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Title	<b>Space-frequency bit-interleaved coded modulation for MIMO-OFDM/OFDMA systems</b>	
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Source(s)	Sumeet Sandhu, Nageen Himayat, Shilpa Talwar, David Cheung, Qinghua Li <b>Intel Corporation</b>	<a href="mailto:sumeet.sandhu@intel.com">sumeet.sandhu@intel.com</a> Voice: +1-408-765-8558
Re:		
Abstract	<p>One of the smart antenna options in the 802.16e standard is multiple-input, multiple-output (MIMO) systems. MIMO requires multiple antennas at both the transmitter and receiver. Multiple transmit antennas can be used in diversity mode to provide greater range or in spatial multiplexing mode to provide higher throughput. The spatial multiplexing MIMO modes in sections 8.4.8.3.3, 8.4.8.3.4, 8.4.8.3.5, 8.4.8.4.3, and 8.4.8.9 consist of simple spatial multiplexing on 1-4 transmit antennas, with no coding across transmit antennas. On each antenna, independent spatial streams with frequency-only bit-interleaved coded modulation (F-BICM) are transmitted. That is, FEC blocks of convolutionally coded input bits are interleaved across frequency tones but not across transmit antennas.</p> <p>In this contribution we propose space-frequency bit-interleaved coded modulation (SF-BICM) which interleaves FEC blocks across both spatial streams and frequency tones. Spatial streams are multiple data streams transmitted over multiple antennas, with or without some form of spatial pre-coding such as beamforming, covariance weighting or singular value decomposition. Space-frequency interleaving provides spatial diversity in addition to frequency diversity, especially with minimum mean squared error (MMSE) spatial filters per tone. Performance of the proposed SF-BICM is compared to simple spatial multiplexing (F-BICM) over 2x2 spatially i.i.d ITU channels. The proposed SF-BICM outperforms F-BICM by 1-3 dB for 200 byte packets.</p>	
Purpose	Adoption of proposed changes into P802.16e <del>Crossed-out indicates deleted text</del> , <u><a href="#">underlined blue indicates new text change to the Standard</a></u>	
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# Space-frequency bit-interleaved coded modulation for MIMO

Sumeet Sandhu, Nageen Himayat, Shilpa Talwar, David Cheung, Qinghua Li  
Intel Corporation

## 1 Background

The spatial multiplexing MIMO modes in sections 8.4.8.3.3, 8.4.8.3.4, 8.4.8.3.5, 8.4.8.4.3, and 8.4.8.9 consist of simple spatial multiplexing on 1-4 transmit antennas, with no coding across transmit antennas. On each antenna, independent spatial streams with frequency-only bit-interleaved coded modulation (F-BICM) are transmitted. That is, FEC blocks of convolutionally-coded input bits are interleaved across frequency tones but not across transmit antennas.

In this contribution we propose space-frequency bit-interleaved coded modulation (SF-BICM) which interleaves FEC blocks across both transmit antennas (or spatial streams) and frequency tones. Space-frequency interleaving provides spatial diversity in addition to frequency diversity, especially with minimum mean squared error (MMSE) spatial filters per tone.

## 2 Proposed text change

[Add a new section 8.4.8.10 as follows]

### 8.4.8.10 Space-frequency bit-interleaved coded modulation (SF-BICM)

This section describes 4 steps for mapping bits to multiple spatial streams and tones. The key changes are steps 1, 2 and 4, and are circled in red in the figure below.

