

Effect of Package Trace and Termination Resistance on Tx Specification

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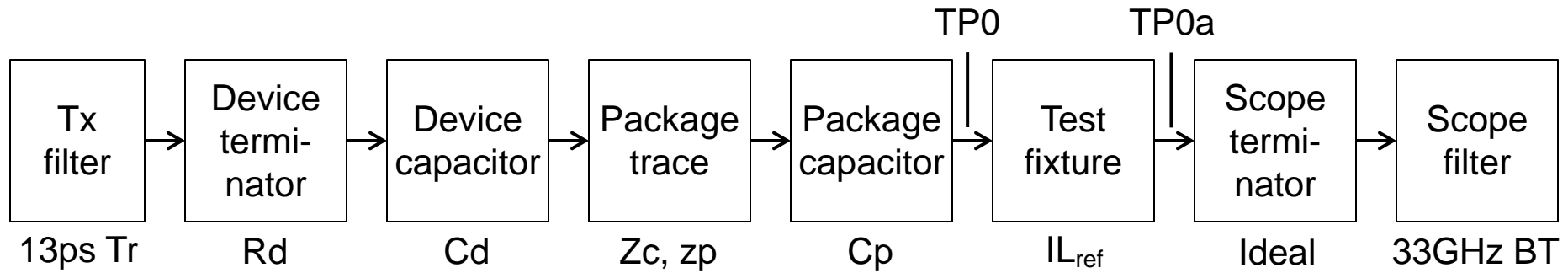
- I have reported that we may need to revise package trace impedance (Z_c , 90Ω) and termination resistance (R_d , 55Ω) in the COM parameters, because they do not necessarily cover corner cases (hidaka_100516_3cd_adhoc.pdf)
- There was a concern that Tx-related COM parameters such as signal amplitude and SNR_{TX} may have to be changed consistently with package parameters, because Tx output amplitude and Tx SNDR will be also affected by the package trace impedance and termination resistance
- Hence, I have studied the effect of package trace impedance and termination resistance on Tx output amplitude and Tx SNDR

Simulated Package Parameters

- The following 10 combinations of parameters were simulated

Case	z _p Package trace length	R _d Termination resistance	Z _c Package trace impedance
#1	12 mm	45 Ω	90 Ω
#2			110 Ω
#3		55 Ω	90 Ω
#4			110 Ω
#5	30 mm	45 Ω	90 Ω
#6			110 Ω
#7		55 Ω	90 Ω
#8			110 Ω
#9	12 mm	50 Ω	100 Ω
#10	30 mm		

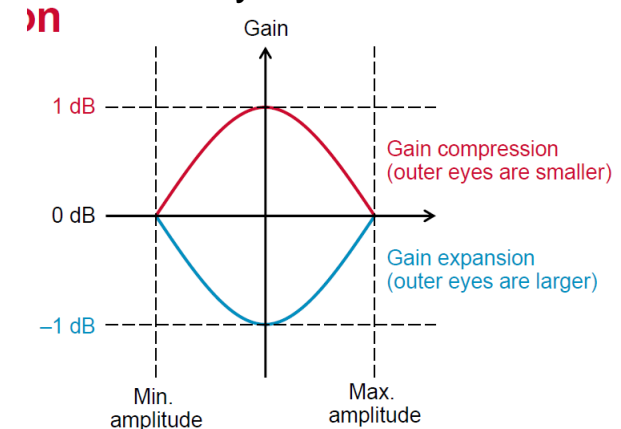
- The conditions proposed in hidaka_100516_3cd_adhoc.pdf were **#2/#3/#4** and **#6/#7/#8**



- Tx filter: $S_{21} = (\text{EQ93A-46} | T_r = 13\text{ps}, \beta = 2)$ (i.e. 13ps 20-80% Tr)
- Device terminator: $S_{21} = 1, S_{22} = \frac{R_d - 50\Omega}{R_d + 50\Omega}$
- Device capacitor: $S = (\text{EQ93A-8} | C = C_d)$
- Package trace: $S = (\text{EQ93A-13,14} | \text{Table93A-3 except } Z_c, z_p)$
- Package capacitor: $S = (\text{EQ93A-8} | C = C_p)$
- Test fixture: $|S_{21}| = 10^{-(\text{EQ93-1})/20}, \angle S_{21} = \text{minimum phase}(|S_{21}|)$
- Scope terminator: $S_{21} = 1, S_{11} = 0$ (i.e. ideal)
- Scope filter: 4-th order Bessel-Thomson LPF with 33GHz 3dB BW
 - $\omega_0 = 98.28967142447435 \text{ G rad/s}$

