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Re:	802.16aD4 and 802.16cD1				
Abstract	This paper proposes a method for using non-squared constellations and how to decode them with independent I and Q.				
Purpose	To be used by TGa and TGc for discussion and to help preparing the draft document.				
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Juan Alberto Torres

Proposal

This paper proposes a method for using non-squared constellations and how to decode them with independent I and Q.

Discussion

Background

When designing a constellation, there is always a concern of the ease of decoding the received signals. For blind decisions, one must both find the nearest point and its numeric representation.

The easiest constellations to use are those that are square with an even power of two number of symbols. These square constellations are sometimes called even constellations because of this even power. The design of the mapping of square constellations is based upon one dimensional mapping techniques that are extended to two dimensions.

One-Dimensional Constellation Mapping

Most one dimensional constellations attempt ease encoding and decoding by algebraically manipulating their numeric value directly to create the transmit signal value. For example, consider the follow one-dimensional mapping:

numeric value	signal value
0	-3
1	-1
2	+1
3	+3

signal value = (numeric value * 2) - 3

One Dimensional Constellation Decisions

The efficient decoding of evenly spaced one-dimensional constellations relies upon the truncation operation inherent when masking binary numbers. By representing the received signal in M.N two complement integer mathematics, the decoder can mask all bits of a power of 2^0 and lower. The decision can be accomplished as follows:

signal value = ((received value) & MASK) + 1

where MASK removes all bits with position 2⁰ or smaller.

Direct Constellation Bit Mapping

It can be directly observed that there are simpler numeric values to signal value translation than the one given above. The following mapping directly maps bits of the signal value to the numeric value. The decoder would have the values of:

numeric value	bit value	signal value	bit value vv
2	10	-3	1111101.00
3	11	-1	1111111.00
0	00	+1	0000001.00
1	01	+3	0000011.00

signal value = (sign extended numeric value * 2) + 1 numeric value = bit positions 2 and 1 of signal value

The decision/decoder now becomes:

signal value = ((received value) & MASK) + 1 numeric value = bit positions 2 and 1 of signal value

Two-Dimension Even Square Constellation Mapping

The extension to two-dimensional even square constellations is elementary. One can provide independent bit groupings in the numeric value and independent dimensional constellation mapping. For example, extending the previous example:

numeric value	bit value	bit value(I Q)	signal value (I, Q)	vv	vv
12	1100	10 10	-3,-3	1111101.00	1111101.00
13	1101	10 11	-3,-1	1111101.00	1111111.00
8	1000	10 00	-3,+1	1111101.00	0000001.00
9	1001	10 01	-3,+3	1111101.00	0000011.00
14	1110	11 10	-1,-3	1111111.00	1111101.00
15	1111	11 11	-1,-1	1111111.00	1111111.00
10	1010	11 00	-1,+1	1111111.00	0000001.00
11	1011	11 01	-1,+3	1111111.00	0000011.00
4	0100	00 10	+1,-3	0000001.00	1111101.00
5	0101	00 11	+1,-1	0000001.00	1111111.00
0	0000	00 00	+1,+1	0000001.00	0000001.00
1	0001	00 01	+1,+3	0000001.00	0000011.00
6	0110	01 10	+3,-3	0000011.00	1111101.00
7	0111	01 11	+3,-1	0000011.00	1111111.00
2	0010	01 00	+3,+1	0000011.00	0000001.00
3	0011	01 01	+3,+3	0000011.00	0000011.00

Notice the I and Q values are formed by reordering the bits of the numeric value.

Two-Dimension Even Square Constellation Decoding

The decision/decoder is created by using two one-dimensional decoders. This attribute allows an easy decoder to be created as:

numeric value = bit positions for
$$2^2$$
 and 2^1 of signal value I and bit positions for 2^2 and 2^1 of signal value Q

The numeric value is formed by moving the signal value bits to the appropriate numeric positions.

