



**IKN**  
Institut für  
Kommunikationsnetze

# Fairness Benchmarking of MACs

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# Goal and Content

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**Goal:** Finding an algorithm to determine the maximal individual node throughputs and at the same time fulfilling bottleneck-link fairness

**Content:**

- Two definitions for bottleneck fairness
- Corresponding fairness algorithms and examples
- Two traffic scenarios

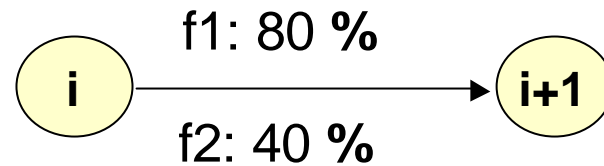
# Local Fairness Definitions

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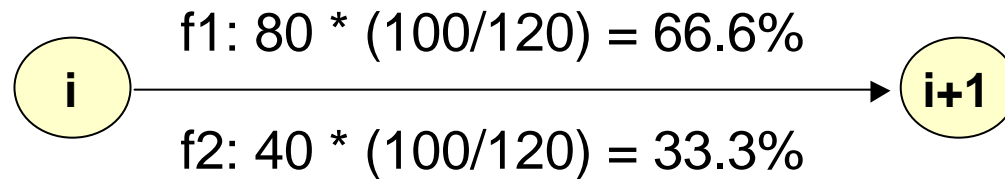
- ① Flow rates on bottleneck are proportionally reduced by the total amount of offered traffic for that bottleneck link
  
- ② Flow rates on bottleneck are proportionally reduced by the total number of connections on bottleneck link

# Example

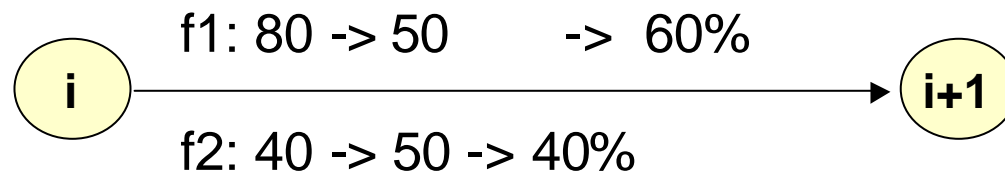
- 2 flows, 1 link:



- Definition 1:



- Definition 2:



# Definitions

## Given:

- Number of nodes  $N$
- Requested rate from node  $i$  to node  $j$   $r_{i,j}$

## Calculated:

- Flow on link  $i$   $f_i$   
Sum of all requested rates passing link  $i$
- Number of demand flows passing link  $i$   $nd_i$
- Remaining capacity on link  $i$   $rc_i$   
Link capacity minus the sum of all allowed rates passing link  $i$
- Allowed rate from node  $i$  to node  $j$   $ar_{i,j}$   
Rate calculated by the algorithms

# Algorithm for Fairness Definition 1

**Set:**  $rc_i = 1;$  // init remaining capacity

**Step 1:** for all links: calculate flow on link  $i$ :  $f_i$

**Step 2:** if (  $rc_i < f_i$  ) // condition for a bottleneck  
take always the highest overloaded bottleneck:  $\min(rc_i/f_i)$   
bottleneck link: indicated by index  $b$   
else  $ar_{i,j} = ar_{i,j} + r_{i,j}$ ; stop;

**Step 3:** for all flows passing this bottleneck set:  $ar_{i,j} = rc_b/f_b \times r_{i,j}$  and  $r_{i,j} = 0$

**Step 4:** calculate remaining capacities  $rc_i$  of all links; goto **Step 1**;

# Algorithm for Fairness Definition 2

**Set:**  $rc_i=1;$

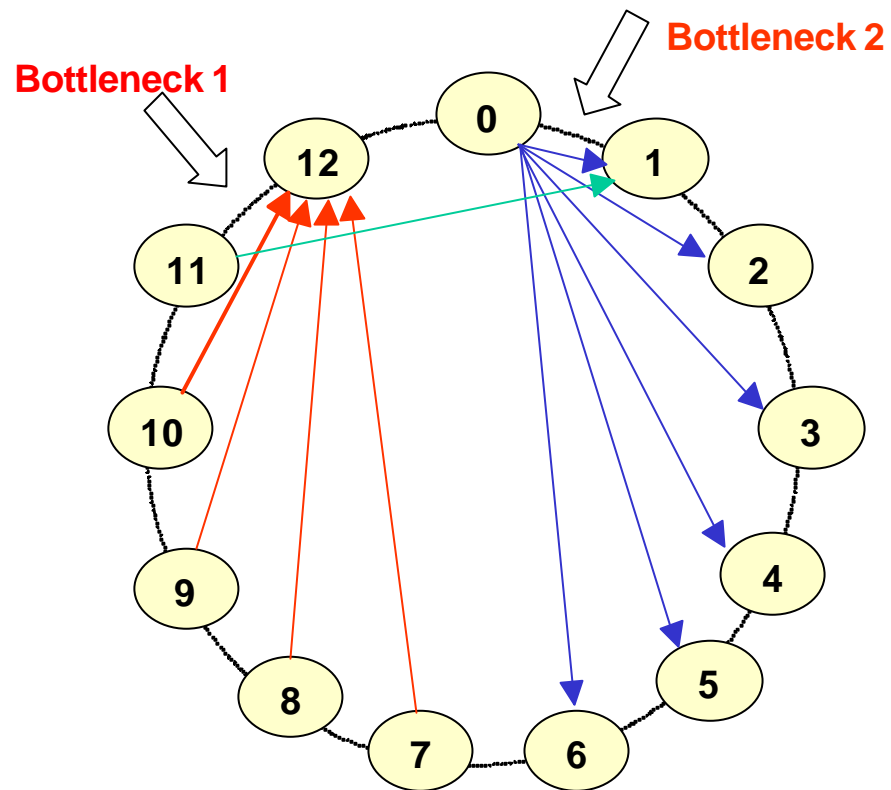
**Step 1:** for all links: calculate flow on link  $i$ :  $f_i$

**Step 2:** if (  $rc_i < f_i$  ) // condition for a bottleneck  
take always the highest overloaded bottleneck:  $\min(rc_i/nd_i)$   
bottleneck link: indicated by index  $b$   
else  $ar_{i,j} = ar_{i,j} + r_{i,j}$ ; stop;

**Step 3:** for all flows passing this bottleneck:  
if ( $rc_b/nd_b > r_{i,j}$ )  
 $ar_{i,j} = r_{i,j}$ ;  $nd_b = nd_b - 1$ ;  $r_{i,j} = 0$ ;  
calculate remaining capacities  $rc_i$  of all links;  
goto **Step 1**;  
else  $ar_{i,j} = rc_b/nd_b$ ;  $r_{i,j} = 0$ ;

