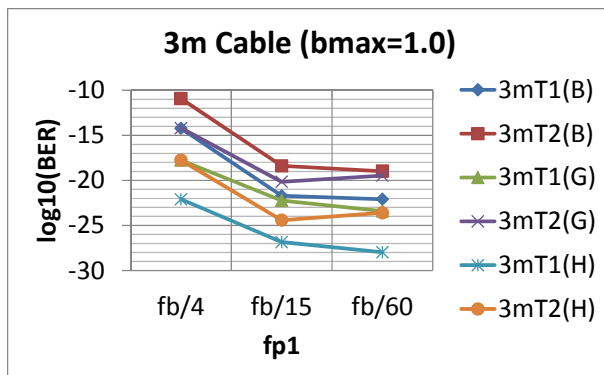
- **bmax(n)**
  - 1.00, 0.50, 0.35 (for all n)
- **CTLE**
  - fp1: fb/4, fb/15, fb/60
  - fz: same as fp1
  - DC gain:
    - min -12dB, max 0dB, step 1dB when fp1 = fb/4 or fb/15
    - min -8dB, max 0dB, step 0.5dB when fp1 = fb/60
- **Channel data**
  - 3m cable: B(30Q4) – fair, G(26QQ) – typical, H(26Q4) – good
  - 5m cable: Q(24QQ) – fair, N(26QQ) – typical, R(24QQ) – good
- **Test conditions**
  - Test 1 (PKG trace = 12mm) and Test 2 (PKG trace = 30mm)
  - DER0 = 1E-12
- **Equalizer parameters: optimized by reference COM code**  
(i.e. [http://www.ieee802.org/3/bj/public/tools/ran\\_com\\_3bj\\_3bm\\_01\\_1114.zip](http://www.ieee802.org/3/bj/public/tools/ran_com_3bj_3bm_01_1114.zip))
- **BER and Eye: analyzed by in-house tool**
  - Parameters of statistical analysis:
    - TX RJ = 0.01UI (rms), TX DJ = 0.15UI ( $\delta$ - $\delta$ ), TX EOJ = 0.035UI (p-p)
    - RX RJ = 0.005UI (rms), RX DJ = 0.075UI ( $\delta$ - $\delta$ ), RX EOJ = 0.0175UI (p-p)
    - TX output noise  $SNR_{TX} = 27$  (dB)
    - RX input noise  $\eta_0 = 5.20E-8$  ( $V^2/GHz$ )
    - Receiver 3dB bandwidth = 0.75 (fb)

