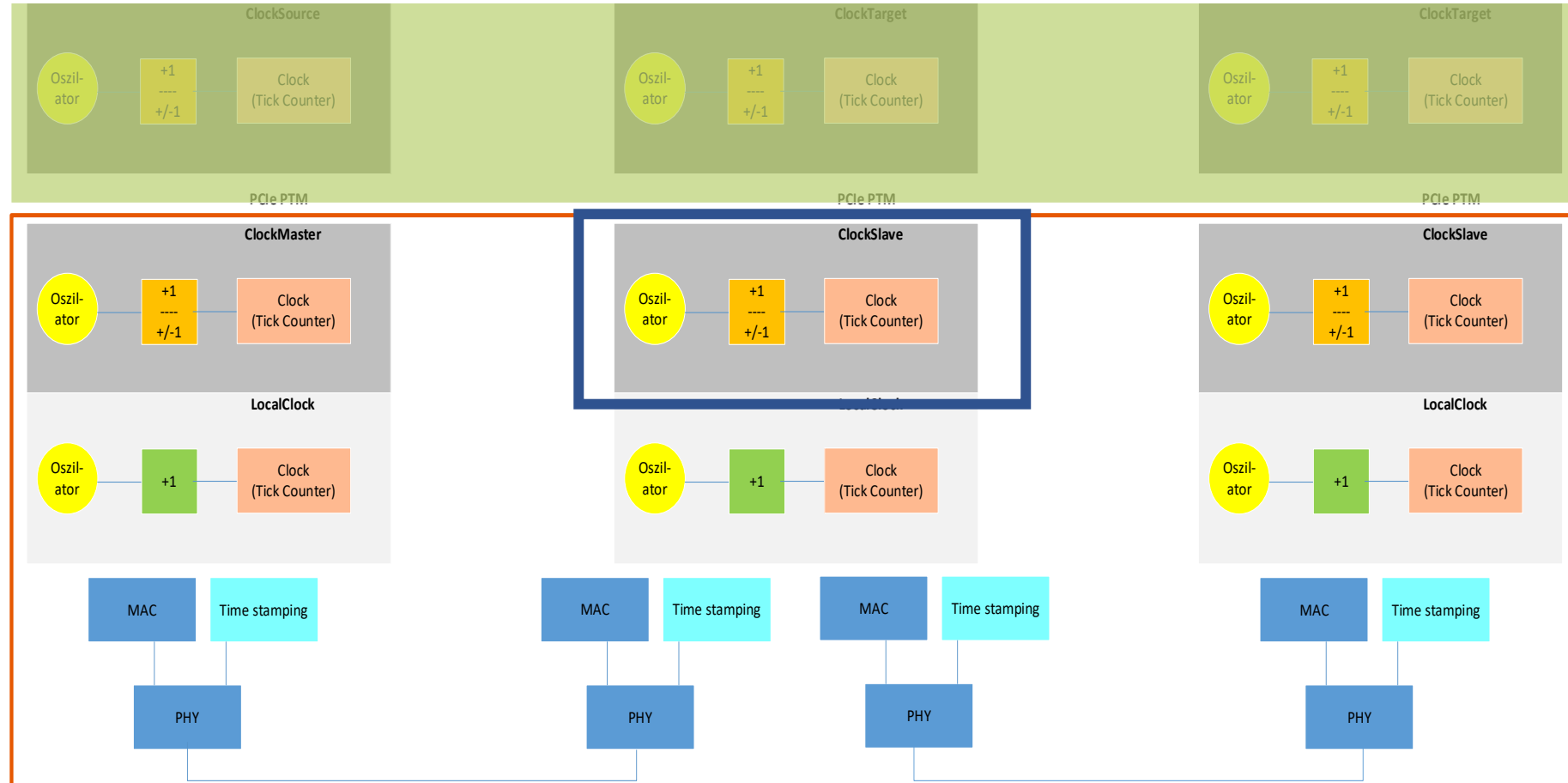


ClockSlave PI Controller: Definition and Implementation

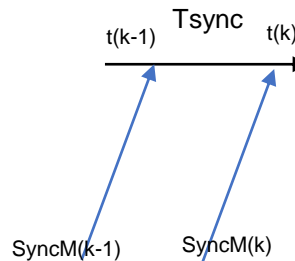
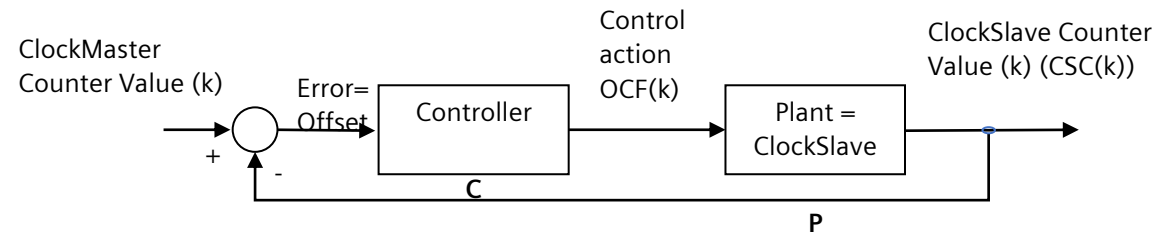
Dragan Obradovic, Siemens AG