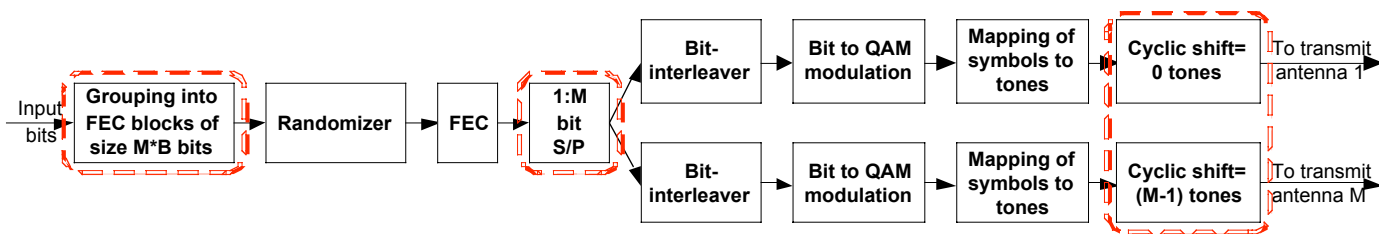


Figure 1: Space-frequency bit-interleaved coded modulation (SF-BICM)

Let  $M$  be the number of spatial streams (where  $M$  is less than or equal to the number of transmit antennas),  $B$  the number of uncoded bits in 1 SISO FEC block,  $N_{CBPS}$  the number of coded bits per convolutionally-coded FEC block (as in Section 8.4.9),  $N$  the FFT size,  $N_{DS}$  the number of tones occupied by  $N_{CBPS}$  bits, and  $q$  the number of bits per QAM symbol.

### SF-BICM TRANSMITTER

- 1) **FEC encoding:** The incoming uncoded bits are grouped into blocks of size  $MB$  and encoded with the usual convolutional code and punctured. The coded output blocks are of size  $MN_{CBPS}$ .

The following steps apply to each FEC block.

- 2) **Serial to parallel multiplexing:** The FEC block is multiplexed to different spatial streams. The bits indexed by  $m:M:MN_{CBPS}$  are mapped to the  $m^{th}$  spatial stream for  $m=1, \dots, M$ .
- 3) **802.16e interleaving and tone mapping:** The resulting groups of  $N_{CBPS}$  bits on each spatial stream are interleaved according to the 802.16e interleaver and Gray mapped to QAM symbols. The resulting QAM symbols are mapped to  $N_{DS}$  tones according to 802.16e sub-channelization and tone-mapping. The same set of tones is occupied on each spatial stream.
- 4) **Cyclic tone shift:** The final step consists of cyclically shifting the symbol sequence mapped to the  $m^{th}$  spatial stream by  $m-1$  tones to the right.

## SF-BICM RECEIVER

In order to map received symbols to bit estimates, the receiver performs steps 1-4 in the reverse order. The output of the per-tone spatial demapper such as MMSE or ML is soft bits.

- 1) **Reverse cyclic tone shift:** The soft bits on the  $m^{th}$  spatial stream are shifted to the left by  $m-1$  tones.
- 2) **802.16e tone demapping and de-interleaving:** The bits on each spatial stream are demapped and de-interleaved to 802.16e tone-demapping and deinterleaving.
- 3) **Parallel to serial de-multiplexing:** Bits on different spatial streams are de-multiplexed into a single stream of  $MN_{CBPS}$  bits.
- 4) **FEC decoding:** The soft coded bits are decoded with the 802.16e depuncturer and convolutional decoder.

## 3 Sample outputs of SISO and MIMO interleavers

### 3.1 SISO interleaver

The mapping of uncoded bits to OFDM tones on a single antenna is shown in Figure 2. The input is uncoded bits and the output is QAM symbols mapped to tones in the assigned subchannels. After all tones in the FFT block have been filled up with symbols, the frequency domain signal is converted to the time domain via the inverse Fast Fourier Transform (I-FFT), prefixed with the cyclic prefix, upconverted to the carrier frequency and launched over the transmit antenna.