# Effect of fp1 on COM and BER for 3m Cable

## ■ fp1 vs COM (DER0=1E-12)



## ■ fp1 vs BER

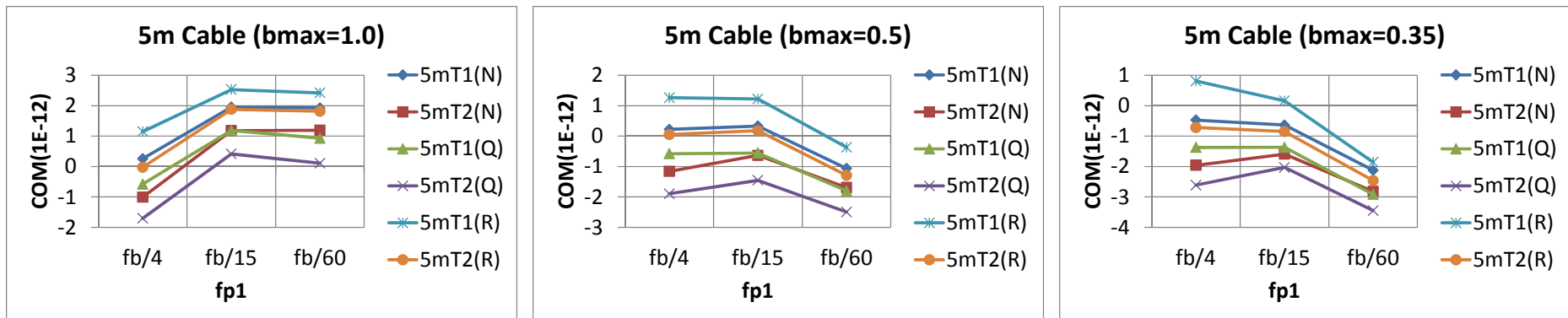


■ COM and BER are roughly consistent when bmax=1.0

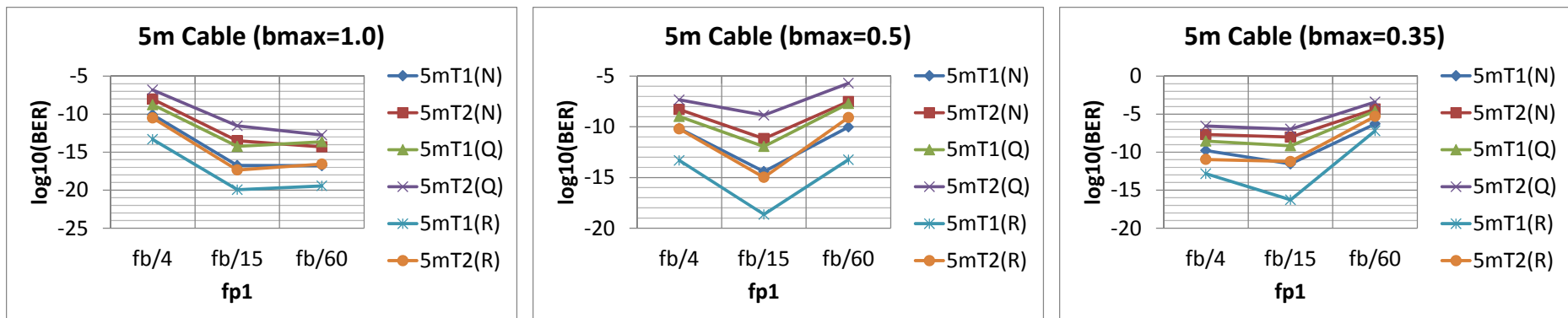
■ COM and BER are very inconsistent when bmax=0.5 or 0.35

