

A photograph of a surfer riding a large, curling wave. The wave is a deep green color and is breaking over the surfer, creating a tunnel effect. The surfer is in silhouette, wearing a wetsuit, and is riding the wave. The sky is a pale blue, and the water is a deep blue. The overall scene is dynamic and energetic.

RS Options for 40GBASE-T

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RS Overview

- Reed-Solomon is a block based error control code, built using Galois field elements
- Galois fields can be constructed from powers of prime numbers
 - Obviously 2^N is a very popular choice, which leads to a maximum block size of $2^N - 1$ symbols
 - Example: 2^8 gives a maximum block size of 255 bytes
- General format is M data symbols + 2T check symbols (a systematic code = payload is directly mapped)

RS Overview (continued)

- For RS codes, the $2T$ check symbols can locate and correct T errored symbols, and detect the presence of $2T$ errored symbols
 - Simple way to look at this limitation is that for each errored symbol, we need one symbol to locate the error within the block, and another symbol to contain the correction
- Code is described as $RS_{2^N}(\text{Total symbols}, \text{Payload symbols})$
 - For example $RS_{256}(128, 120)$ would have 120 payload bytes in a frame with 8 check bytes capable of correcting 4 bytes in the frame
- Optimal RS block size is typically chosen such that 2^N symbols are just slightly larger than the number of symbols you have to correct
 - This usually maximizes the number of correctable symbols within the block

“Free” bits within the 40GBASE-T Frame

- 40GBASE-T is based on reusing 10GBASE-T frame
- Within 10GBASE-T frame are the following possible bits:
 - Auxiliary bit
 - CRC-8 (presumably not needed as RS coverage is better than CRC)
 - 50 potentially superfluous 65B frames – i.e. can convert to 129B, 257B, etc. assuming the control code and ordered set start locations can be adequately mapped from XGMII
- Error control code has to protect $512 \times 3 = 1536$ uncoded bits

“Free” bits within the 40GBASE-T Frame (continued)

- Current 40GBASE-T scheme:
 - Converts 50x 65B blocks into 2x 65B + 12x 257B freeing up 36 bits
 - Combine with CRC-8 to create 44 free bits
 - Use an 11-bit symbol to create a 2 symbol correcting RS2048 code
 - Thus 1536 bits maps into 140 11-bit symbols with 4x zero bits giving us an RS2048(144,140) code
- Unfortunately, the symbol size is not optimal, as RS2048 can deal with a 2047 x 11-bit block

Optimal RS Code Choice for 40GBASE-T

- Working in a 2^N -based field, we have the following choices for 1536 bits:
 - $2^7 = \text{RS128}$ gives a maximum block size of $127 \times 7 = 889$ bits
 - $2^8 = \text{RS256}$ gives a maximum block size of $255 \times 8 = 2040$ bits
- RS256 is the best choice as $1536 \text{ bits} = 192 \text{ bytes}$
- Issue is that we need 48 bits instead of 44 bits to make GF256 effective (correct 3x 8-bit symbols)
- So we need four more bits from the frame

40GBASE-T Error Control Coding Proposal

- Convert 50x 65B blocks into 2x 65B + 6x 513B blocks freeing up 42 bits
- Combine with CRC-8 to create 50 free bits
- Use an 8-bit symbol to create a 3 symbol correcting RS256 code
- Thus 1536 bits maps into 192 8-bit symbols with 2x zero bits giving us an RS256(198,192) code

512/513B Encoding

- The 64/66B PCS of 40GBASE-R uses 11 block field types to transport all of the Start-of-Frame, End-of-Frame, and Ordered Set information received from the XLGMII interface*