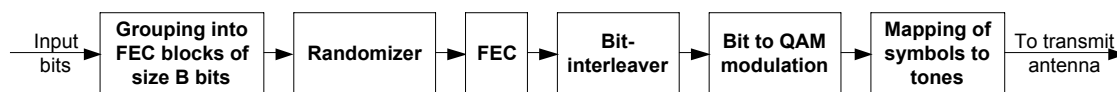


Figure 2: IEEE 802.16e mapping of uncoded bits to OFDM tones on a single antenna

The bit to tone mapping consists of the following steps

- 1) Grouping of bits into blocks of size B, where  $B = 6, 12, 24, \dots, 48$  bytes depending on the QAM size.
- 2) Scrambling of bits in one block
- 3) FEC coding of bits in one block (convolutional coding followed by puncturing)
- 4) Bit interleaving of bits in one block
- 5) Mapping of interleaved bits to QAM symbols
- 6) Mapping of QAM symbols to tones in the assigned subchannel

Here step 4 distributes the adjacent coded bits across tones so as to provide frequency diversity. In general, adjacent bits in a convolutionally coded sequence must be placed on tones separated by at least one coherence bandwidth in order to extract full frequency diversity in a frequency selective channel. A regular spacing of adjacent bits across tones is sufficient. For example, 48 coded inputs bits indexed as 1, 2, 3, ..., 48 are mapped to 48 tones for BPSK modulation in 802.11a as shown below.

**Example A: 802.11a OFDM PHY : data tones=48, interleaving depth=3, BPSK modulation**

1 BITS per BPSK symbol, mapped to tones 1:48

<u>1</u>	17	33	<u>2</u>	18	34	<u>3</u>	19	35	<u>4</u>	20	36	5	21	37	6	22	38	7
23	39	8	24	40	9	25	41	10	26	42	11	27	43	12	28	44	13	29
45	14	30	46	15	31	47	16	32	48									

Here adjacent bits  $i$  and  $j$  are separated by at least 3 tones for all  $i$ . This regular spacing extracts most of the maximum possible frequency diversity corresponding to delay spreads equal to the cyclic prefix (equal to 16 time samples, for a 64-point FFT, sample time = 50 ns).

Although regular spacing of bits maximizes the performance of a point-to-point OFDM link, it may not be robust in the presence of co-channel interference in a multi-cellular OFDMA system like 802.16e. If one of the OFDMA users is assigned a regularly spaced subset of tones, it may suffer high interference from an extra-cellular user assigned the same set of tones. In order to provide robustness against interference, step 6 assigns adjacent bits to irregularly spaced tones spread throughout the spectrum. An example is shown below for 1 FEC block of 96 bits which is mapped to rate  $\frac{1}{2}$  QPSK symbols on 1 FUSC sub-channel consisting of 48 tones in an FFT size of 512 tones.

**Example B: 802.16e FUSC DL: 1 sub-channel, 1 FEC block, 48 data tones, rate  $\frac{1}{2}$  QPSK**

2 BITS per QPSK symbol

<u>1</u>	33	65	<u>2</u>	34	66	<u>3</u>	35	67	<u>4</u>	36	68	5	37
17	49	81	18	50	82	19	51	83	20	52	84	21	53
Columns 15 through 28													
69	6	38	70	7	39	71	8	40	72	9	41	73	10
85	22	54	86	23	55	87	24	56	88	25	57	89	26
Columns 29 through 42													
42	74	11	43	75	12	44	76	13	45	77	14	46	78
58	90	27	59	91	28	60	92	29	61	93	30	62	94
Columns 43 through 48													
15	47	79	16	48	80								
31	63	95	32	64	96								

Columns of BITS above are mapped to the following TONES

Columns 1 through 14													
46	60	64	75	84	97	103	107	117	131	135	146	154	167
Columns 15 through 28													
173	177	186	201	205	216	223	237	243	246	256	271	276	287
Columns 29 through 42													
294	309	315	318	328	342	347	358	365	379	387	390	401	415
Columns 43 through 48													
420	431	438	451	458	461								

The separation between adjacent tones above is irregular.

### 3.2 Proposed MIMO interleaver

The proposed modifications to the existing 802.16e bit-to-tone mapping are steps 1, 2 and 4 as circled in red below.