ClockSlave



ClockSlave Control Loop

- Control loop necessary to enable „**tracking**“ of the ClockMastertime (“MasterTime”) by ClockSlave
- **Offset**: difference between the MasterTime the slave “n” becomes via Sync Messages (corrected by the pDelay) and the ClockMaster time
- **OCF**: controller output, which scales the frequency of the free running clock (e.g. LocalClock) in order to minimize Offset
- Frequency scaling achieved by changing the number of ticks of the free running clock by ± 1 in appropriate time intervals



- Controller is active only at the arrival of Sync Message
 - Sync Messages arrive periodically with the period of $\sim T_{sync}$ (Sync interval at the GM)
- ➔ The controller is practically time-discrete

ClockSlave Control Loop: Time Discrete Representation

- **Controller:** → time discrete PI controller

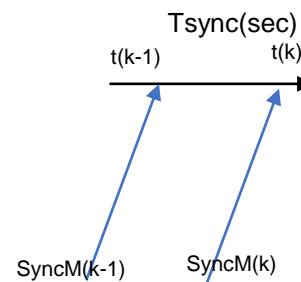
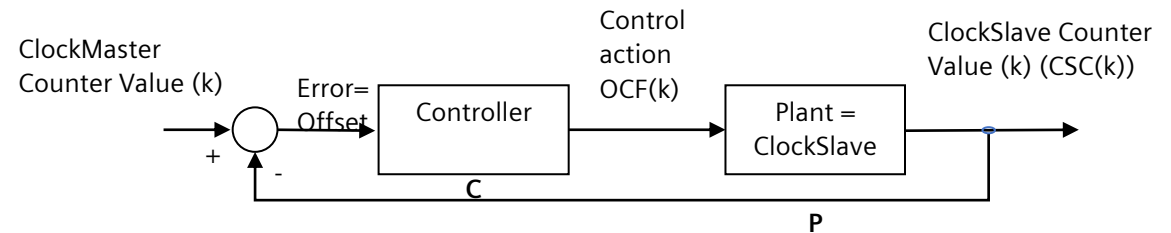
$$OCF(k) = OCF(k - 1) + K_p \cdot (Offset(k) - Offset(k - 1)) + K_I \cdot Offset(k - 1) \cdot T_{sync}$$

$$OCF(z) = \frac{K_p \cdot (z - 1) + K_I \cdot T_{sync}}{z - 1} \cdot err(z)$$

- **Plant (ClockSlave):** an integrator of the free running clock frequency (f_{nom} : nominal and f_t : true frequency)

$$CSC(k) = CSC(k - 1) + OCF(k - 1) \cdot f_t \cdot T_{sync}$$

$$CSC(z) = \frac{f_t \cdot T_{sync}}{z - 1} \cdot OCF(z)$$



$$K_p = \frac{K_{p1}}{f_{nom} \cdot 1sec}; K_I = \frac{K_{I1}}{f_{nom} \cdot 1sec^2}$$

Where K_{p1} and K_{I1} are the parameters of the time continuous PI controller (optimized for a pure integrator) as the plant which was discretized

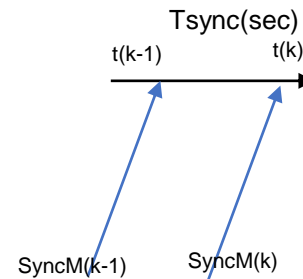
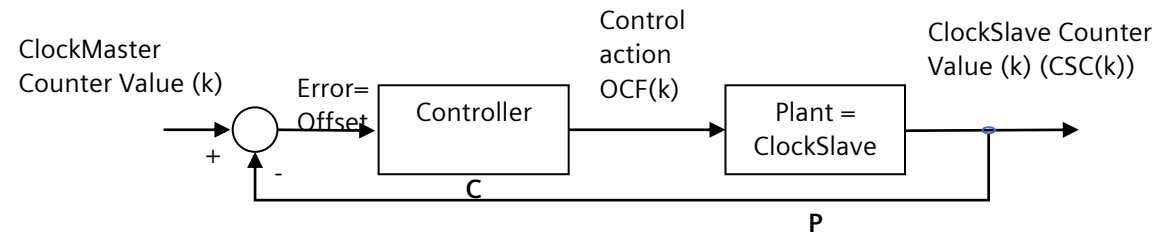
ClockSlave Control Loop: Time Discrete Representation