**Step 4:** calculate remaining capacities  $rc_i$  of all links; goto **Step 1**;

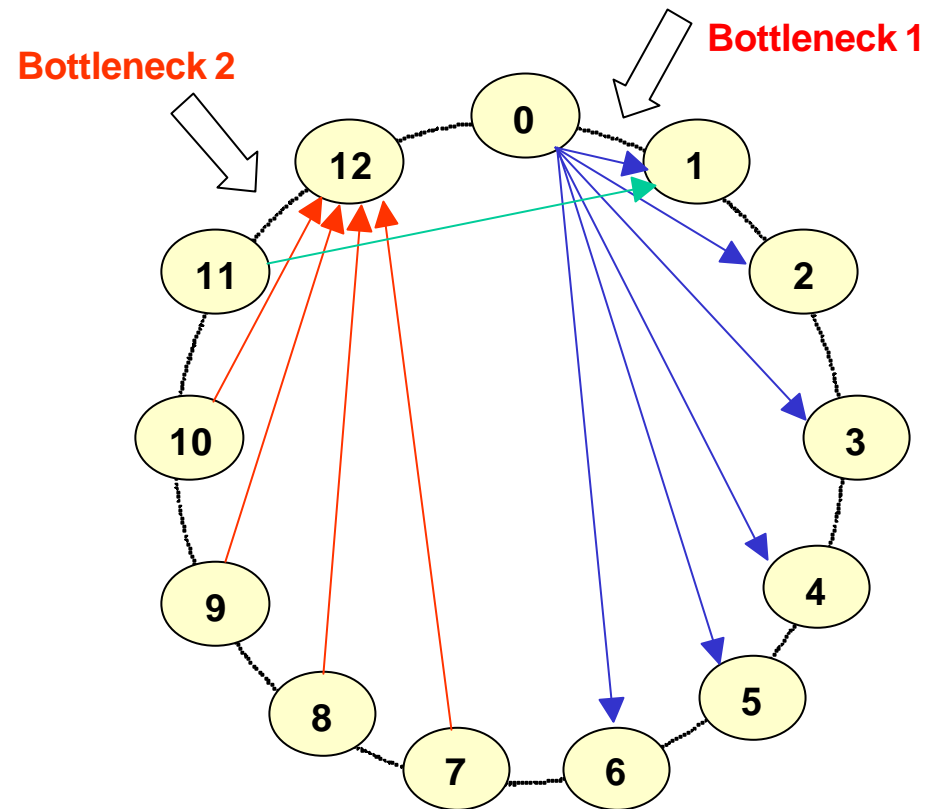
# Example: Fairness Definition 1



Source	Sink	Rate	Fair
0	1	0.01	0.01
0	2	0.01	0.01
0	3	0.01	0.01
0	4	0.01	0.01
0	5	0.01	0.01
0	6	0.01	0.01
7	12	0.1	0.071
8	12	0.1	0.071
9	12	0.1	0.071
10	12	0.1	0.071
11	1	1	0.71

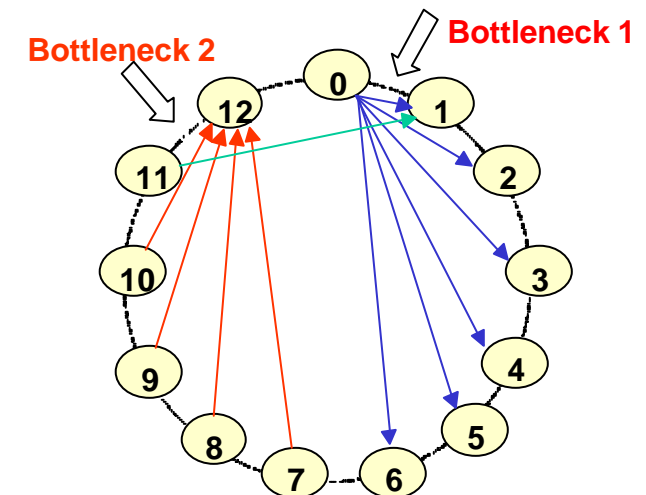
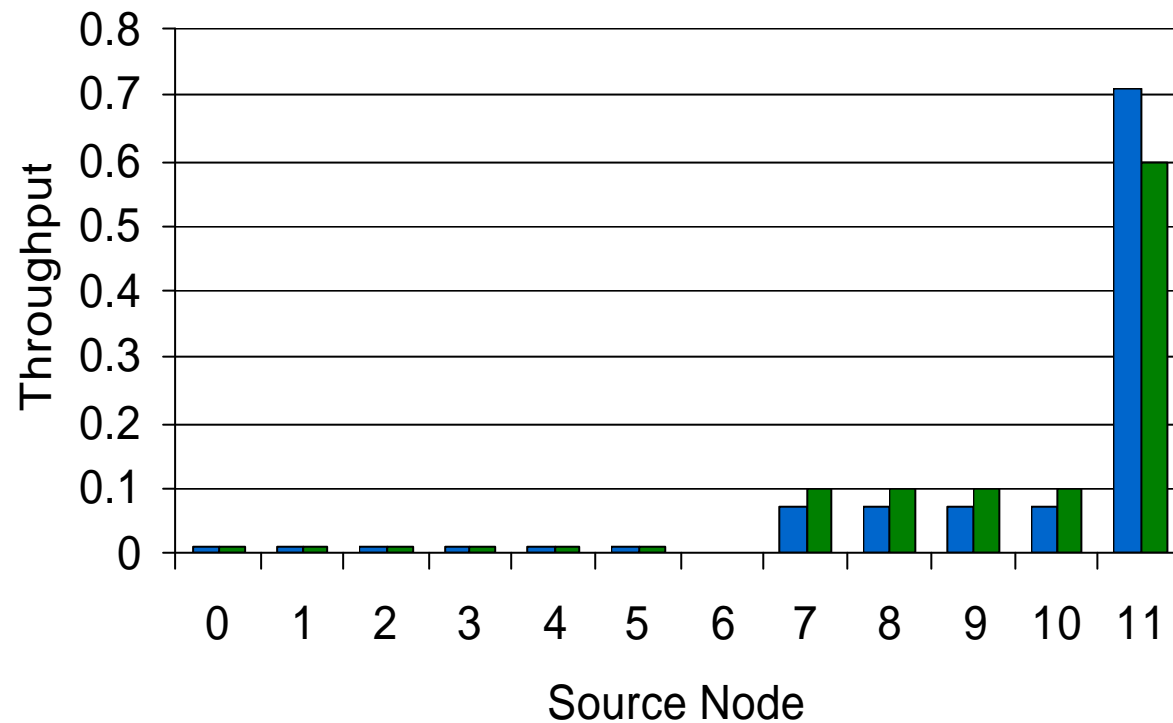