# Effect of fp1 on COM and BER for 5m Cable

## ■ fp1 vs COM (DER0=1E-12)



## ■ fp1 vs BER

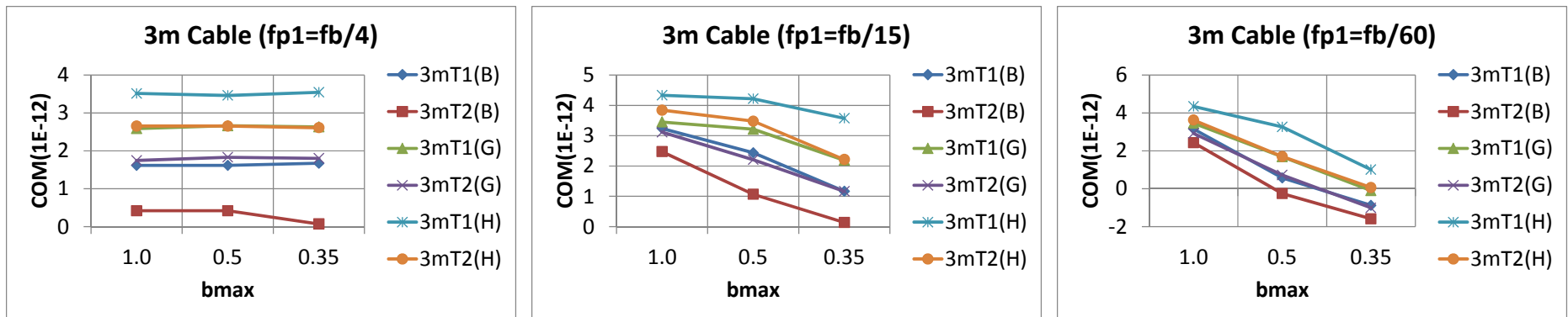


■ COM and BER are roughly consistent when bmax=1.0

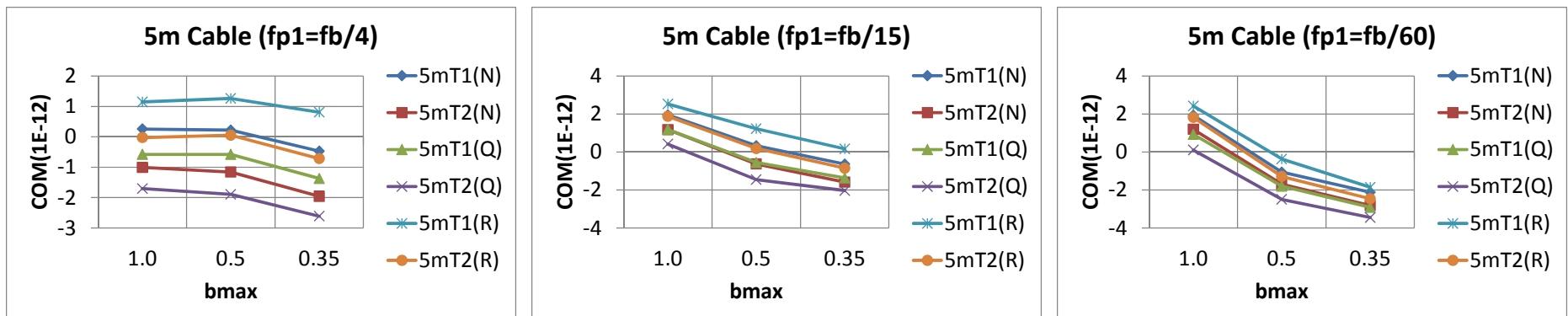
■ COM and BER are very inconsistent when bmax=0.5 or 0.35

# Effect of bmax on COM

## ■ bmax vs COM (3m Cable)



## ■ bmax vs COM (5m Cable)

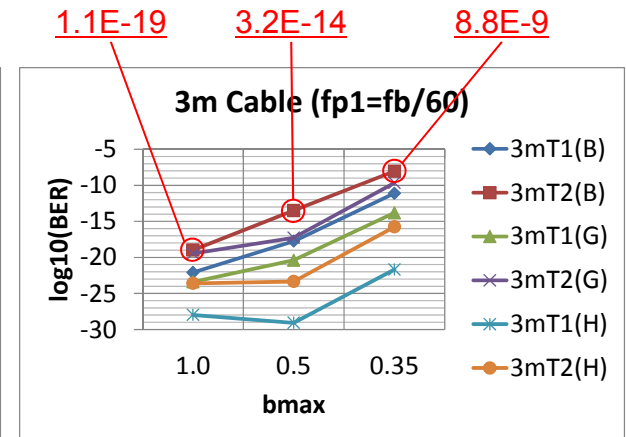
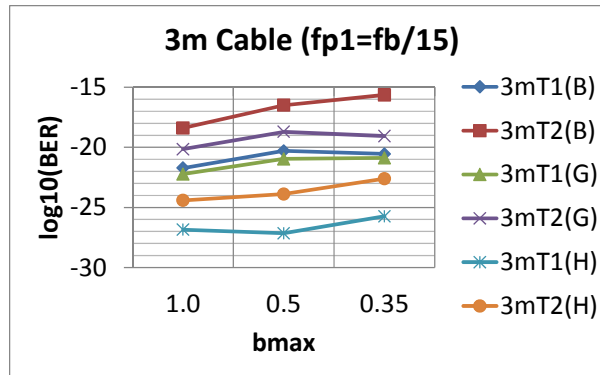
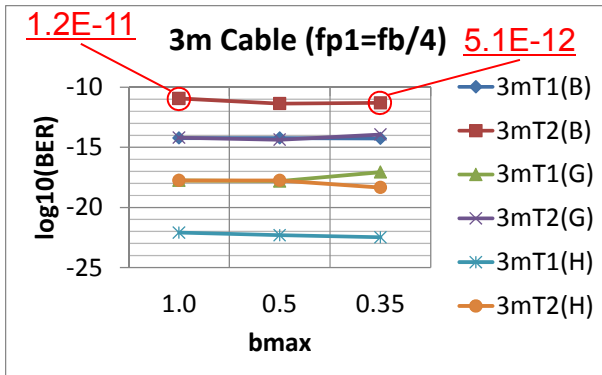