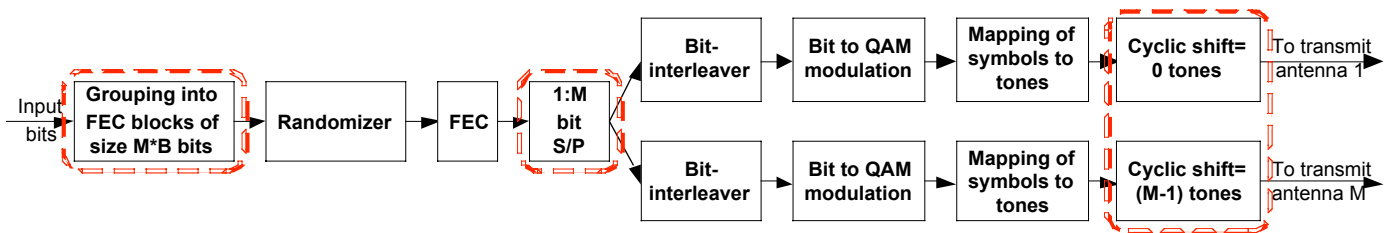


Figure 3: Proposed SF-BICM mapping of bits to multiple antennas (or spatial streams)

- 1) **FEC encoding:** Group the incoming uncoded bits into blocks of size  $MB$ , such that the coded output blocks are of size  $MN_{CBPS}$ . It is important to create larger FEC blocks to preserve frequency diversity

going from SISO to MIMO systems. If the FEC block size were held constant and  $N_{CBPS}$  bits were mapped to  $1/M$  of the SISO tones on  $M$  antennas, spreading across fewer tones on each antenna will not provide full frequency diversity.

- 2) **Serial to parallel antenna multiplexing:** Coded bits are serial to parallel multiplexed to different antennas. The bits indexed by  $m:M:MN_{CBPS}$  are mapped to the  $m^{th}$  antenna.
- 3) **802.16e interleaving, modulation and tone mapping:** The resulting groups of  $N_{CBPS}$  bits on each antenna are interleaved according to the 802.16e interleaver and Gray mapped to QAM symbols. The resulting QAM symbols are mapped to tones in the assigned 802.16e sub-channels.
- 4) **Cyclic tone shift:** The final step consists of introducing a cyclic shift of  $m-1$  tones to the symbol sequence mapped to the  $m^{th}$  antenna. This ensures that adjacent coded bits aren't mapped to the same tone on different antennas. If adjacent coded bits get mapped to the same tone on different antennas, an MMSE receiver correlates the noise on all these bits thus degrading performance. Placing adjacent coded bits on different tones on different antennas de-correlates noise on adjacent bits, thus improving performance and providing greater spatial diversity.

#### Remarks

- a) Note that the amount of cyclic shift may be greater than 1 tone from antenna to antenna, although a shift of 1 works well in most cases. In general, the optimum cyclic shift must be determined by simulation for different rates and MIMO configurations. The maximum cyclic shift is equal to  $N_{DS}/M$ , where  $N_{DS}$  = number of data tones that 1 FEC block is mapped to.
- b) Step 2 in the interleaver design provides spatial diversity with ML/MAP receivers, steps 1 and 3 provide frequency diversity, and step 4 provides spatial diversity with linear receivers that induce correlation among tones and antennas (e.g. MMSE).
- c) This interleaver applies to spatial streams with ABL (adaptive bit loading) as well. Bits are multiplexed as per step 2 in the interleaver. As the lower modulation order symbols fill up, remaining bits are placed on higher modulation symbols.

An example of SF-BICM with a cyclic shift of 1 tone is provided below.

**Example C: Proposed SF-BICM for 2 transmit antennas on 802.16e FUSC DL: 1 sub-channel, 1 FEC block, 48 data tones, rate \_ QPSK**

#### 2 BITS per QPSK symbol mapped to transmit antenna #1

Columns 1 through 14													
<u>1</u>	65	129	<u>3</u>	67	131	5	69	133	7	71	135	9	73
33	97	161	35	99	163	37	101	165	39	103	167	41	105
Columns 15 through 28													
137	11	75	139	13	77	141	15	79	143	17	81	145	19
169	43	107	171	45	109	173	47	111	175	49	113	177	51
Columns 29 through 42													
83	147	21	85	149	23	87	151	25	89	153	27	91	155
115	179	53	117	181	55	119	183	57	121	185	59	123	187
Columns 43 through 48													
29	93	157	31	95	159								
61	125	189	63	127	191								

