
Proposed Worst Case Link Model for Optical Physical Media Dependent Specification Development.

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Outline

- Objectives
- Multimode Fiber Bandwidth Model
- Link and Channel Rise Times
- Extinction Ratio & RIN
- Mode Partition Noise (MPN)
- Inter-symbol Interference (ISI)
- Experimental Results
- Conclusions

Goals

- Develop an accurate analytical model for laser based multimode fiber links.
 - *Use original Del Hanson model for LED based links as the starting point,*
 - *Insert additional terms specific to laser based links,*
 - *Investigate accuracy of model by comparison with experiment.*
- Develop worst case spread sheet model as basis for the development of the physical media dependent specifications.

MMF Chromatic Bandwidth Model

Chromatic Dispersion Coefficients:

$$D1 = \frac{S0}{4} \cdot \left(\lambda_c - \frac{\lambda_0^4}{\lambda_c^3} \right) \quad \text{and} \quad D2 = 0.3 \cdot S0 \cdot \sigma\lambda$$

where,

$S0$ = Dispersion Slope Parameter at λ_0 in (ps/nm²km),

λ_0 = Zero Dispersion Wavelength in nm,

λ_c = Source Center Wavelength in nm,

$\sigma\lambda$ = Source rms Wavelength in nm.

Chromatic Bandwidth, BW_{ch} , in MHz:

$$BW_{ch} = \frac{0.187}{L \cdot \sigma\lambda} \cdot \frac{1}{\sqrt{D1^2 + D2^2}}$$

where L is the link length in km.

Link and Channel Response Time

Let the 10-90% fiber exit rise and fall time be $T_e(\text{ns})$. It is given by:

$$T_e^2 = (C1/BW_m)^2 + (C1/BW_{ch})^2 + T_s^2$$

where,

BW_m = Modal Bandwidth (MHz);

BW_{ch} = Chromatic Bandwidth (MHz);

T_s = Source 10-90% response time;

L = Link length in km;

$C1$ = conversion factor; 480 for gaussian impulse response.

The channel exit rise and fall time, $T_c(\text{ns})$, is reduced by receiver bandwidth, $BW_r(\text{MHz})$. For single pole receiver T_c is:

$$T_c^2 = T_e^2 + (350/BW_r)^2$$

Extinction Ratio & RIN

The extinction ratio penalty in dB is: $P_{\epsilon} = 10 \cdot \log \left[\frac{1 + 10^{-\frac{\epsilon}{10}}}{1 - 10^{-\frac{\epsilon}{10}}} \right]$

where ϵ is the extinction ratio of the laser source in dB.

The penalty in dB due to laser relative intensity noise, RIN (dB/Hz) is:

$$P_{\text{rin}} = 5 \cdot \log \left[\frac{1}{1 - (Q^2 \cdot \sigma_r^2)} \right] \quad \text{and} \quad \sigma_r^2 = 4 \cdot \text{BWr} \cdot 10^{\frac{\text{RIN}}{10}}$$

where BWr is the receiver bandwidth in Hz, and Q is 7.03 for BER of 1 in 10^{12}

Two basic effects of chromatic dispersion

Chromatic dispersion: *different propagation velocities of light components having different colours.*

It leads to two different effects:

- pulse spread, resulting in ISI;
- Mode Partition Noise (MPN)

Pulse broadening and ISI

The ISI-caused chromatic dispersion penalty (in dB) can be estimated as follows[4]:

$$P_{\text{ISI}} = 5 \log [1 + 2 \pi (B D L \sigma_{\lambda})^2]$$

where B is Baud rate, D is fiber chromatic dispersion coefficient, L is link length and σ_{λ} is the RMS spectral width of laser.

However, this is a poor estimate of P_{ISI} . We will improve it later.

Mode partition noise (MPN)

Partitioning of laser power between laser modes does not change the total transmitted power and does not cause additional noise at the laser output.

However, different laser modes travel at different velocities in the fiber.

As a result, power fluctuations between modes lead to MPN at the fiber output.