# Example: Fairness Definition 2

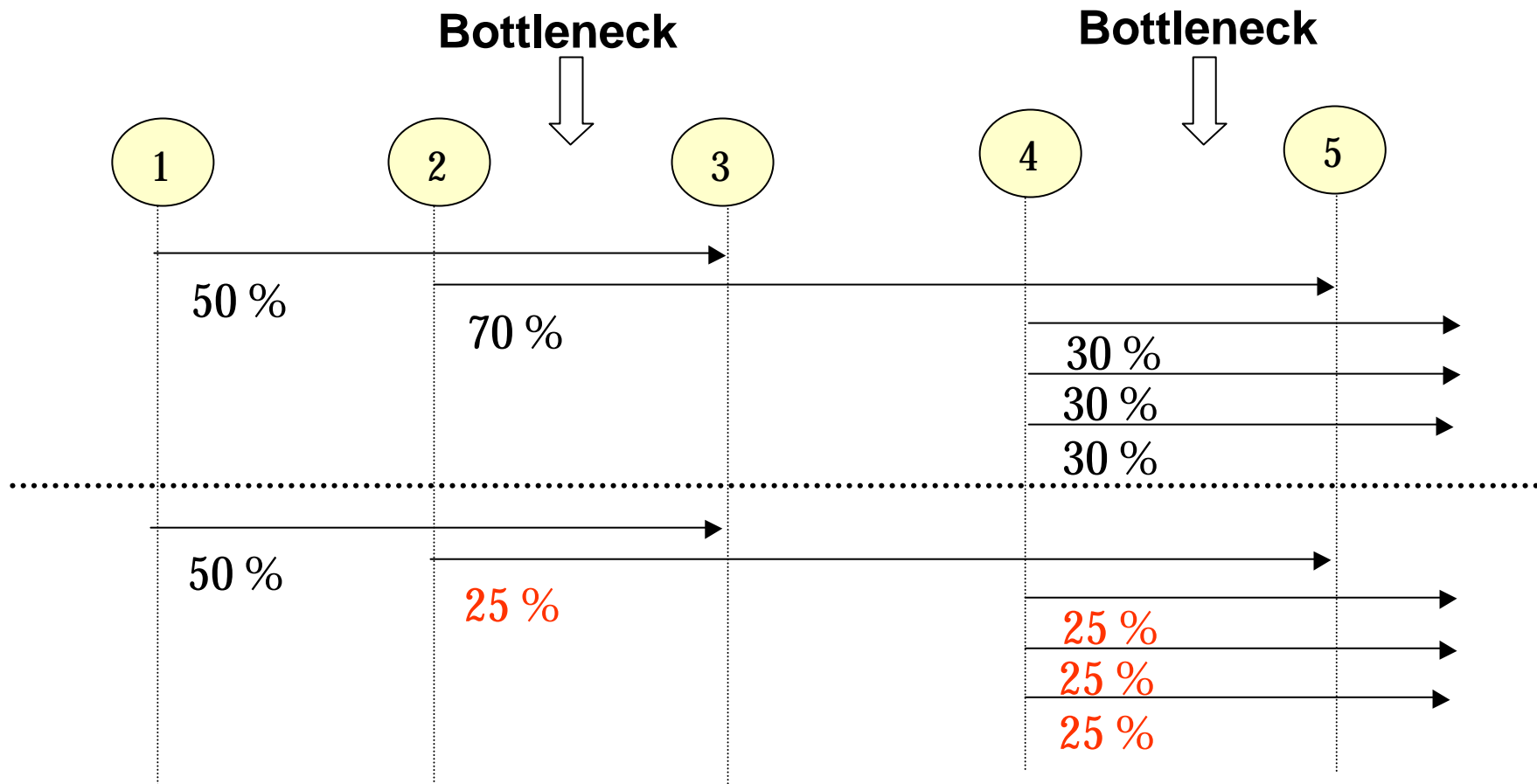


Source	Sink	Rate	Fair
0	1	0.01	0.01
0	2	0.01	0.01
0	3	0.01	0.01
0	4	0.01	0.01
0	5	0.01	0.01
0	6	0.01	0.01
7	12	0.1	0.1
8	12	0.1	0.1
9	12	0.1	0.1
10	12	0.1	0.1
11	1	1	0.6

# Throughput

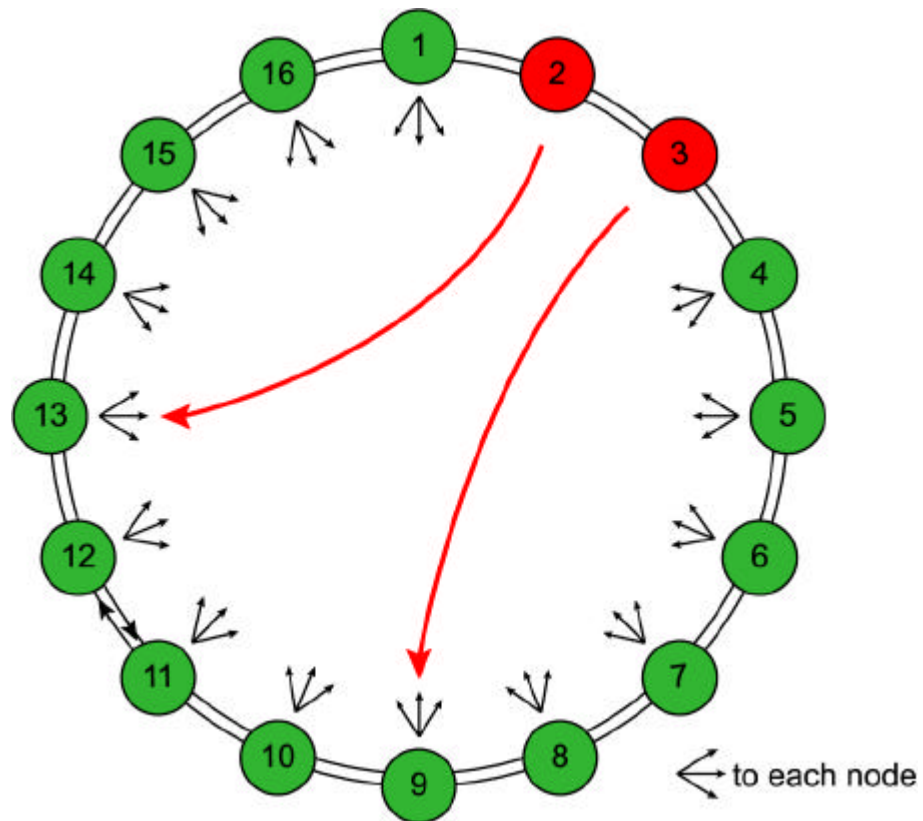


# Example: Fairness Definition 2



Some bottlenecks can be resolved by resolving other bottlenecks

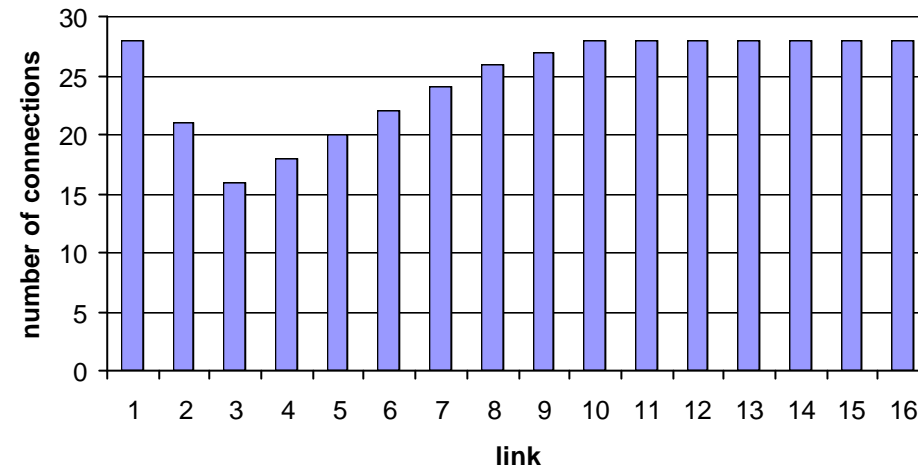
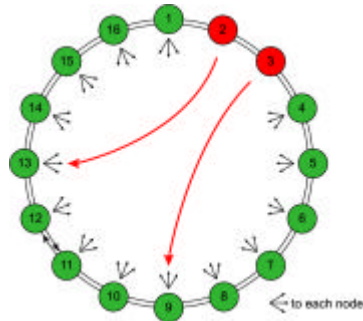
# Scenario 1