→  
Shift of 1 tone from antenna 1 to 2

#### 2 BITS per QPSK symbol mapped to transmit antenna #2

Columns 1 through 14													
160	<u>2</u>	66	130	<u>4</u>	68	132	6	70	134	8	72	136	10
192	34	98	162	36	100	164	38	102	166	40	104	168	42
Columns 15 through 28													
74	138	12	76	140	14	78	142	16	80	144	18	82	146
106	170	44	108	172	46	110	174	48	112	176	50	114	178
Columns 29 through 42													
20	84	148	22	86	150	24	88	152	26	90	154	28	92
52	116	180	54	118	182	56	120	184	58	122	186	60	124
Columns 43 through 48													
156	30	94	158	32	96								
188	62	126	190	64	128								

Columns of BITS on both antennas above are mapped to the following TONES (same as SISO)

Columns 1 through 14	46	60	64	75	84	97	103	107	117	131	135	146	154	167
Columns 15 through 28	173	177	186	201	205	216	223	237	243	246	256	271	276	287
Columns 29 through 42	294	309	315	318	328	342	347	358	365	379	387	390	401	415
Columns 43 through 48	420	431	438	451	458	461								

### 4 Simulation Results

This section demonstrates performance of the proposed SF-BICM over 2x2 MIMO systems in PUSC mode with 1024-point FFT. The 2x2 MIMO architecture transmits 2 spatial streams, one on each transmit antenna, and uses an MMSE receiver to recover them. Performance is tested on ITU pedestrian channel model A with a low rms delay spread of 45 ns, and the Pedestrian model B with a high rms delay spread of 750 ns, at a Doppler spread corresponding 3 km/h. The frequency selective channels on each transmit-receive antenna pair are i.i.d. Packet error rate is computed for 200 byte packets. Two data rates are considered: rate\_QPSK and rate\_16-QAM. We assume perfect channel estimation, phase and carrier tracking and symbol synchronization, and floating point precision.

Performance of three schemes is shown in Figure 6: (1) the proposed SF-BICM labeled “-h Bit Intlv”, (2) simple spatial multiplexing labeled “x-No Intlv” and illustrated in Figure 4, and (3) a simpler symbol interleaver labeled “-0-Sym Intlv” and illustrated in Figure 5.

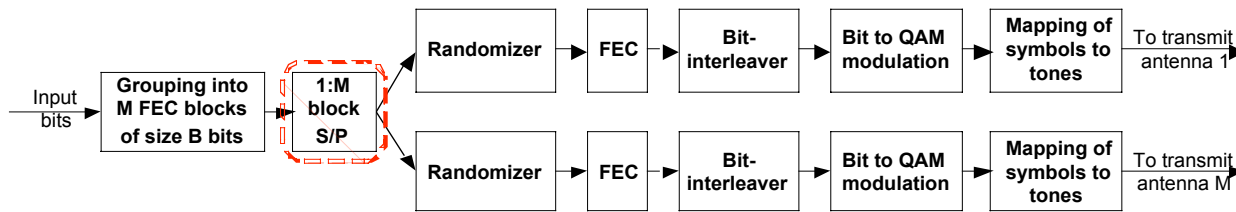


Figure 4: Simple spatial multiplexing of FEC blocks on multiple antennas

The block interleaver takes consecutive blocks of B bits and multiplexes them to different antennas. Therefore bits on different transmit antennas are independent. On each antenna, 802.16e interleaving is followed. This method (F-BICM) is expected to provide frequency diversity but no spatial diversity.