Mode partition noise penalty

The power penalty in dB due to MPN can be estimated as [4]:

$$P_{\text{mpn}} = 5 \log [1 / (1 - Q_a^2 \sigma_{\text{mpn}}^2)]$$

where Q_a is the desired argument of:

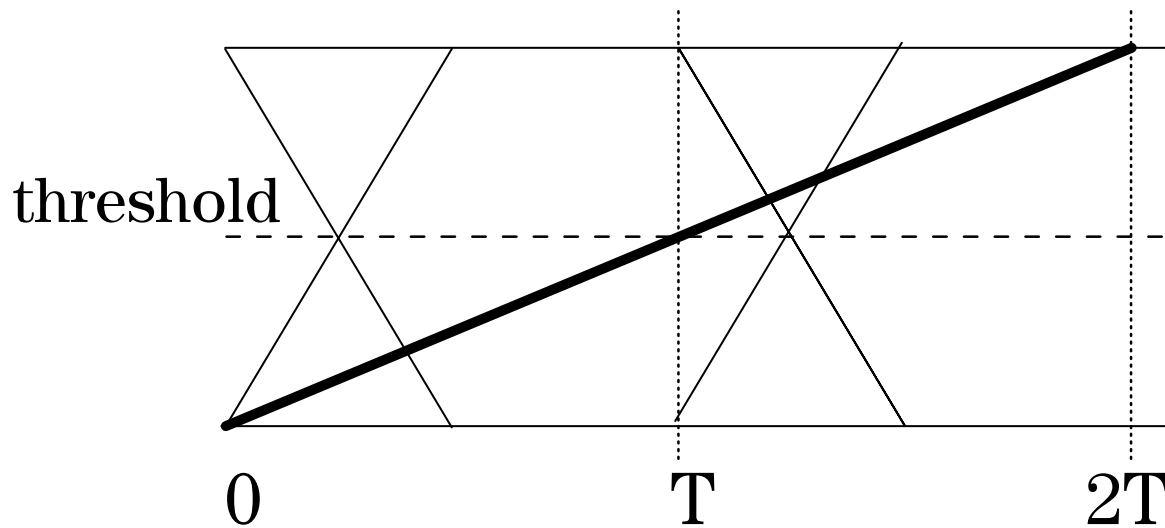
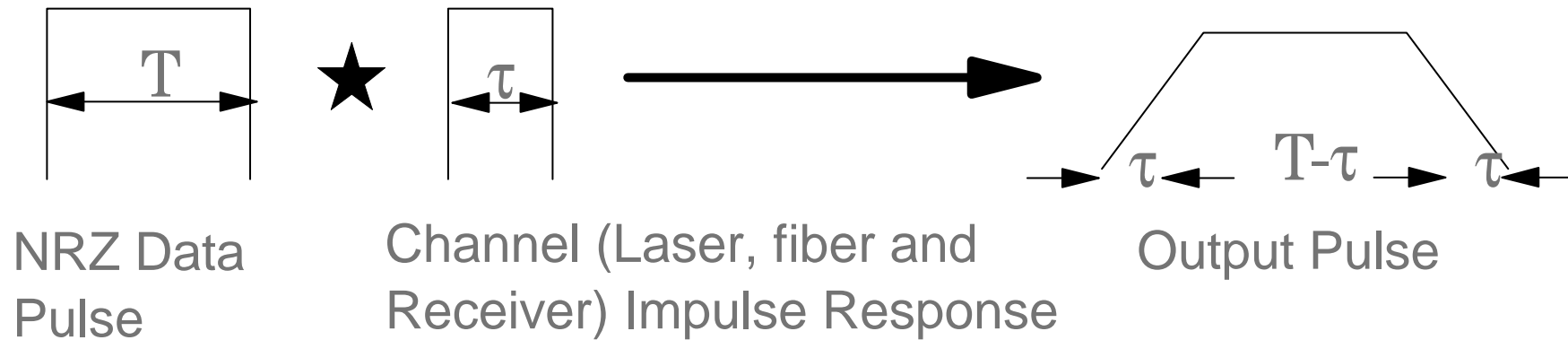
$$\text{BER}(Q) = [Q (2 \pi)^{1/2}]^{-1} \exp(- Q^2 / 2)$$

and

$$\sigma_{\text{mpn}}^2 = (k / 1.414) [1 - \exp\{ - (\pi B D L \sigma_\lambda^2) \}]$$

σ_{mpn}^2 is the MPN variance.