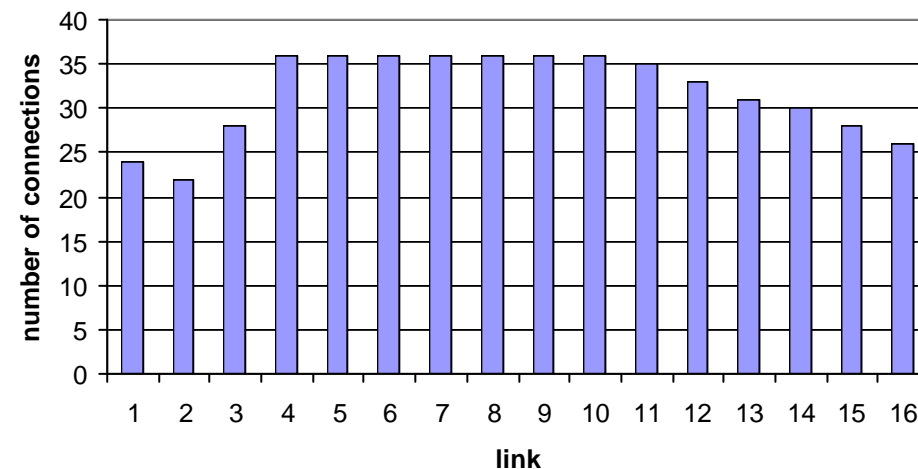
**Uniform traffic**  
**Saturated sources**  
**16 nodes**

# Number of Connections per Bottleneck Link

## Scenario 1



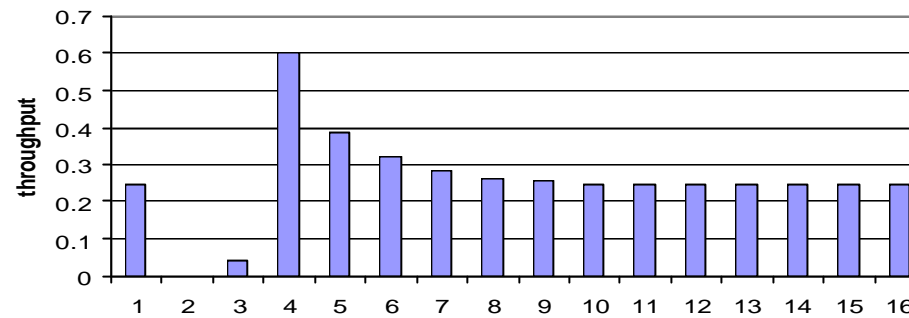
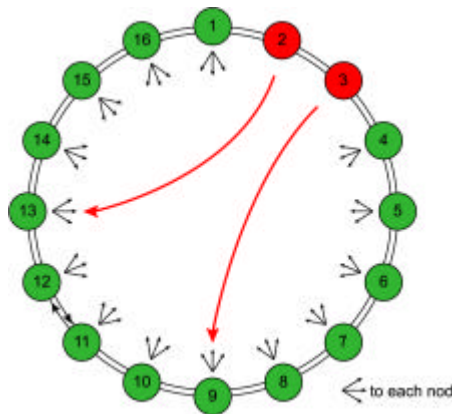
Ring 0



