

Voltage Transfer Function¹

¹ “Introduction to Frequency Domain Analysis (3 Classes)” Slide 46 ff, Signal Integrity ELECT865 @ University of South Carolina
<http://www.ee.sc.edu/classes/Spring04/elct865/images/Class7-8-9.ppt>



Voltage Transfer Function

- ✓ What is really of most relevance to time domain analysis is the voltage transfer function.
- ✓ It includes the effect of non-perfect loads.
- ✓ We will show how the voltage transfer functions for a 2 port network is given by the following equation.

$$\frac{s_{21}}{2} \cdot (\Gamma_L + 1) \cdot (1 - \Gamma_s)$$

$$1 - s_{11} \cdot \Gamma_s - s_{22} \cdot \Gamma_L - s_{21} \cdot s_{12} \cdot \Gamma_L \cdot \Gamma_s + s_{11} \cdot s_{22} \cdot \Gamma_L \cdot \Gamma_s$$

- ✓ Notice it is not s_{21}

Example on how to use the transfer function

3

Simple static example for transfer function impact from channel parameters

Richard Mellitz 9/29/04

Insertion and return channel loss in dB dB_loss := 25 ch_RL := 3

$$\begin{aligned} s21 &:= 10^{\frac{-\text{dB_loss}}{20}} & s11 &:= 10^{\frac{-\text{ch_RL}}{20}} & \Gamma_s &:= 0 \\ s12 &:= s21 & s22 &:= s11 \end{aligned}$$

Gamma s is the source reflection coef.
Gamma L is the load reflection coef

Use 1/2 source voltage at source resistor instead of at source node

$$\frac{s21 \cdot (\Gamma_L + 1) \cdot (1 - \Gamma_s)}{1 - s11 \cdot \Gamma_s - s22 \cdot \Gamma_L - s21 \cdot s12 \cdot \Gamma_L \cdot \Gamma_s + s11 \cdot s22 \cdot \Gamma_L \cdot \Gamma_s} \quad \text{simplifies to-->} \quad \frac{s21 \cdot (\Gamma_L + 1)}{1 - s22 \cdot \Gamma_L}$$

$$\text{dB_RL} := 10 \quad \Gamma_L := -10 \quad 20 \log \left[\frac{s21 \cdot (\Gamma_L + 1)}{1 - s22 \cdot \Gamma_L} \right] = -30.056$$

$$\text{dB_RL} := 12 \quad \Gamma_L := -10 \quad 20 \log \left[\frac{s21 \cdot (\Gamma_L + 1)}{1 - s22 \cdot \Gamma_L} \right] = -28.934$$

10 dB of RL lowers the transfer function by 5 dB
12 dB of RL lowers the transfer function by 3.9 dB

Complete analysis requires complex and frequency dependant parameters