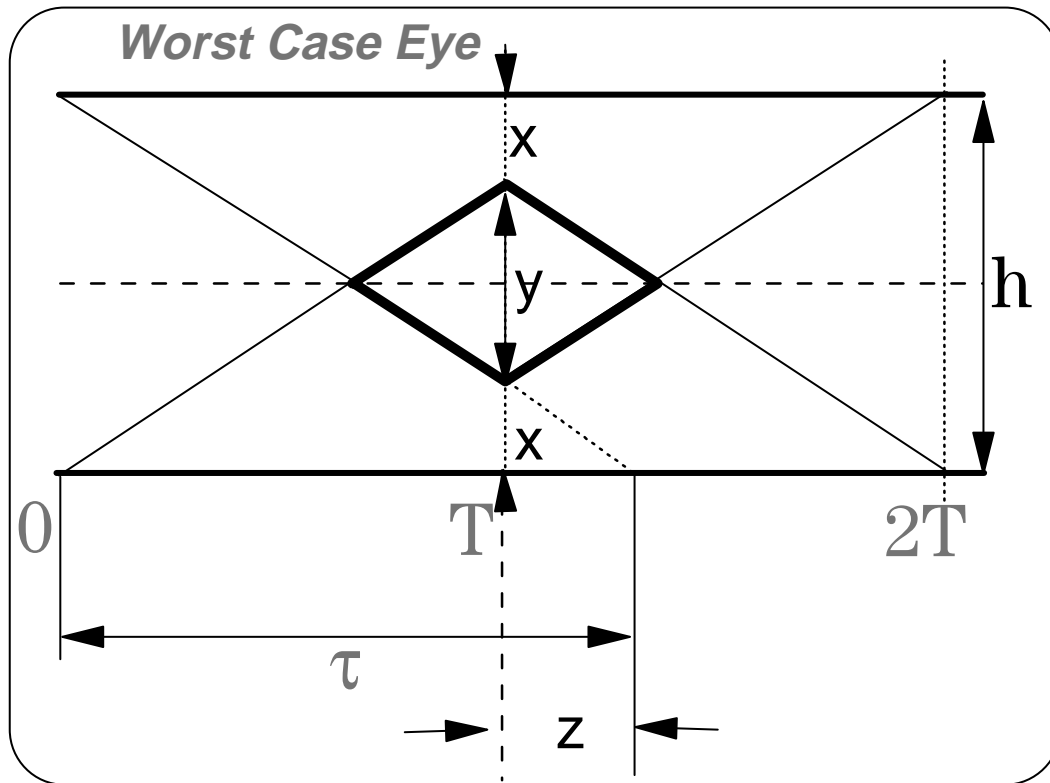
ISI in a Unequalized Optical Receiver: *Trapezoidal Output*



- Eye Fully Open for $T_c < 0.8 T$
- Eye Closed for $T_c = 1.6 T$
- T_c is 10% -90% risetime

★ See reference 3 for more details

ISI in an Unequalized Optical Receiver: Trapeziodal Output for $T_c > 0.8 T$



The ISI penalty, P_{isi} , is:

$$P_{isi} = h/y$$

$$= \tau / (2T - \tau)$$

But $T_c = 0.8\tau$

so that for $T_c > 0.8T$:

$$P_{isi} = T_c / (1.6 - T_c)$$

$P_{isi} = \text{zero}$ otherwise

ISI in an Unequalized Optical Receiver: *Arbitrary Output Pulse Shapes*

The ISI penalty is given by [3]: $P_d = 10 \log \left(\frac{1}{1 - E_m} \right)$

$$\text{where } E_m = 2 \left(1 - \int_{-\infty}^{\infty} H_p(f) \cdot H_f(f) \cdot H_r(f) \cdot e^{-i \cdot 2 \cdot \pi \cdot f \cdot t_0} df \right)$$

$H_p(f)$ is spectrum of the data pulse, $H_f(f)$ is the transfer function of the laser and fiber, $H_r(f)$ is the transfer function of the receiver and t_0 is the sampling time.

Multimode Fiber Links

Multimode fiber systems are usually approximated by an overall gaussian impulse response.