■ COM is not much affected by bmax when  $fp1 = fb/4$

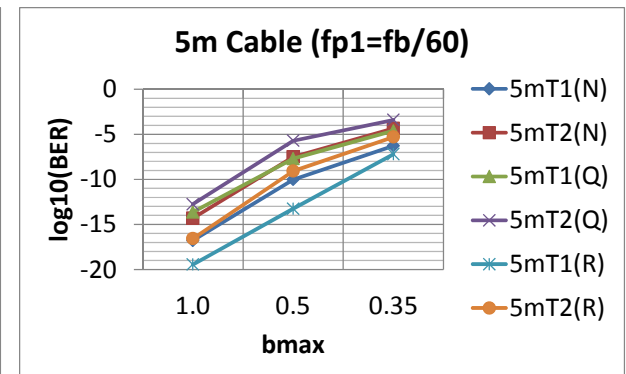
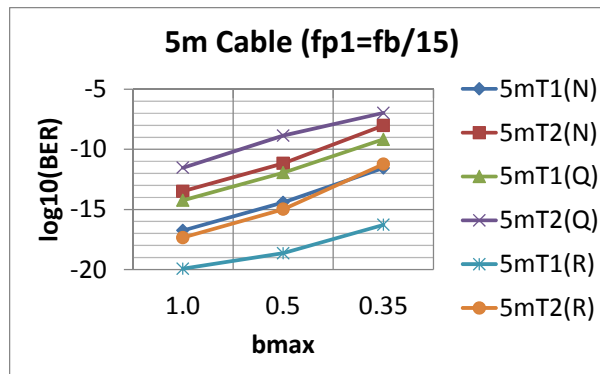
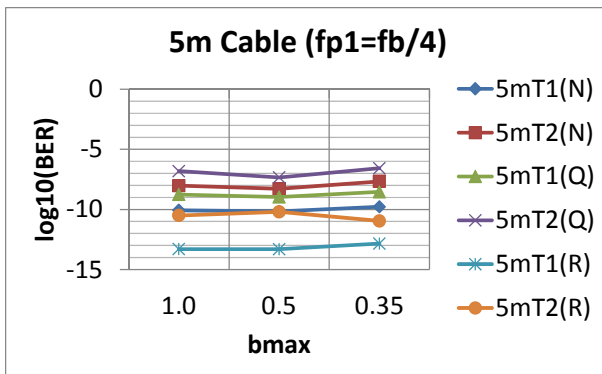
■ COM is largely degraded by bmax when  $fp1 = fb/15$  or  $fb/60$

# Effect of bmax on BER

## ■ bmax vs BER (3m Cable)



## ■ bmax vs BER (5m Cable)



■ BER is not affected by bmax when  $fp1 = fb/4$

■ BER is largely degraded by bmax when  $fp1 = fb/15$  or  $fb/60$

■ 3m T2(B) is good with  $fp1=fb/60$  and  $bmax=1$ , but fails with  $bmax=0.35$

# Detail Analysis of Case A and Case B

■ Channel: 3m cable H(26Q4), Test 1,  $b_{max}=0.35$

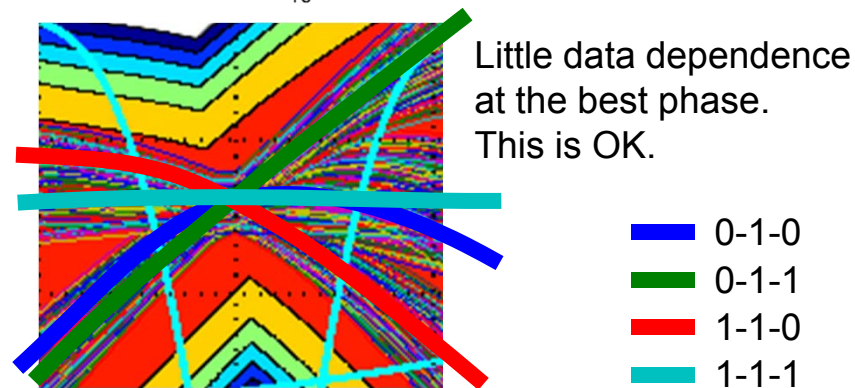
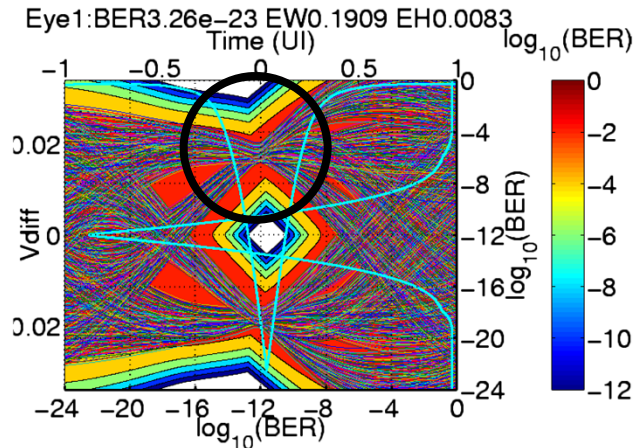
■ Case A ( $fp1=fb/4$ )

■ DCgain = -12 dB,  $b(1) = 0.337389$  (not restricted)

■ COM (DER0=1E-12)