| Input Data | Syn c | Block Payload | | | | | | | | | | | |
|---|-------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----|
| Bit Position: | | 0 | 1 | | | | | | | | | 2 | 65 |
| Data Block Format: | | | | | | | | | | | | | |
| D ₀ D ₁ D ₂ D ₃ D ₄ D ₅ D ₆ D ₇ | 01 | D ₀ | D ₁ | D ₂ | D ₃ | D ₄ | D ₅ | D ₆ | D ₇ | | | | |
| Control Block Formats: | | | | | | | | | | | | | |
| C ₀ C ₁ C ₂ C ₃ C ₄ C ₅ C ₆ C ₇ | 10 | 0x1E | C ₀ | C ₁ | C ₂ | C ₃ | C ₄ | C ₅ | C ₆ | C ₇ | | | |
| S ₀ D ₁ D ₂ D ₃ D ₄ D ₅ D ₆ D ₇ | 10 | 0x78 | D ₁ | D ₂ | D ₃ | D ₄ | D ₅ | D ₆ | D ₇ | | | | |
| O ₀ D ₁ D ₂ D ₃ Z ₄ Z ₅ Z ₆ Z ₇ | 10 | 0x4B | D ₁ | D ₂ | D ₃ | O ₀ | 0x000_0000 | | | | | | |
| T ₀ C ₁ C ₂ C ₃ C ₄ C ₅ C ₆ C ₇ | 10 | 0x87 | | | C ₁ | C ₂ | C ₃ | C ₄ | C ₅ | C ₆ | C ₇ | | |
| D ₀ T ₁ C ₂ C ₃ C ₄ C ₅ C ₆ C ₇ | 10 | 0x99 | D ₀ | | | C ₂ | C ₃ | C ₄ | C ₅ | C ₆ | C ₇ | | |
| D ₀ D ₁ T ₂ C ₃ C ₄ C ₅ C ₆ C ₇ | 10 | 0xAA | D ₀ | D ₁ | | | C ₃ | C ₄ | C ₅ | C ₆ | C ₇ | | |
| D ₀ D ₁ D ₂ T ₃ C ₄ C ₅ C ₆ C ₇ | 10 | 0xB4 | D ₀ | D ₁ | D ₂ | | | C ₄ | C ₅ | C ₆ | C ₇ | | |
| D ₀ D ₁ D ₂ D ₃ T ₄ C ₅ C ₆ C ₇ | 10 | 0xCC | D ₀ | D ₁ | D ₂ | D ₃ | | | | C ₅ | C ₆ | C ₇ | |
| D ₀ D ₁ D ₂ D ₃ D ₄ T ₅ C ₆ C ₇ | 10 | 0xD2 | D ₀ | D ₁ | D ₂ | D ₃ | D ₄ | | | C ₆ | C ₇ | | |
| D ₀ D ₁ D ₂ D ₃ D ₄ D ₅ T ₆ C ₇ | 10 | 0xE1 | D ₀ | D ₁ | D ₂ | D ₃ | D ₄ | D ₅ | C ₇ | | | | |
| D ₀ D ₁ D ₂ D ₃ D ₄ D ₅ D ₆ T ₇ | 10 | 0xFF | D ₀ | D ₁ | D ₂ | D ₃ | D ₄ | D ₅ | D ₆ | | | | |

Figure 82-5—64B/66B block formats

* Versus 15 block field types in 10G

512/513B Encoding (continued)

- Since the block field type is an 8-bit value, there are 256 possible block field types, of which 11 are used
- Requires 4 bits to represent these block field types, leaving us 4 bits to encode all possible combinations of 64/66 block types in all combinations of 8 locations
- This can only be done using a clever scheme such as Trowbridge, et al. presented in 2007 (http://www.ieee802.org/3/hssg/public/july07/trowbridge_010707.pdf)
 - Here he uses the control/data bit for the block to indicate whether there are control frames present
 - If there are they are all placed at the top of the block with the first bit being used to indicate whether there are more control blocks to follow, and the next three bits to indicate the row

512/513B Encoding (continued)