For NRZ data pulses and the gaussian product $H(f)H_r(f)$, E_m is given by:

$$E_m = 2 - 4 \int_{-\infty}^{\infty} \frac{\sin \left(\pi \cdot \frac{f}{B} \right)}{\pi \cdot f} \cdot \exp \left[-\frac{(2 \cdot \pi \cdot f \cdot \sigma)^2}{2} \right] \cdot \exp(i \cdot 2 \cdot \pi \cdot f \cdot t_0) df$$

ISI in an Unequalized Optical Receiver: *Link with Gaussian Impulse Response*

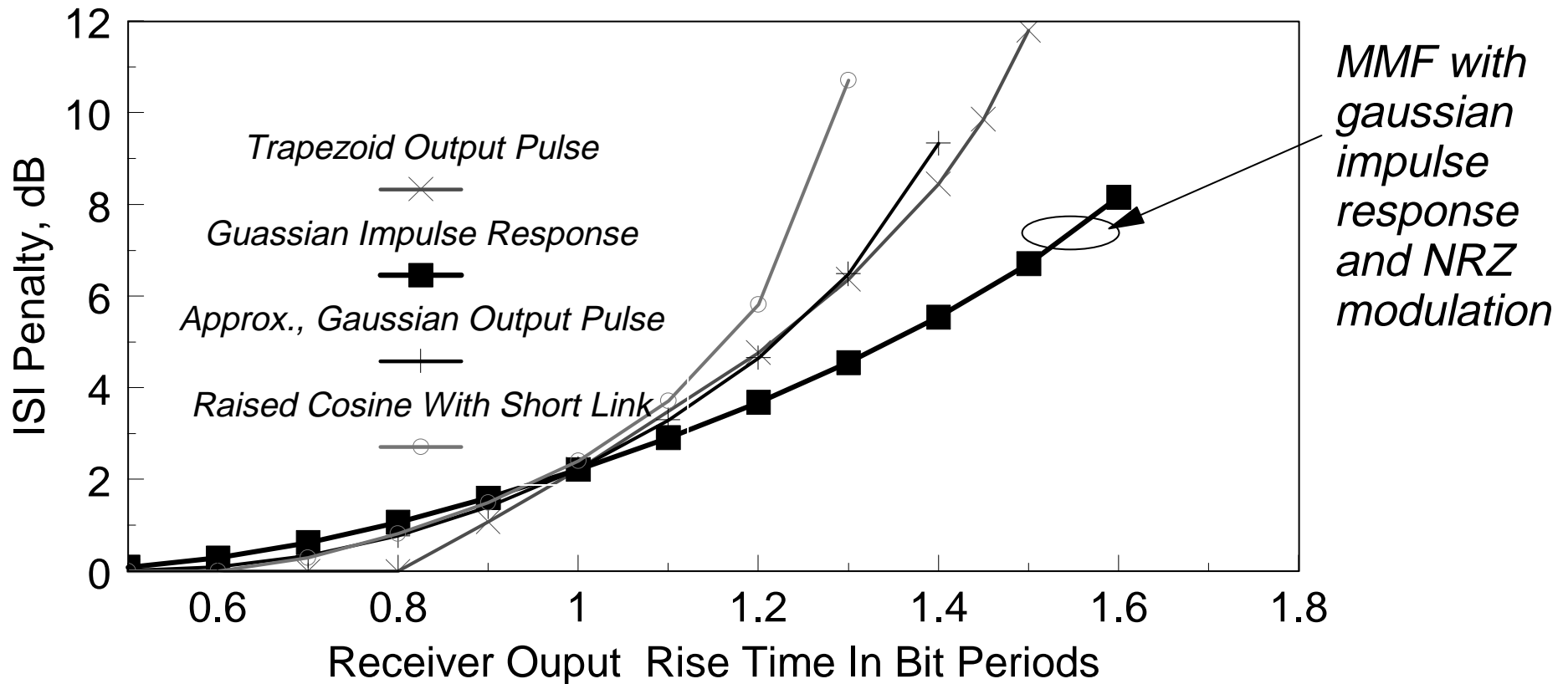
$$E_m = 2 - 4 \int_{-\infty}^{\infty} \frac{\sin\left(\pi \cdot \frac{f}{B}\right)}{\pi \cdot f} \cdot \exp\left[-\frac{(2 \cdot \pi \cdot f \cdot \sigma t)^2}{2}\right] \cdot \exp(i \cdot 2 \cdot \pi \cdot f \cdot t_0) df$$

The power penalty (**Pisi**) for the MMF link, with an assumed gaussian impulse response, was estimated by calculating **E_m** numerically. The numerically calculated curve was found to be well approximated by:

$$P_{isi} = 10 \cdot \log \left[\frac{1}{1 - 1.425 \exp\left[-1.28 \left(\frac{T_b}{T_c}\right)^2\right]} \right]$$