- 3.5463 dB (reference implementation)
- 3.71644 dB (our implementation)

■ BER = 3.26E-23



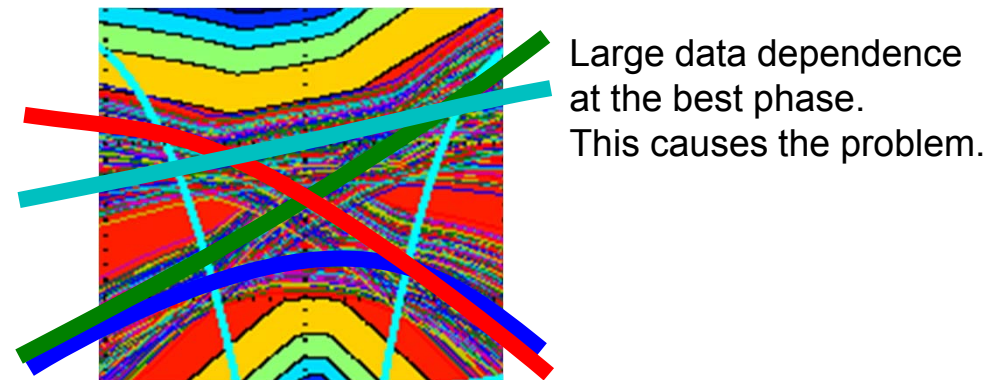
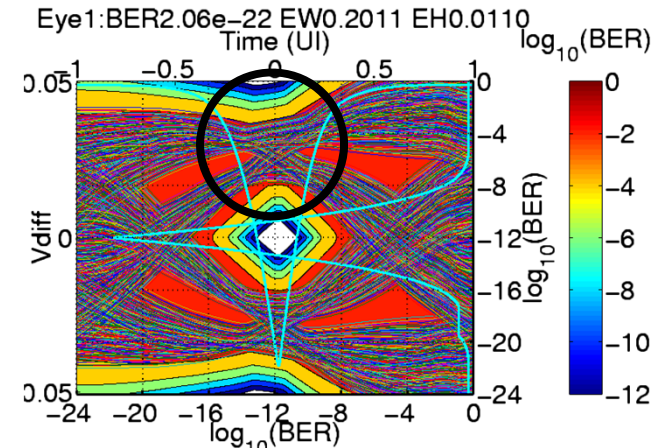
■ Case B ( $fp1=fb/60$ )

■ DCgain = -6.5 dB,  $b(1) = 0.35$  (restricted by  $b_{max}$ )

■ COM (DER0=1E-12)

- 1.0056 dB (reference implementation)
- 1.37456 dB (our implementation)

■ BER = 2.06E-22





# Two Options to meet the MTTFPA requirements



## ■ Option 1

- Revise COM criteria (currently 3dB) so that there is enough margin
  - To achieve  $BER < 1E-15$ , when we pass the COM test with  $DER_0 = 1E-12$ 
    - Statistically guarantee the channel quality so that we can achieve  $BER < 1E-15$
    - I am currently working on this statistical calculation
- Test Rx for  $BER < 1E-15$  with no restrictions on DFE coefficients
  - For a combination of compliant channel and Rx, since BER will be less than  $1E-15$ , we will meet the MTTFPA requirement
  - We may use other means such as plotting a bathtub curve to shorten test time
- I have considered an alternative Rx test for  $BER < 1E-12$  with DFE coefficients  $< 0.35$ , but such an alternative test is not acceptable
  - For some good channels, BER can be  $< 1E-15$  with high DFE coefficients, whereas BER is degraded  $> 1E-12$ , if high DFE coefficients are not allowed
    - Such good channels have high loss in high frequency due to material loss, but the channel design is good enough, because we can achieve sufficiently low BER. I think such good design channels should be accepted as compliant.

## ■ Option 2

- Use precoding to *eliminate* burst errors due to DFE error propagation
  - This is a simple solid solution (next page)