For each symbol, there are the following operations:

AND 2 OR 2

Two-Dimension Odd Square Constellation Mapping

While it is slightly more complicated, one can produce similar results for square with an odd power of two number of symbols. These constellations are produced from removing half the symbols of an even square constellation. Consider, for example, a square even constellation of 2⁴ points:

numeric value	bit value (I Q)	bit value (I, Q)	signal value	vv	vv
12	1100	10 10	-3,-3	1111101.00	1111101.00
13	1101	10 11	-3,-1	1111101.00	1111111.00
8	1000	10 00	-3,+1	1111101.00	0000001.00
9	1001	10 01	-3,+3	1111101.00	0000011.00
14	1110	11 10	-1,-3	1111111.00	1111101.00
15	1111	11 11	-1,-1	1111111.00	1111111.00
10	1010	11 00	-1,+1	1111111.00	0000001.00
11	1011	11 01	-1,+3	1111111.00	0000011.00
4	0100	00 10	+1,-3	0000001.00	1111101.00
5	0101	00 11	+1,-1	0000001.00	1111111.00
0	0000	00 00	+1,+1	0000001.00	0000001.00
1	0001	00 01	+1,+3	0000001.00	0000011.00
6	0110	01 10	+3,-3	0000011.00	1111101.00
7	0111	01 11	+3,-1	0000011.00	1111111.00
2	0010	01 00	+3,+1	0000011.00	0000001.00
3	0011	01 01	+3,+3	0000011.00	0000011.00

By removing every other symbols, in a two dimensional sense, in the I/Q plane, produces the following odd constellation of 2^3 points.

numeric value	bit value (I Q)	bit value (I,Q)	signal value	VV	VV
12	1100	10 10	-3,-3	1111101.00	1111101.00
8	1000	10 00	-3,+1	1111101.00	0000001.00
15	1111	11 11	-1,-1	1111111.00	1111111.00
11	1011	11 01	-1,+3	1111111.00	0000011.00
4	0100	00 10	+1,-3	0000001.00	1111101.00
0	0000	00 00	+1,+1	0000001.00	0000001.00
7	0111	01 11	+3,-1	0000011.00	1111111.00
3	0011	01 01	+3,+3	0000011.00	0000011.00

The 4 data bits are combined using the least significant bit as a common two-dimensional mapping bit, namely:

numeric value	bit value I Q common	bit value (I, Q)	signal value	v	v
6	110	110	-3,-3	1111101.00	1111101.00
4	100	100	-3,+1	1111101.00	0000001.00
7	111	111	-1,-1	1111111.00	1111111.00
5	101	101	-1,+3	1111111.00	0000011.00
2	010	010	+1,-3	0000001.00	1111101.00
0	000	0 0 0	+1,+1	0000001.00	0000001.00
3	011	011	+3,-1	0000011.00	1111111.00
1	001	0 0 1	+3,+3	0000011.00	0000011.00

Two-Dimension Odd Square Constellation Decoding

Though square, one cannot apply the techniques used for the even square constellations directly to the odd constellations. This is because the decision regions are shaped as diamonds (rotated squares). To combat this problem, the following decision/decoding strategy is used:

- a. rotate the constellation forward by 45 degrees
- b. make independent I and Q decisions
- c. rotate the constellation back by 45 degrees

This following procedure illustrates this technique.

```
rotated value I =
                       received value I - received value Q
rotated value Q =
                       received value Q + received value I
rotated value I =
                       (rotated value I/2 + 1) & MASK
rotated value Q =
                       (rotated value Q / 2 ) & MASK
                       rotated value I + rotated value Q + 1
signal value I =
signal value Q =
                       rotated value Q - rotated value I+1
                       bit positions for 2 2 signal value I and
numeric value =
                       bit positions for 2<sup>2</sup> signal value Q and
                       bit position 2<sup>1</sup> of signal value I or Q
```

The numeric value is formed by moving the signal value bits to the appropriate numeric positions.

For each symbol, there are the following operations:

ADD 5 SHIFT 2 AND 2 OR 2

Though almost three times as expensive in primitive operations as the even square constellation, this odd square constellation can be still be decoded in a very small number of primitive operations.