1. Get S_{21} of the entire model from 1MHz to f_{max} with 1MHz step
 - $f_{max} = 26.5625\text{GHz} \times M \div 2$, where $M = 32$
2. Get a single-bit pulse response
3. Get a linear cycle response of PRBS13Q with ideal levels
4. Cancel the DC offset of the linear cycle response of PRBS13Q
5. Get a non-linear cycle response of PRBS13Q by gain expansion / compression (similar to a methodology in healey_3bs_02_0916)
 - Simulated from -1.0dB to +1.0dB with 0.2dB step
6. Get V0, V1, V2, and V3 per 120D.3.1.2.1
7. Get Vmid, ES1, and ES2 per 120D.3.1.2
8. Get $ES = (ES1 + ES2) / 2$ per 120D.3.1.3
9. Get linear fit pulse $p(k)$ and error $e(k)$ per 120D.3.1.3, 94.3.12.5.2, 85.8.3.3.5
 - $D_p = 2$ and $N_p = 200$
10. Get steady-state voltage v_f and linear fit pulse peak p_{max} per 120D.3.1.4
11. Get σ_e from $e(k)$, then get SNDR per 120D.3.1.6
 - σ_n is always set to $p_{max} \times 10^{(-50/20)}$ (i.e. -50dB) to have noise floor

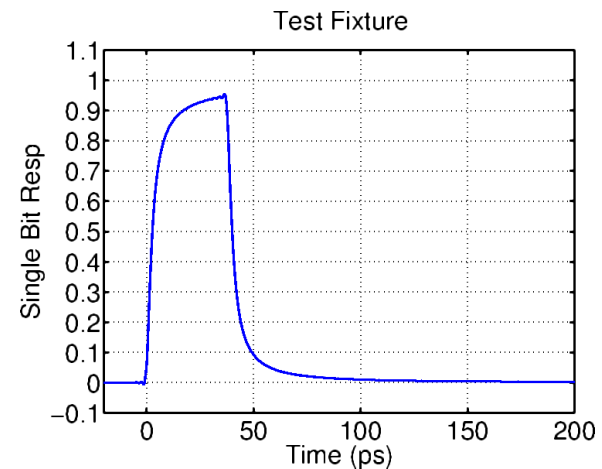
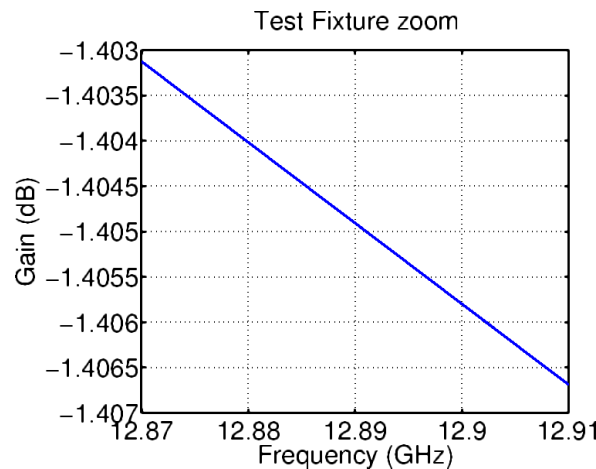
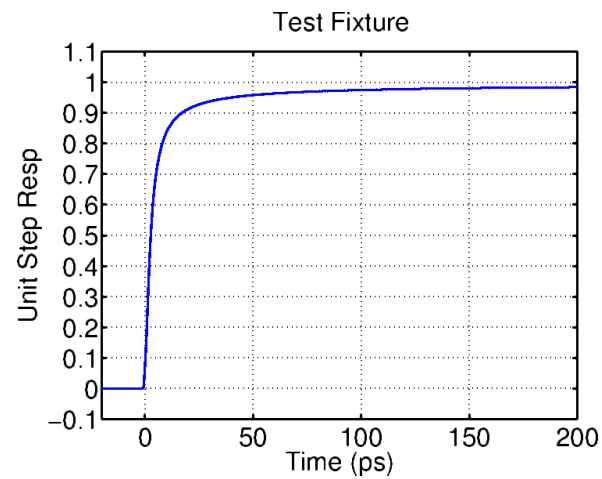
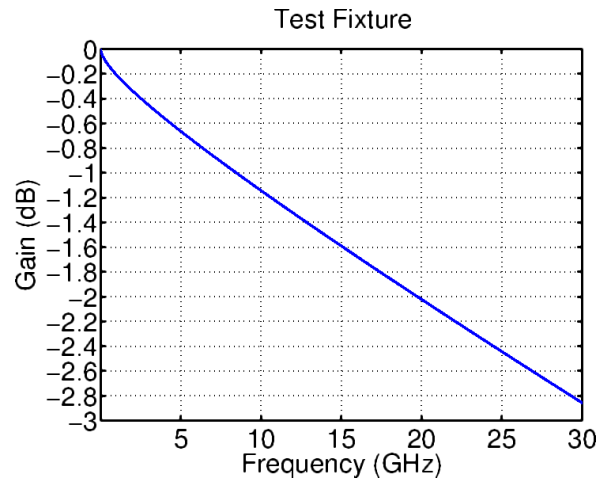
From healey_3bs_02_0916