- Tx side: encode the transmitting data by  $b(k) = b(k-1) \oplus a(k)$
- Rx side: decode the received data by  $a'(k) = b(k) \oplus b(k-1)$ 
  - $\oplus$ : an exclusive-OR operator
  - $a(k)$ : original data sequence
  - $b(k)$ : transferred data sequence (NRZ)
  - $a'(k)$ : recovered data sequence
- Any burst error on  $b(k)$  from  $k_1$  to  $k_2$  ( $k_1 \leq k_2$ ) is converted to two errors on  $a'(k)$ , one at  $a'(k_1)$ , and another at  $a'(k_2+1)$ 
  - Hence, **it eliminates any burst errors**
- This is essentially in the same principle as precoding in Duobinary signaling, or precoding in KP4 (although it is a variant for PAM4).
  - We cannot omit DFE to achieve low BER. That is a difference from Duobinary signaling.
- Minor drawbacks
  - If there is no error propagation, BER for random error is doubled
    - I think this is OK, because the packet is anyway dropped, or protected by FEC
  - If there is no DFE, unnecessary extra circuit is required
    - I think this is OK, because DFE is commonly used
  - The encoder has a critical path of an exclusive OR within 1UI
    - I think this is achievable
- I don't know why this hasn't been discussed (maybe everyone is too busy), but I believe this is a solid solution and better than restricting high DFE coefficients
- Is it too late to discuss this scheme? Or, am I missing something?

# Appendix

# Difference between COM and our BER analysis



## ■ COM

- Directly calculate a single probability distribution (i.e. PDF or CDF)
- Jitter is added at all ISI locations

## ■ Our BER analysis

- Calculate multiple (4 for NRZ, 32 for PAM4) probability distributions for all the combinations of prior, next, and cursor symbol levels
  - # of cursor symbol levels is half, because of vertical symmetry
  - Jitter is added differently for each distribution, taking account of each transition
    - Jitter at 010 is smaller than at 011 or 110, because derivative is cancelled and small
    - No jitter is added for distribution at 111 sequence, because there is no transition
- Final CDF is the worst case that is the max value of multiple CDFs:

$$P_{worst}(y) = \frac{1}{2} \max_k [P_k(y)] = \frac{1}{2} \max_k \left[ \int_{-\infty}^y p_k(y) dy \right]$$

- Here,  $P_{worst}(y)$  and  $P_k(y)$  are CDFs and  $p_k(y)$  are PDFs.
- Coefficient 1/2 is for the fact that this is only for lower side of the entire final CDF:

$$P_{final}(y) = \max[P_{worst}(y), P_{best}(y)] = \max \left[ P_{worst}(y), \min_k [P_k(y)] \right]$$

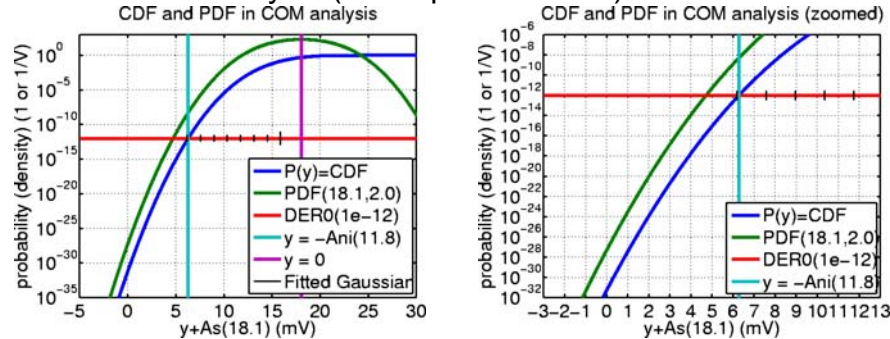
- No jitter is added at ISI locations other than between prior symbol and cursor symbol or between cursor symbol and next symbol
  - Due to this difference, estimated BER is a little lower than DER0 when COM is 0dB

# Very Detail Analysis of Case A and Case B

Notation: PDF( $\mu, \sigma$ ),  $\mu$ =mean,  $\sigma$ =RMS

## ■ Case A (fp1=fb/4)

### ■ COM analysis (our implementation)

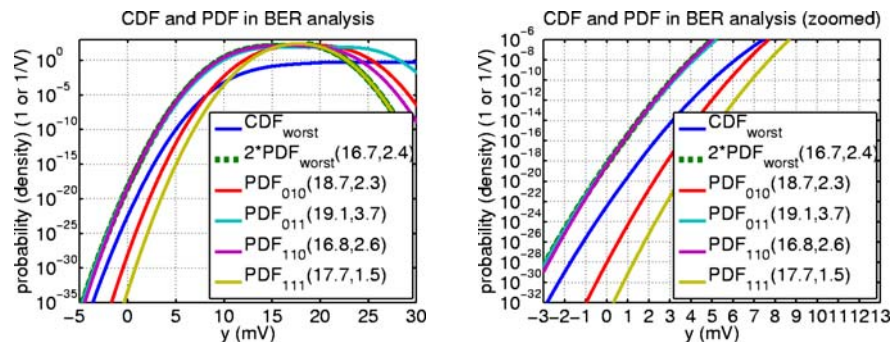


PDF:  $As=\mu=18.1\text{mV}$ ,  $\sigma=2.0\text{mV}$ ,  $Ani=11.8\text{mV}\sim 5.9\sigma$