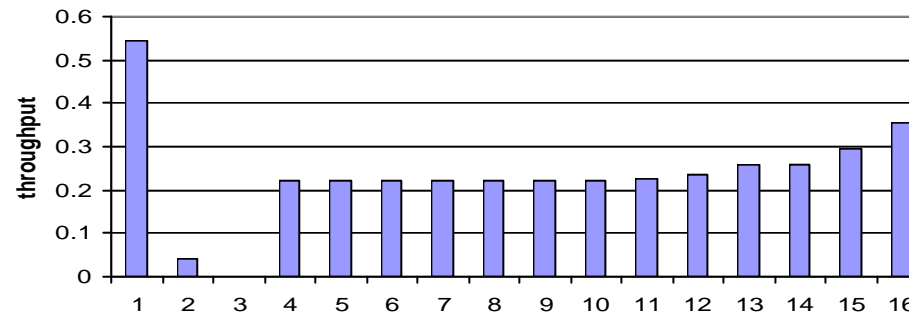
Ring 1

# Throughput per Node

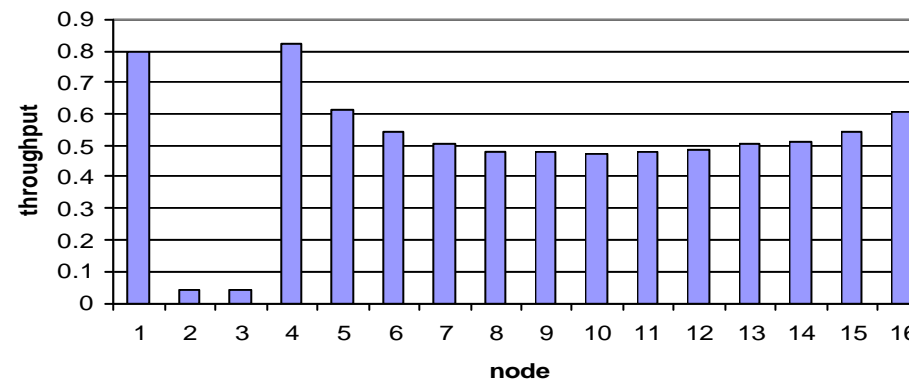
## Scenario 1



Ring 0



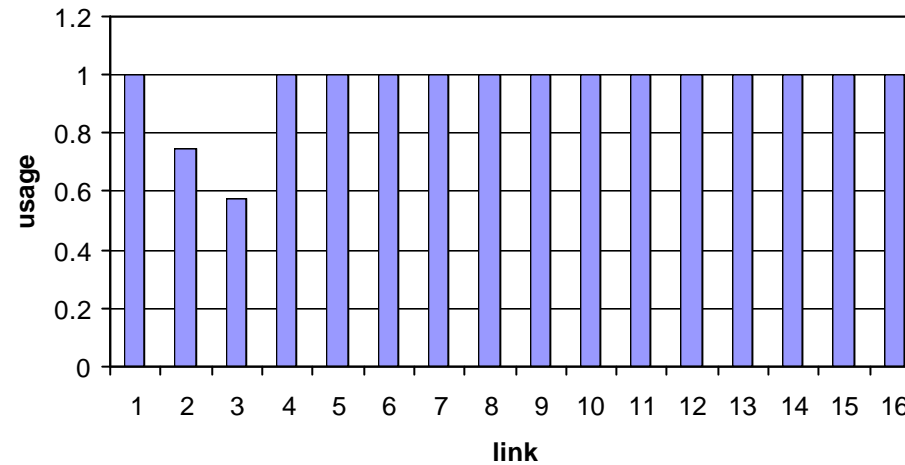
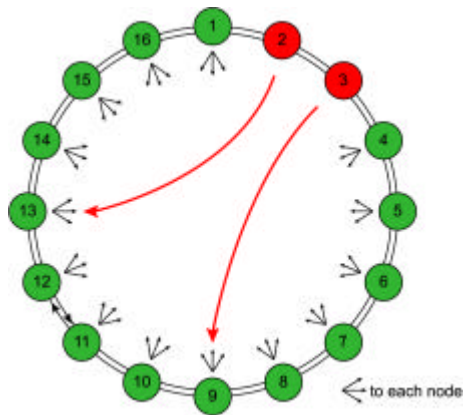
Ring 1