Penalties from ISI: *Theory*

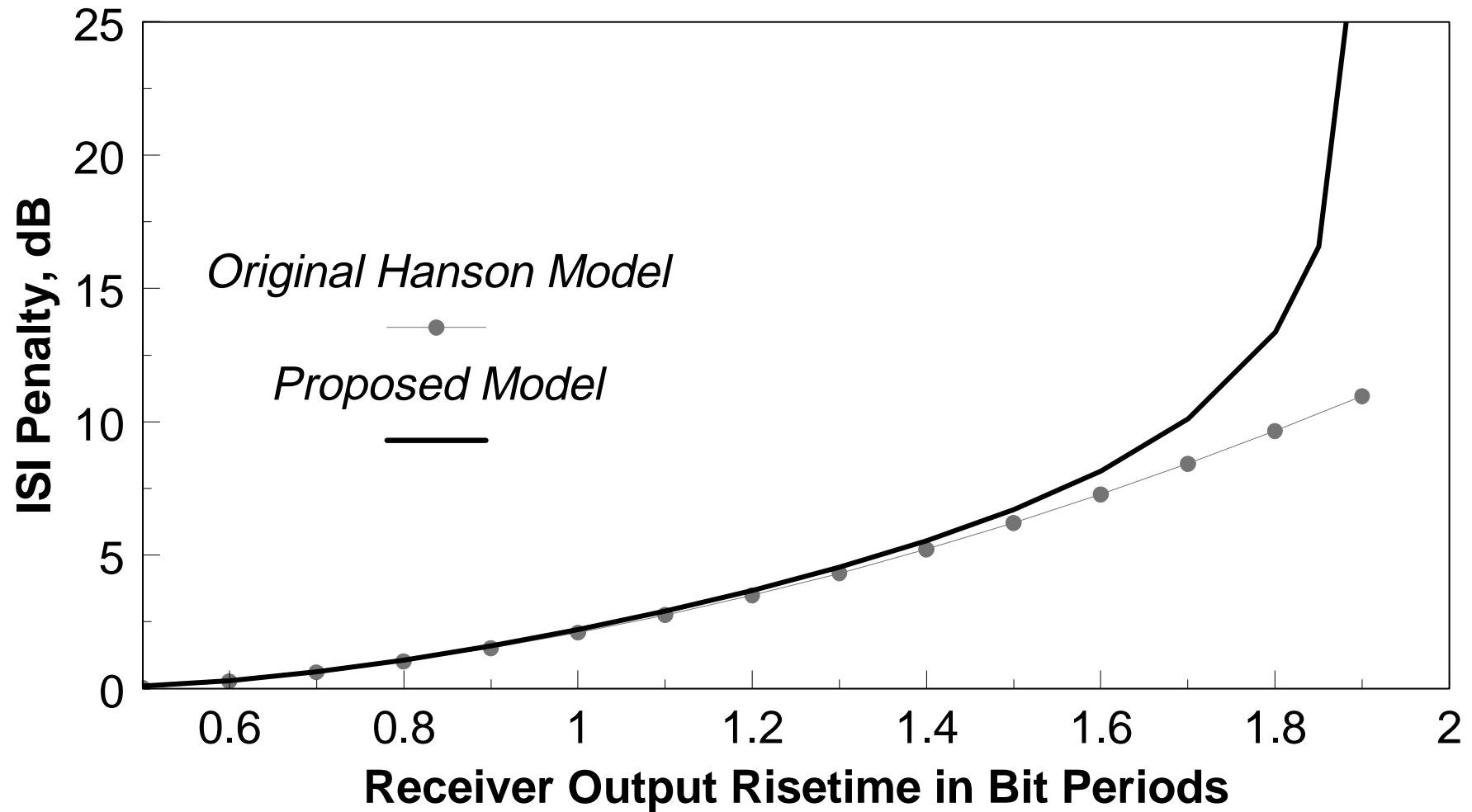
Penalties From ISI for Various Output Pulse Shapes
(Theory of reference 3 used for calculations)



- ▶ *If the output pulse rise time is greater than the bit period then the worst case ISI penalty depends on receiver output pulse shape.*