- **OpenLoop:** $\rightarrow P \cdot C$

$$CSC(z) = \frac{f_t \cdot T_{sync}}{z-1} \cdot \frac{K_p \cdot (z-1) + K_I \cdot T_{sync}}{z-1} \cdot Offset(z)$$

$$= \frac{T_{sync} \cdot f_t}{f_{nom}} \cdot \frac{K_{p1} \cdot (z-1) + K_{I1} \cdot T_{sync}}{(z-1)^2} \cdot Offset(z)$$

- \rightarrow The plant, and consequently the whole control loop, is linear time-invariant only if f_t is constant
- \rightarrow If f_t is constant but different from the nominal frequency, the ratio $\frac{f_t}{f_{nom}}$ changes the gain of the OL; the controller has to be able to deal with this uncertain gain (its gain margin has to be appropriately large)



$$K_p = \frac{K_{p1}}{f_{nom} \cdot 1sec}; \quad K_I = \frac{K_{I1}}{f_{nom} \cdot 1sec^2}$$

Where K_{p1} and K_{I1} are the parameters of the time continuous PI controller) optimized for a pure integrator) as the plant which was discretized

ClockSlave Control Loop: Time Discrete Representation and Implementation

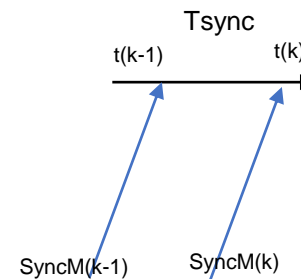
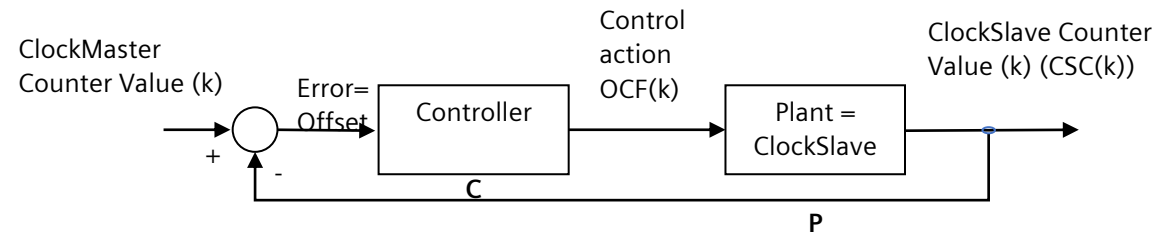
- **Controller:** → time discrete PI controller

OCF provides information about how many ticks have to be added/subtracted to the number of ticks of the free running clock (e.g. Local Clock) within T_{sync}

→ We can calculate the time interval in the free running clock (its number of ticks) when the change of one tick takes place

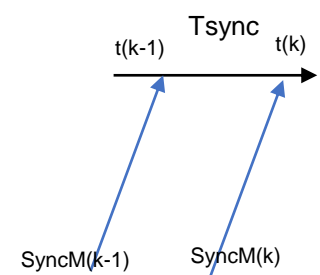
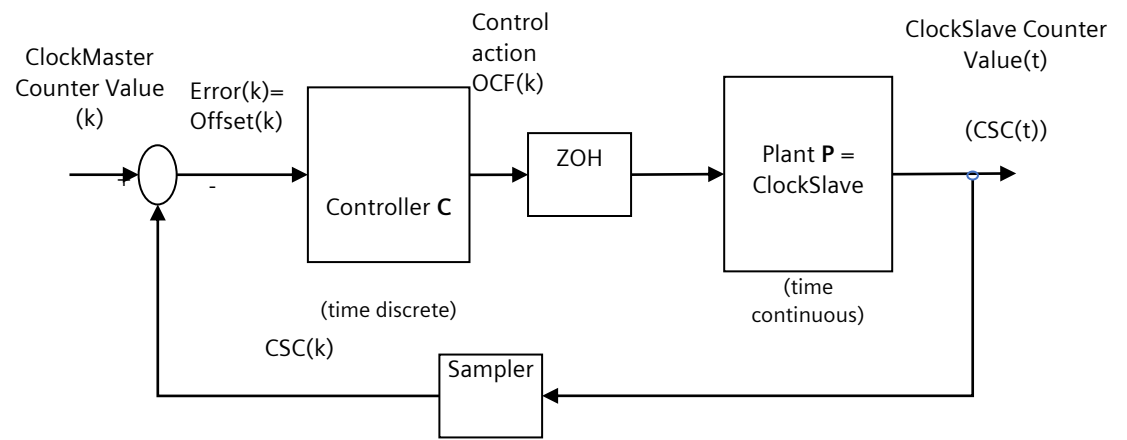
$$OCF_{interval}(k) = \text{round} \left(\frac{\text{sign}(OCF(k) - 1)}{OCF(k) - 1} \right)$$