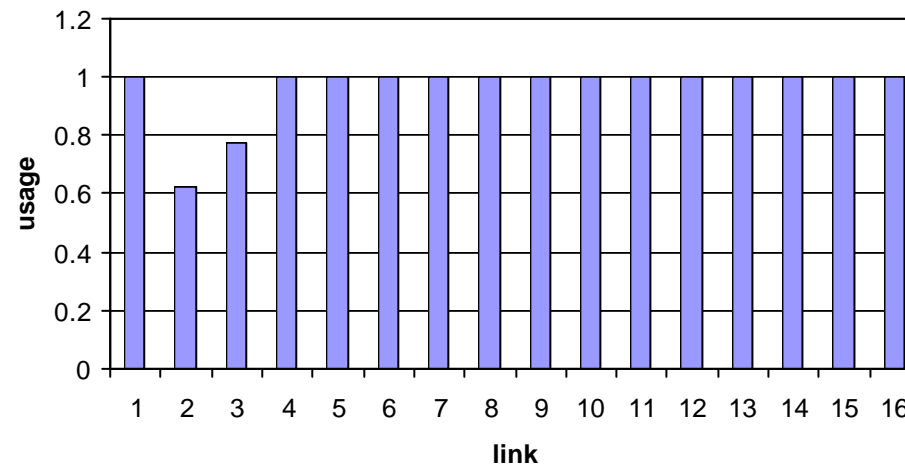
Ring 0 +  
Ring 1

# Link Usage

## Scenario 1



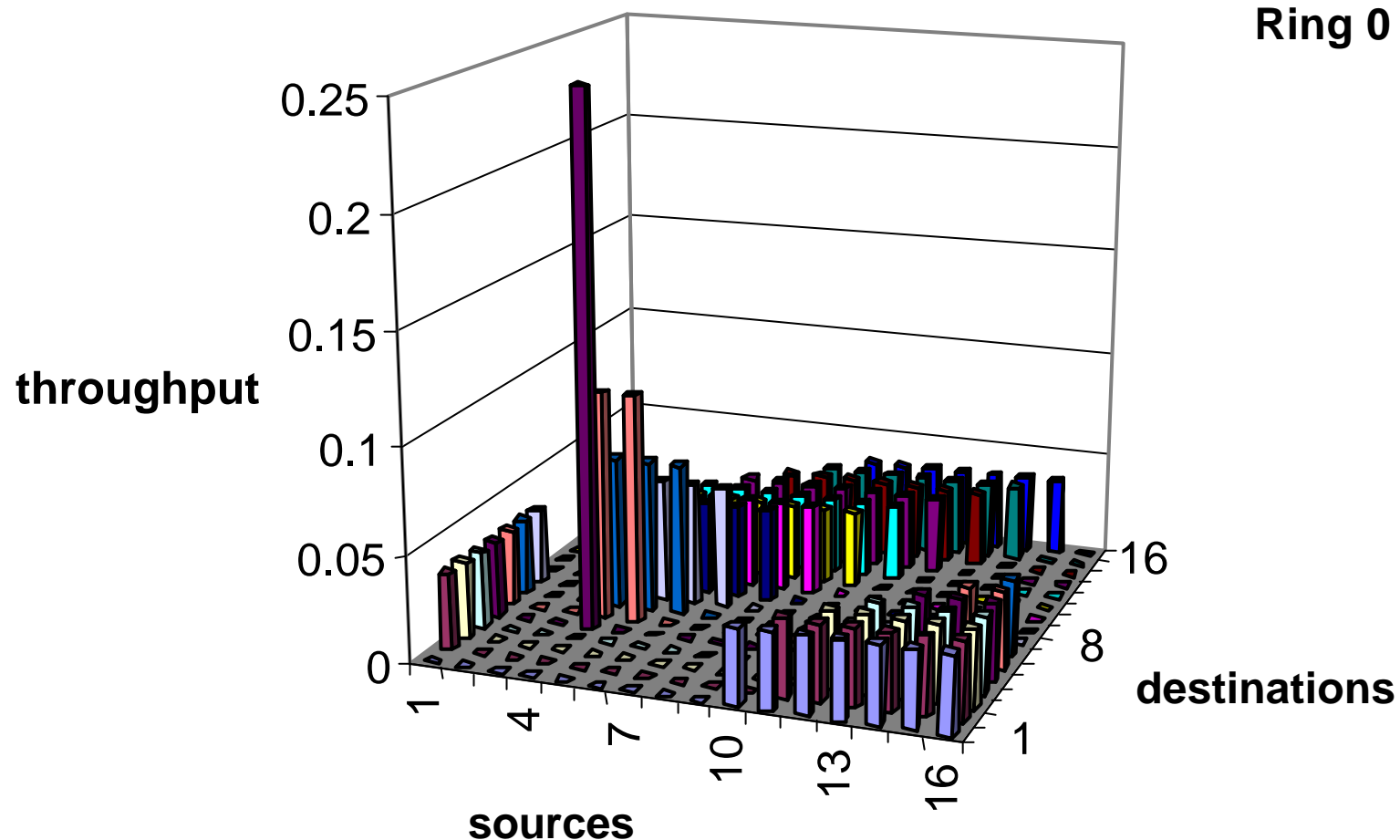
Ring 0



Ring 1

# Throughput per Source/Destination Pair

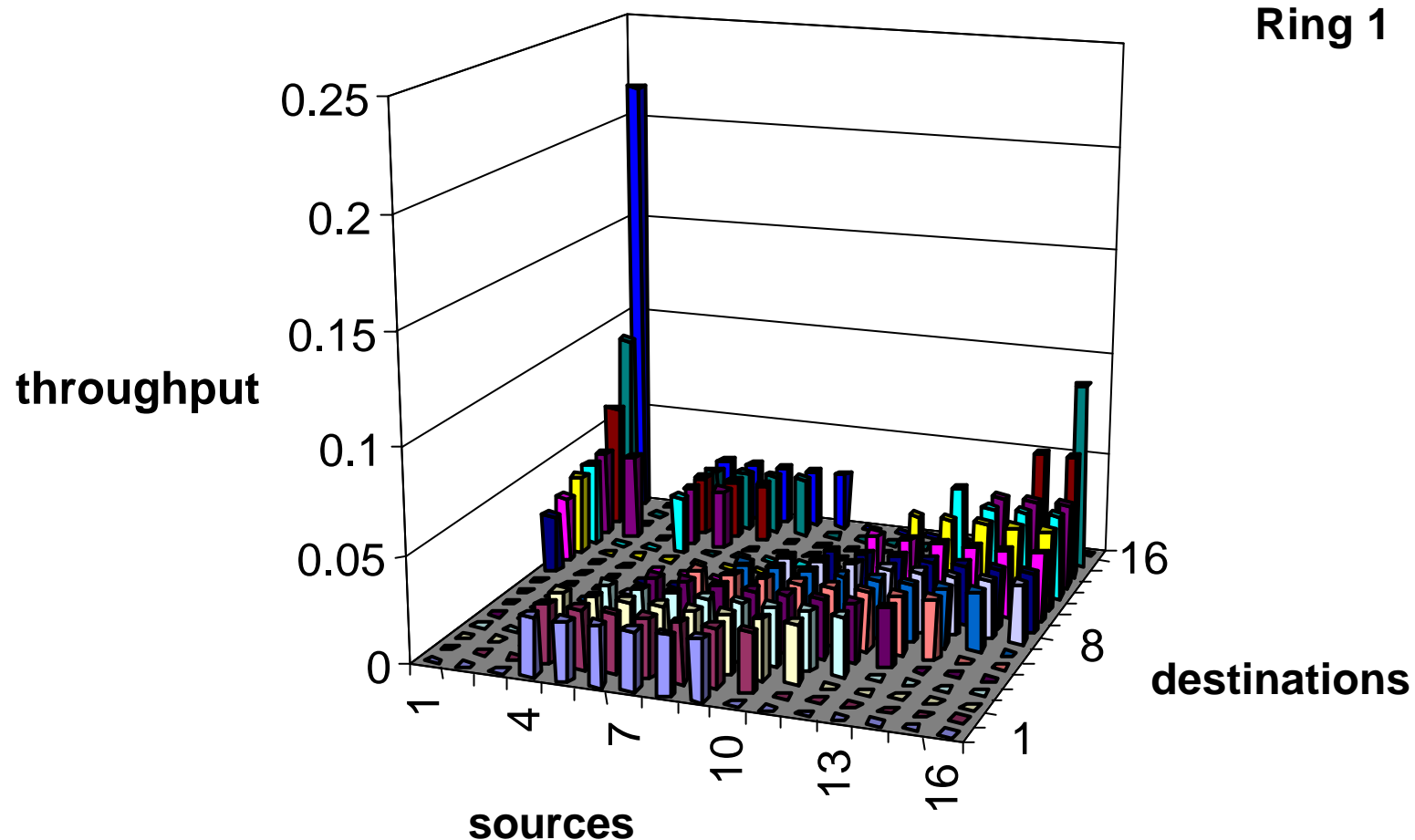
## Scenario 1



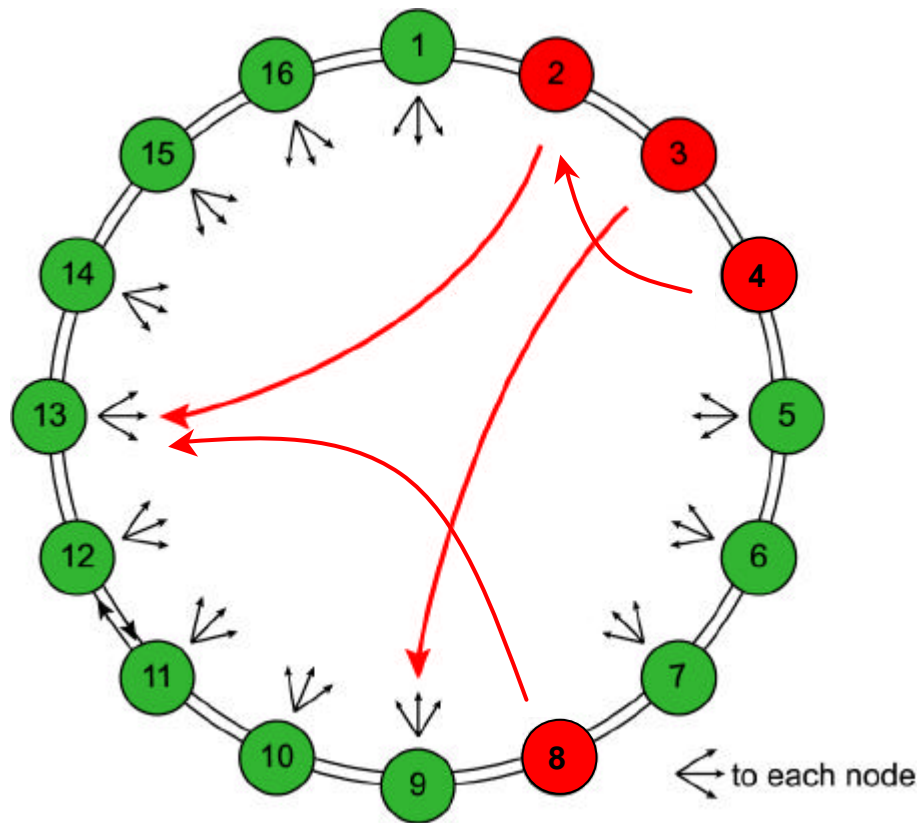


# Throughput per Source/Destination Pair

## Scenario 1



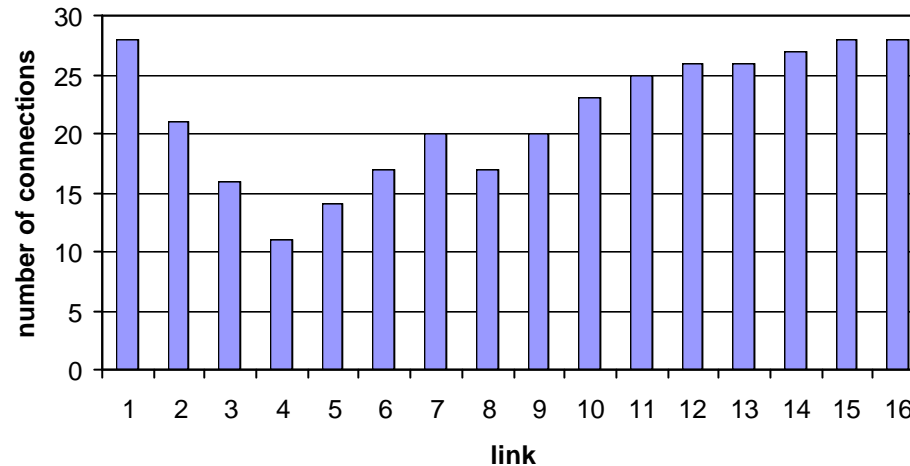