Comparison of ISI Models: *Theory*

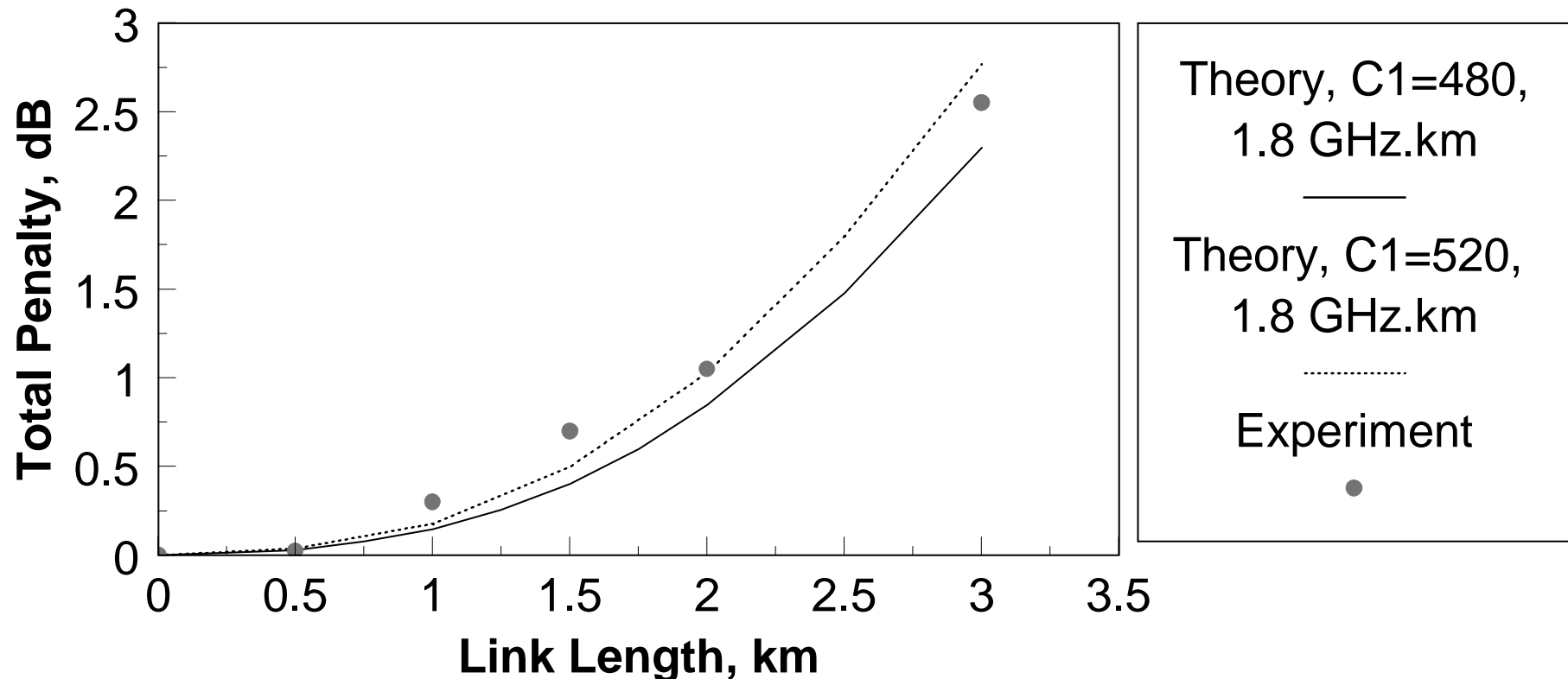
Penalty from ISI Versus Output Pulse Rise Time



Comparison of Theory & Experiment:

Long Wavelength Link With Typical Components

Power Penalty Versus Link Length

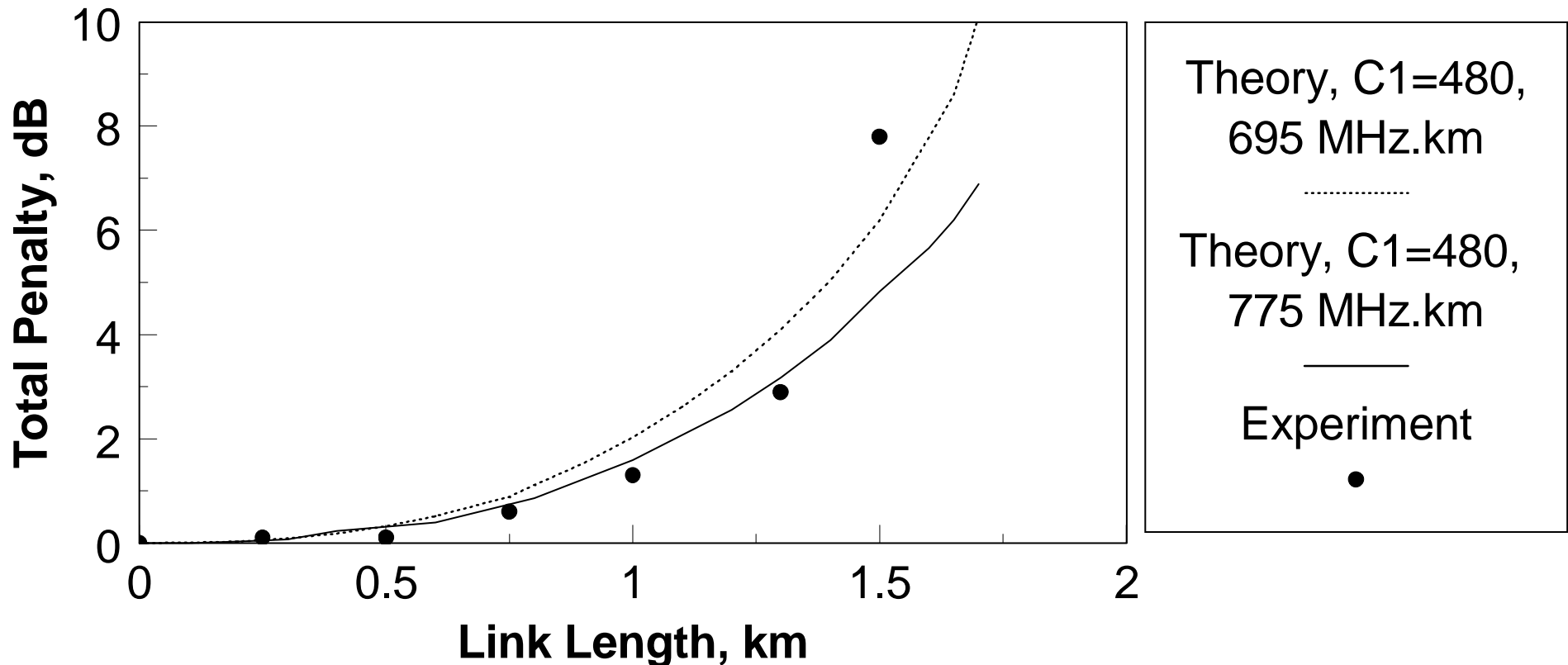


*HP coaxial laser, 1318 nm, 1.5 nm rms width, $k=0.5$, $T_s=350$ ps, $RIN = -137$ dB/Hz
62MMF, 2 GHz.km modal bandwidth, Zero Dispersion=1377nm, $S_o=0.084$ ps/(nm².km),
ALL ABOVE TRANSCEIVER AND FIBER PARAMETERS WERE MEASURED BY HPLB*

Comparison of Theory & Experiment:

Short Wavelength (857 nm) Link With Typical Components

Power Penalty Versus Link Length

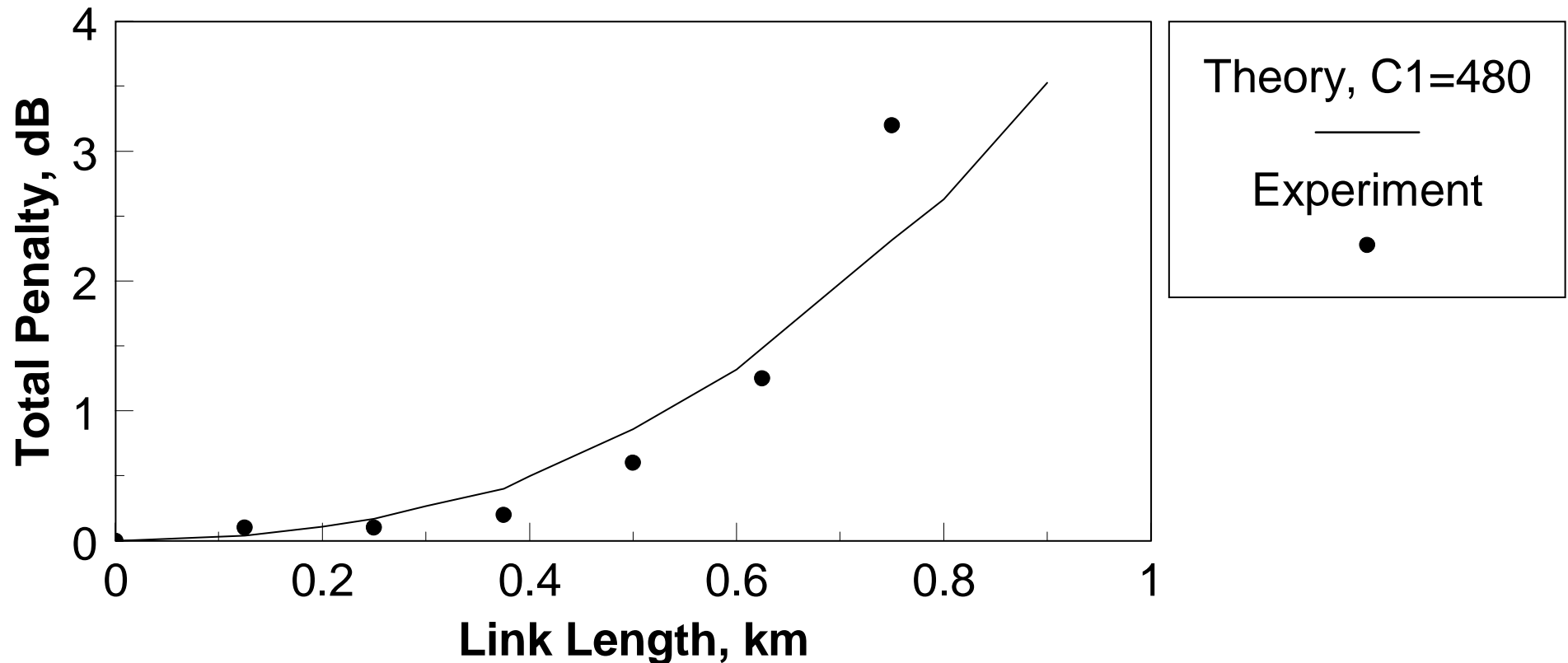


*SW (FP) laser, 857 nm, 0.85 nm rms width, $k=0.85$, $T_s=300$ ps, $RIN=-125$ dB/Hz
62MMF, 775 MHz.km modal bandwidth, Zero Dispersion=1377nm, $S_o=0.084$ ps/(nm.km)
ALL ABOVE TRANSCEIVER AND FIBER PARAMETERS WERE MEASURED BY HPLB*

Comparison of Theory & Experiment:

Short Wavelength (770 nm) Link With Typical Components

Power Penalty Versus Link Length



*SW (FP) laser, 794 nm, 0.8 nm rms width, $k=0.85$, $T_s=300$ ps, $RIN=-120$ dB/Hz
62MMF, 525 MHz.km modal bandwidth, Zero Dispersion=1377nm, $S_o=0.084$ ps/(nm.km)²
ALL ABOVE TRANSCEIVER AND FIBER PARAMETERS WERE MEASURED BY HPLB*

Conclusions

- We have developed an analytical model for laser based multimode fiber links;
 - *Using the original Del Hanson model for LED based links as the starting point,*
 - *Inserting additional terms specific to laser based links.*
- We have shown that the model accurately predicts the link penalties for laser based links operating at wavelengths of 770 nm, 850 nm and 1300 nm.
- A spread sheet model has been developed which will be the basis of "Link Lengths For 850 nm & 1300 nm Optical PMDs With All Link Penalties" to be presented by Del Hanson.

References

1. ANSI T1.646-1995, Broadband ISDN-Physical Layer Specification For User-Network Interfaces, Appendix B.
2. Gair D. Brown, "Bandwidth and Rise Time Calculations for Digital Multimode Fiber-Optic Data Links", Journal of Lighthwave Technology, VOL. 10, No. 5, May 1992, pp 672-678.
3. James L. Gimlett and Nim K. Cheung, "Dispersion Penalty Analysis for LED/Single-Mode Fiber Transmission Systems", Journal of Lighthwave Technology, VOL., LT-4, No. 9, Sept., 1986, pp 1381-1392.
4. Govind P. Agrawal, P. J. Anthony and T. M. Shen, "Dispersion Penalty for 1.3- μm Lightwave Systems with Multimode Semiconductor Lasers", Journal of Lightwave Technology, VOL., 6, No. 5, May., 1988, pp 620-625.