COM= $20*\log_{10}(18.1\text{mV}/11.8\text{mV})=3.72\text{dB}$

BER= $P(-As)=5.3E-32$

### ■ BER analysis (vertical PDF/CDF at the best phase)



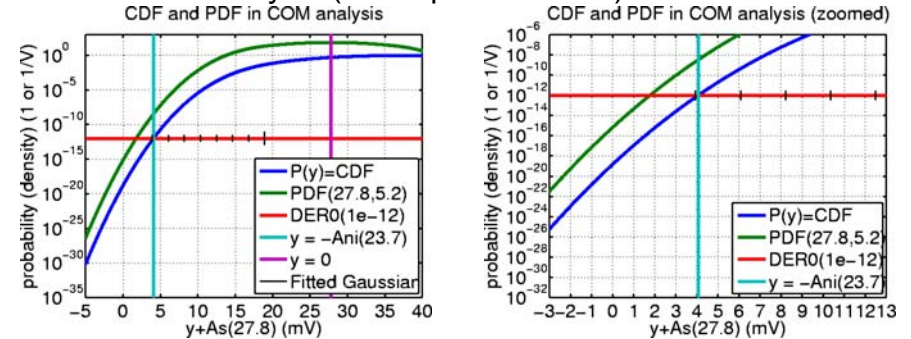
$2*PDF_{\text{worst}}$  ( $\mu=16.7, \sigma=2.4$ ) follows PDF<sub>110</sub> ( $\mu=16.8, \sigma=2.6$ )

$\sigma$  of PDF<sub>010</sub> & PDF<sub>111</sub> is smaller than PDF<sub>011</sub> & PDF<sub>110</sub>

$\mu$  is similar between PDFs with respect to  $\sigma$  value

## ■ Case B (fp1=fb/60)

### ■ COM analysis (our implementation)



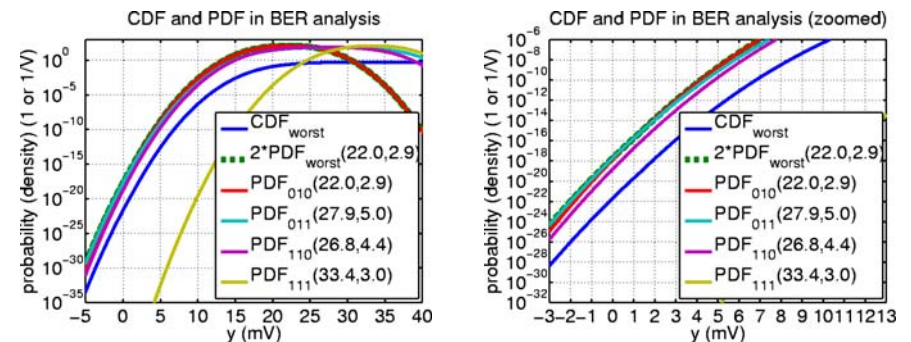
PDF:  $As=\mu=27.8\text{mV}$ ,  $\sigma=5.2\text{mV}$ ,  $Ani=23.7\text{mV}\sim 4.6\sigma$

COM= $20*\log_{10}(27.8\text{mV}/23.7\text{mV})=1.38\text{dB}$

BER= $P(-As)=1.51E-19$

$\sigma$  and BER are much larger (COM is smaller) than Case A

### ■ BER analysis (vertical PDF/CDF at the best phase)



$2*PDF_{\text{worst}}$  ( $\mu=22.0, \sigma=2.9$ ) follows PDF<sub>010</sub> ( $\mu=22.0, \sigma=2.9$ )

$\sigma$  of PDF<sub>010</sub> & PDF<sub>111</sub> is smaller than PDF<sub>011</sub> & PDF<sub>110</sub>

$\mu$  of PDF<sub>010</sub> and PDF<sub>111</sub> are quite different w.r.t.  $\sigma$  value