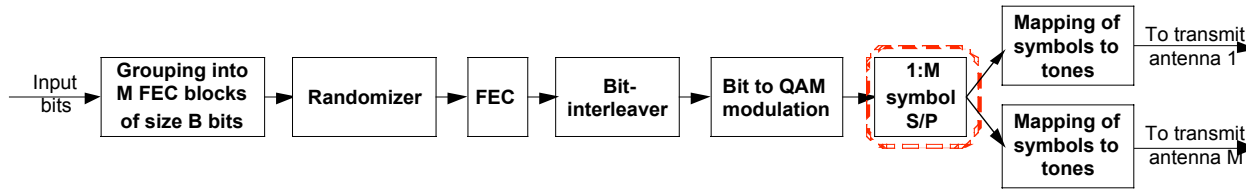


Figure 5: Symbol interleaving on multiple antennas

The symbol interleaver multiplexes consecutive coded QAM symbols on different antennas. This method is expected to provide some frequency diversity and some spatial diversity.

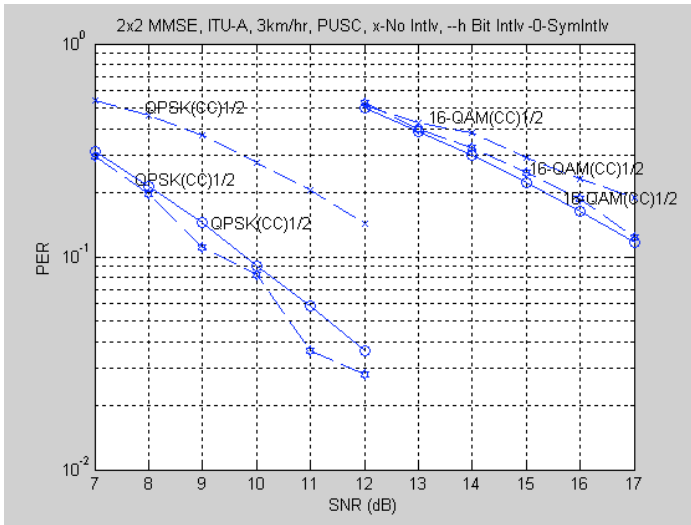


Figure 6(a): SF-BICM vs BICM over low delay spread

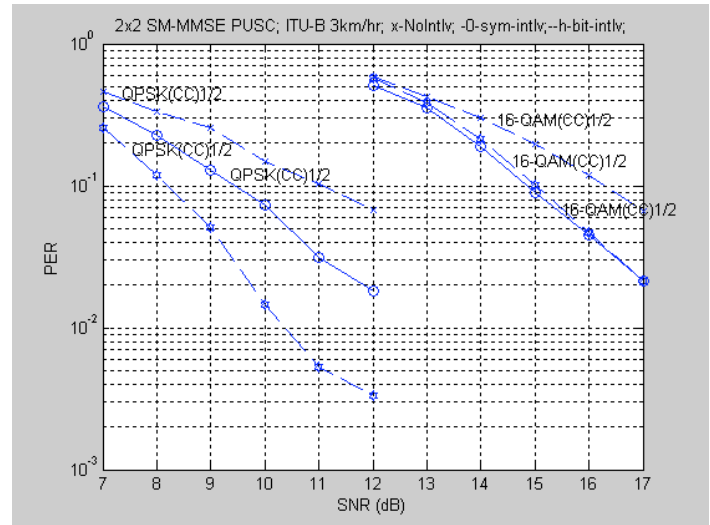


Figure 6(b): SF-BICM vs BICM over high delay spread

In Figures 6(a) and 6(b), the slopes of MIMO+SFI are sharper than those of MIMO+SM, suggesting better diversity. Performance of symbol interleaving lies in between SF-BICM and F-BICM. With higher frequency diversity in 6(b), SF-BICM outperforms F-BICM by 3 db at PER 10%. SF-BICM provides a higher gain for lower data rates, extending the connectivity and cell range. The MMSE receiver induces correlation across antennas because of cross-talk, and the channel induces correlation across tones because of limited delay spread. Together these two factors induce correlation among adjacent tones on all antennas. Our proposed interleaver places bits on uncorrelated tones and antennas as much as possible, thereby improving performance with the MMSE receiver.

## Acknowledgments

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