1 indicates another control block to follow

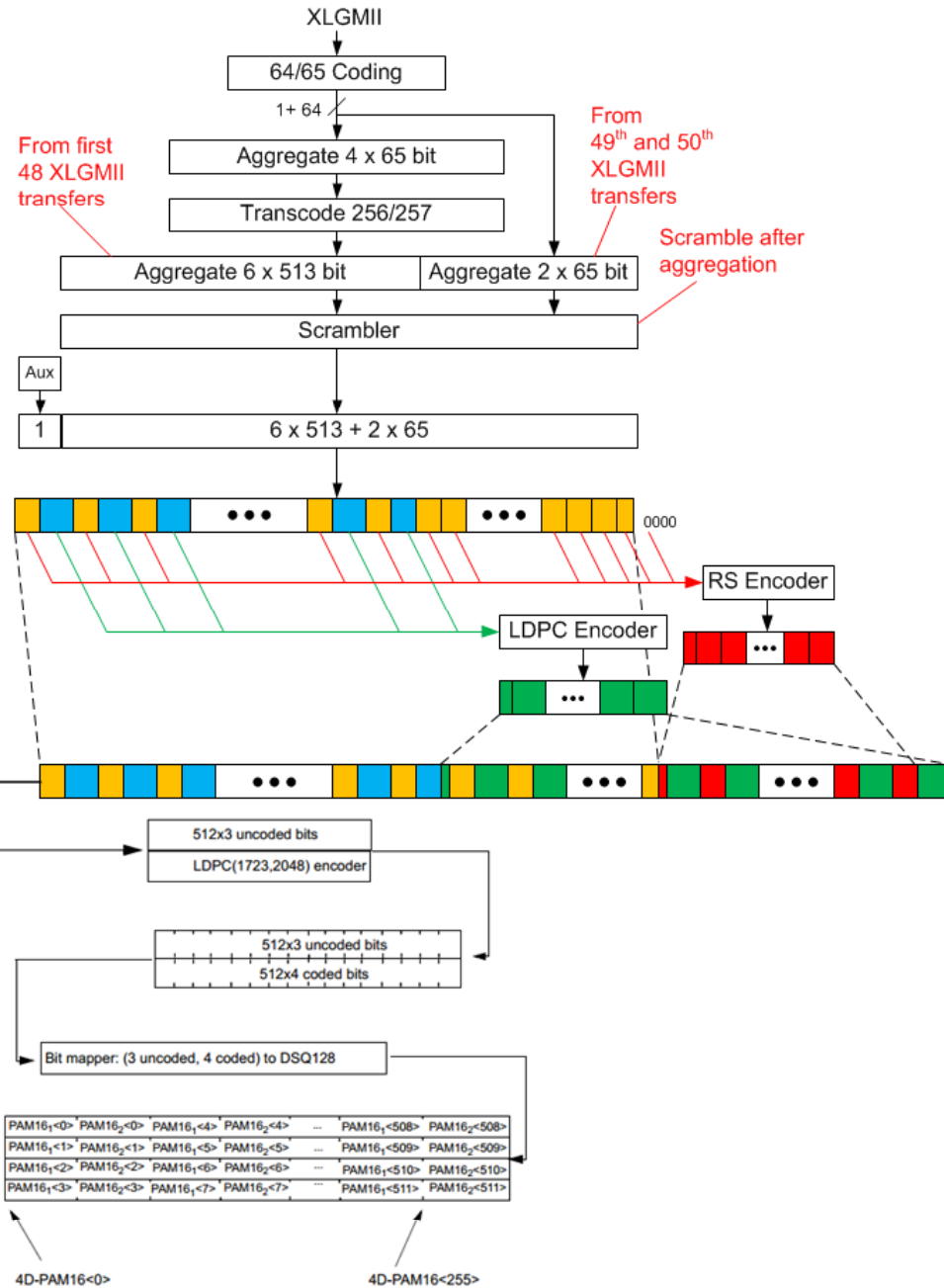
3-bit *rrr* indicates which row the control block came from

0 indicates no more control blocks to follow

4-bit *cccc* indicates the original block field type

| | | | | | | | |
|----------|---|---|---|---|---|---|---|
| 1rrrcccc | C | C | C | C | C | C | C |
| 1rrrcccc | C | C | C | C | C | C | C |
| 0rrrcccc | C | C | C | C | C | C | C |
| D | D | D | D | D | D | D | D |
| D | D | D | D | D | D | D | D |
| D | D | D | D | D | D | D | D |
| D | D | D | D | D | D | D | D |
| D | D | D | D | D | D | D | D |

Mapping



RS256(198,192) generator:

$$g(x) = \prod_{j=0}^2 (x - \alpha^j) = g_4x^4 + g_3x^3 + g_2x^2 + g_1x + g_0$$

Generator

- RS256(198,192) generator:

$$g(x) = \prod_{j=0}^5 (x - \alpha^j) = g_6x^6 + g_5x^5 + g_4x^4 + g_3x^3 + g_2x^2 + g_1x + g_0$$

where α is a primitive element of the finite field defined by the polynomial $0x11D = x^8 + x^4 + x^3 + x^2 + 1$

Complexity

- Using a symbol-based Euclidean decoder:
- RS2048(144,140)
 - 1048 XOR gates, 354 AND gates, 213 x 11 Flops, 295 x 11 Regfile, 1x 11-bit lookup
- RS256(198,192)
 - 1434 XOR gates, 300 AND gates, 324 x 8 Flops, 405 x 8 Regfile, 1x 8-bit lookup

- Roughly equivalent complexity

Conclusion

- With this modification we can correct 3 groups of 8 bits, versus 2 groups of 11 bits, allowing for greater and more flexible protection against uncoded bit errors