$\sigma$  of  $2*PDF_{\text{worst}}$  and BER are similar to Case A

# Suggestions for COM

- In our BER analysis, use of multiple distributions was the key to obtain satisfactory results for test cases where a single large ISI (i.e. the largest ISI) is *close to the RSS value of all ISIs*
  - Our BER analysis is not necessarily the best, but probably better than COM
  
- COM is very likely inaccurate when a DFE coefficient is restricted by  $b_{\max} < 1$ , because restriction of a DFE coefficient causes the single large residual ISI close to the RSS value
  
- We may fix the COM formula in a similar way to our BER analysis, but I have not come to a complete suggestion yet
  - I may provide it later, but it takes some time
  
- In the mean time, it is OK to use the current COM with  $b_{\max} = 1$  and high tap-count DFE, because no single large ISI is left after DFE cancels major ISIs
  - In fact, I do not see a large discrepancy between COM and BER as long as I use  $b_{\max} = 1$

# References

[1] [http://grouper.ieee.org/groups/802/3/by/public/May15/sun\\_3by\\_01\\_0515.pdf](http://grouper.ieee.org/groups/802/3/by/public/May15/sun_3by_01_0515.pdf)

[2] [http://www.ieee802.org/3/by/public/adhoc/architecture/sun\\_061015\\_25GE\\_adhoc.pdf](http://www.ieee802.org/3/by/public/adhoc/architecture/sun_061015_25GE_adhoc.pdf)

# References of Channel Data



- ~ = <http://www.ieee802.3.org/3/>
- 3 meter cable assembly
  - A: ~/100GCU/public/ChannelData/CD\_11\_0415/3m\_QSFP\_30AWG.zip (Tx2-Rx2.s4p)
  - B: ~/by/public/channel/TE\_QSFP\_4SFP\_3m\_30AWG.zip (TE\_3m30AWG\_QSFP\_4SFP\_P1\_TX1\_P2\_RX1\_THRU.s4p)
  - C: ~/100GCU/public/ChannelData/Molex\_11\_0516/bugg\_02\_0511.zip (3m 30AWG Unicore/Cable 1/P1 RX1/TX1.s4p)
  - D: ~/by/public/channel/TE\_QSFP\_4SFP\_3m\_28AWG.zip (TE\_3m28AWG\_QSFP\_4SFP\_P1\_TX1\_P2\_RX1\_THRU.s4p)
  - E: ~/by/public/channel/TE\_QSFP\_QSFP\_3m\_26AWG\_MaxLossExample\_15p993dB.zip
  - F: ~/by/public/channel/Amphenol\_NDACGJ-0003-QSFP-4SFP\_3m\_26AWG\_APN43140033HXJ.zip (P2TX1\_P1RX1.s4p)
  - G: ~/100GCU/public/ChannelData/Molex\_11\_0516/bugg\_02\_0511.zip (3m 26AWG leoni/P1 RX1/TX1.s4p)
  - H: ~/by/public/channel/TE\_QSFP\_4SFP\_3m\_26AWG.zip (TE\_3m26AWG\_QSFP\_4SFP\_P1\_TX1\_P2\_RX1\_THRU.s4p)
  - J: ~/by/public/channel/TE\_QSFP\_QSFP\_3m\_25AWG\_MaxLossExample\_15p35dB.zip
  - K: ~/by/public/channel/TE\_QSFP\_QSFP\_3m\_24AWG\_MaxLossExample\_14p49dB.zip
  - L: ~/by/public/channel/TE\_QSFP\_4SFP\_3m\_24AWG.zip (TE\_3m24AWG\_QSFP\_4SFP\_P1\_TX1\_P2\_RX1\_THRU.s4p)
- 5 meter cable assembly
  - M: ~/100GCU/public/ChannelData/CD\_11\_0415/5m\_QSFP\_26AWG.zip (Tx1-Rx1.s4p)
  - N: ~/100GCU/public/ChannelData/Molex\_11\_0516/bugg\_02\_0511.zip (5m 26AWG Leoni/P1 RX1/TX1.s4p)
  - P: ~/by/public/channel/Amphenol\_NDACGJ-0005-QSFP\_4SFP\_5m\_26AWG\_APN14440053HYT.zip(P2TX1\_P1RX1.s4p)
  - Q: ~/100GCU/public/ChannelData/Molex\_11\_0210/5m/5m\_all.zip (P1 RX0/TX0.s4p)
  - R: ~/100GCU/public/ChannelData/molex\_12\_0310/cableb\_bugg\_03\_0312.zip (P1RX1/P2TX1.s4p)



Thank you