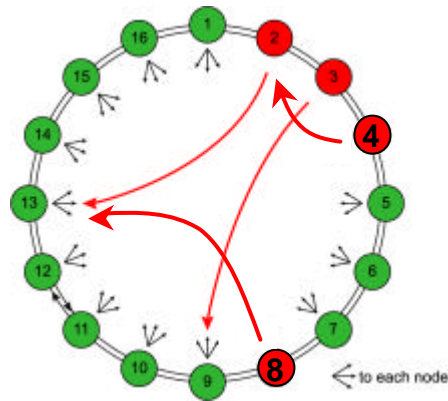
# Scenario 2



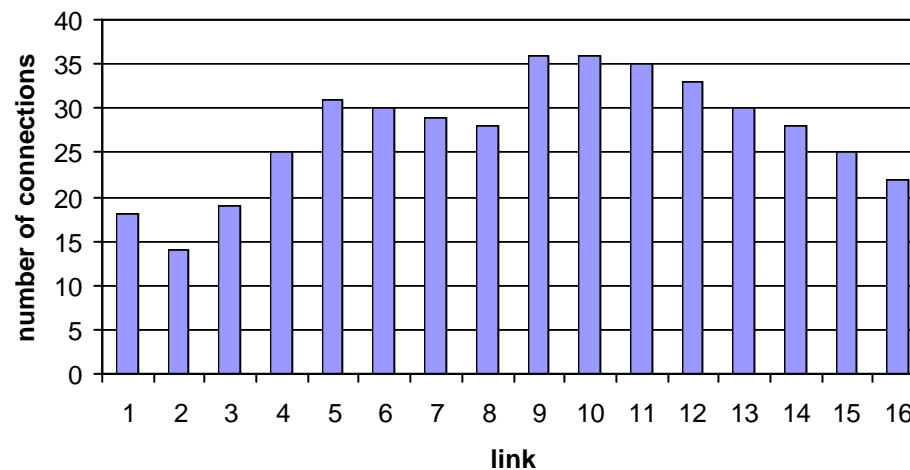
Uniform traffic  
Saturated sources  
16 nodes

# Number of Connections per Bottleneck Link

## Scenario 2



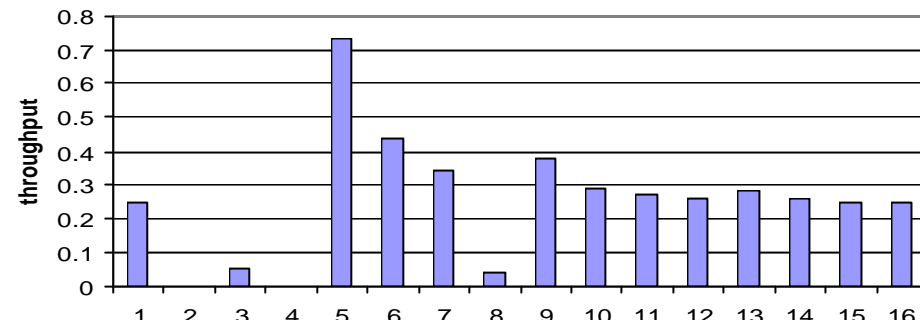
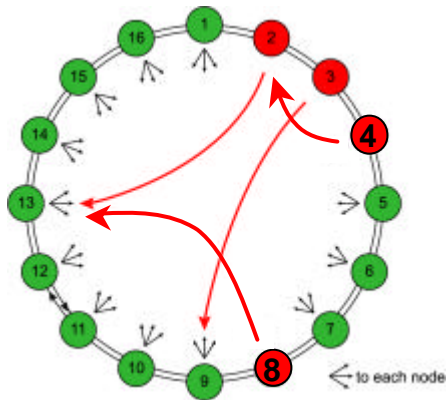
Ring 0