The change in ticks is given by: $\text{sign}(OCF(k) - 1)$, hence it can be zero or ± 1



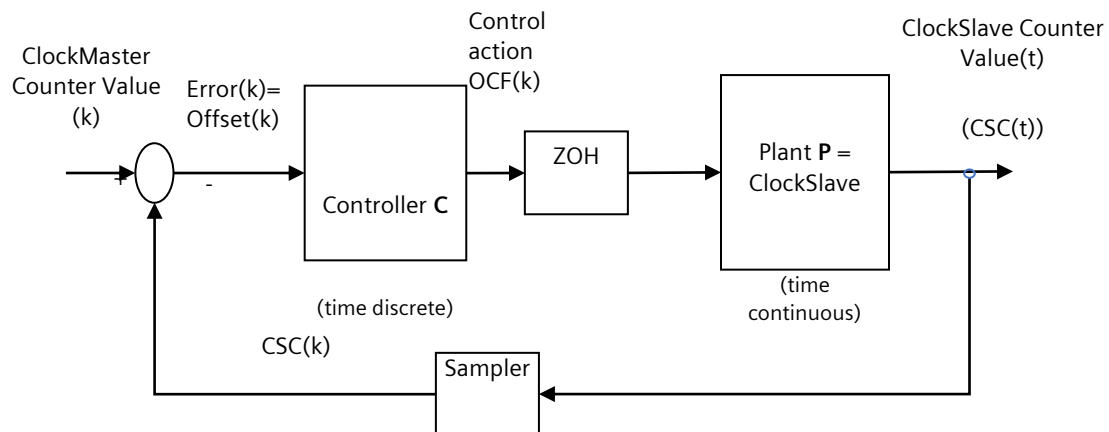
ClockSlave Control Loop: Mixed Time Discrete & Time Continuous Representation

- Time discrete representation of the closed loop: signals are calculated and transmitted only at the discretization events (arrival of Sync Messages)
- But ClockSlave provides time continuously!
- How is this achieved?: → by ZOH function, i.e. by making the time discrete output of the PI controller constant within the sampling interval

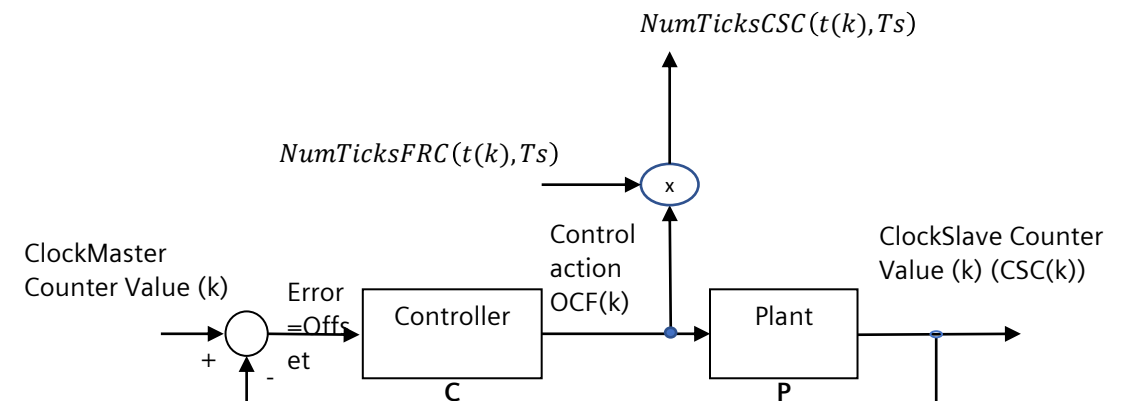


ClockSlave Control Loop: Mixed Time Discrete & Time Continuous Representation

- Alternative Representations



- The ClockSlave time is available continuously!



ClockSlave Control Loop Characteristics

- **Bandwidth:** determined by T_{sync} (we cannot track frequencies of the MasterTime changes with a period $< T_{sync}$)
 - have T_{sync} and $pDelay$ request intervals small
- **Noise:** the MasterTime is noisy (we have to keep the signal2noise ratio large enough)
 - reduce stamping errors, have T_{sync} and the $pDelay$ intervals large (contradicting the bandwidth recommendation)
- **Tracking Delay:** MasterTime information is delayed by aggregated ResidenceTimes and $pDelays$; Other delays also play a role
 - Have short ResidenceTimes