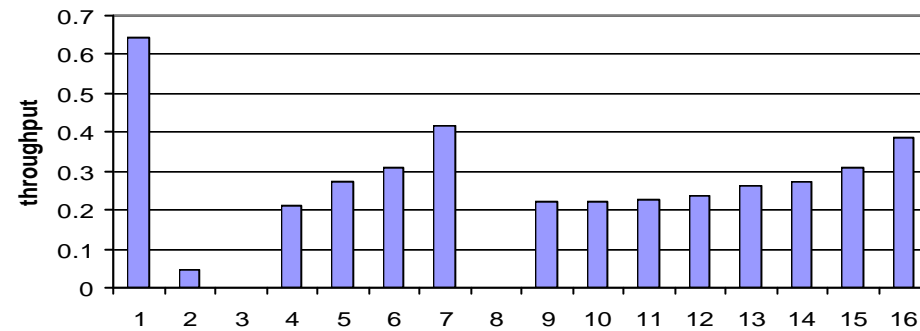
Ring 1

# Throughput per Node

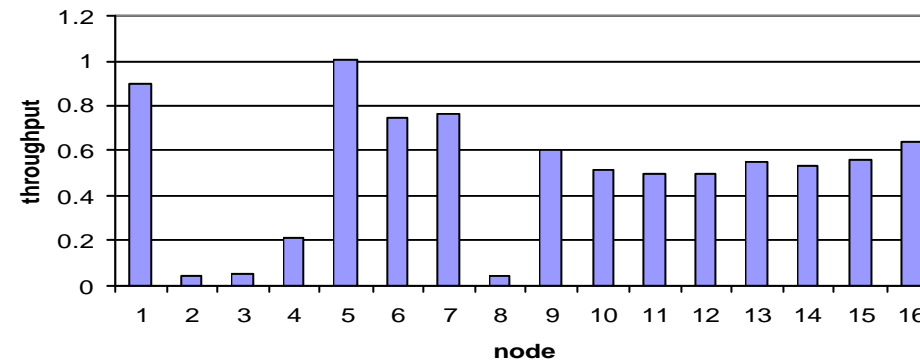
## Scenario 2



Ring 0



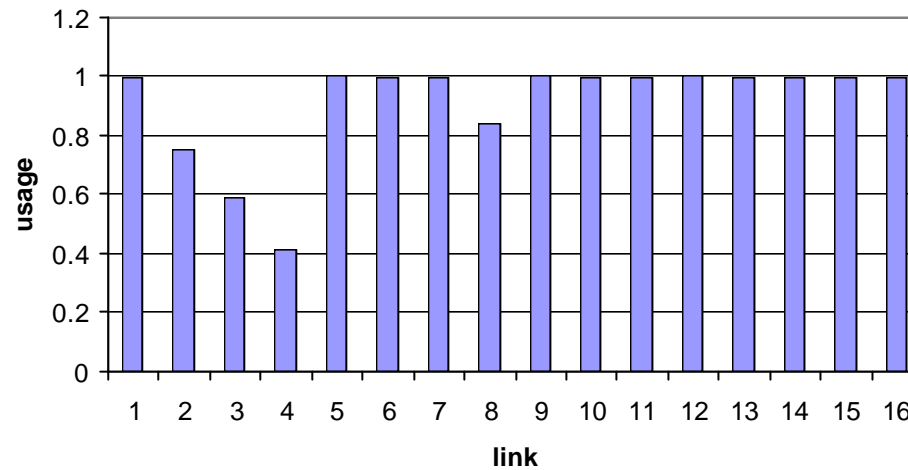
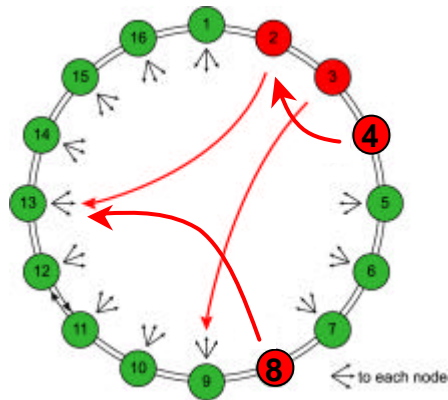
Ring 1



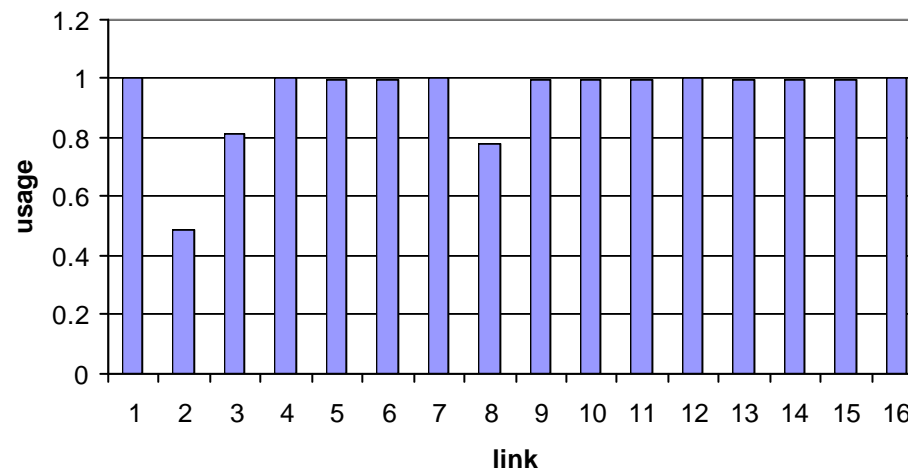
Ring 0 +  
Ring 1

# Link Usage

## Scenario 2



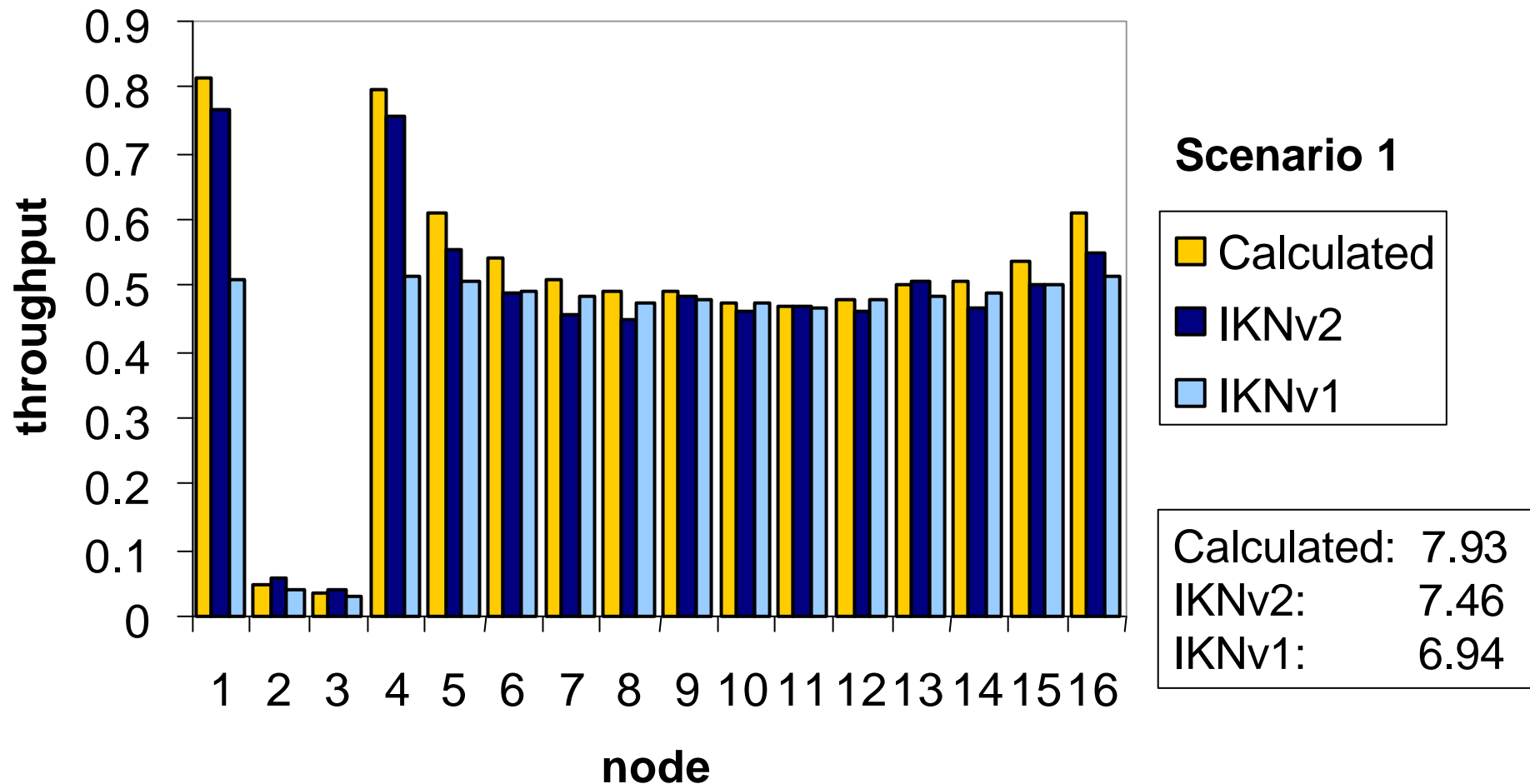
Ring 0



Ring 1

# Throughput Comparison

Cyclic Reservation MAC : IKNv1 (July 2001)  
IKNv2 (Jan. 2002)



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# Conclusion

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- Two algorithms for solving the bottleneck problem have been shown
- The result is the optimum solution to this problem
- Both algorithms scale well
- Thus, both can be used to determine the fair bottleneck rates
  - Theoretical benchmarking
  - On-line scheduling