■ The reference insertion loss of the test fixture is defined by

$$\blacksquare IL_{ref}(f) = -0.0015 + 0.144\sqrt{f} + 0.069f \quad (93-1)$$

- 1.4049dB at 12.89GHz

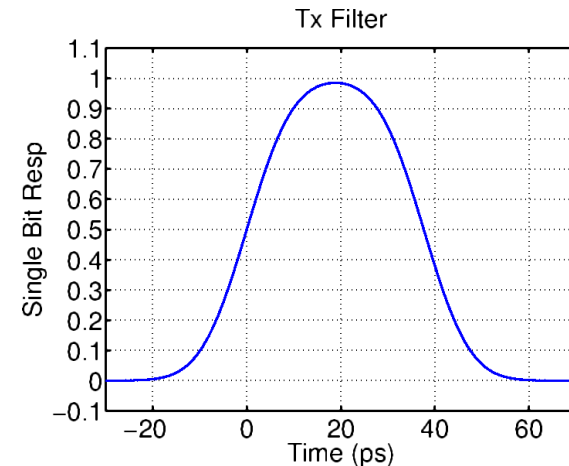
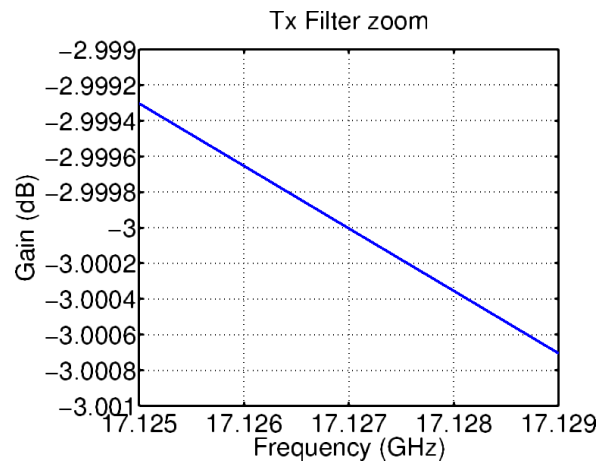
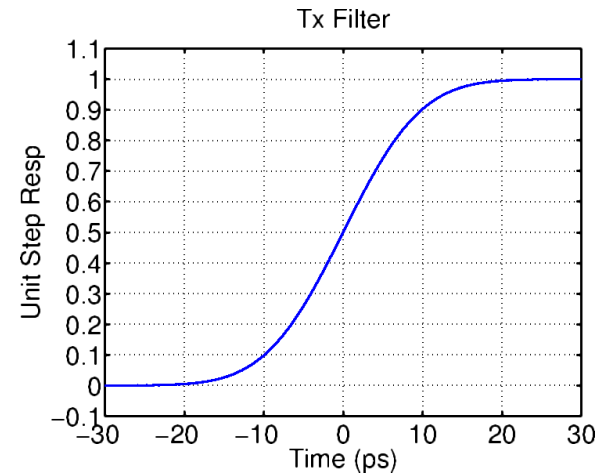
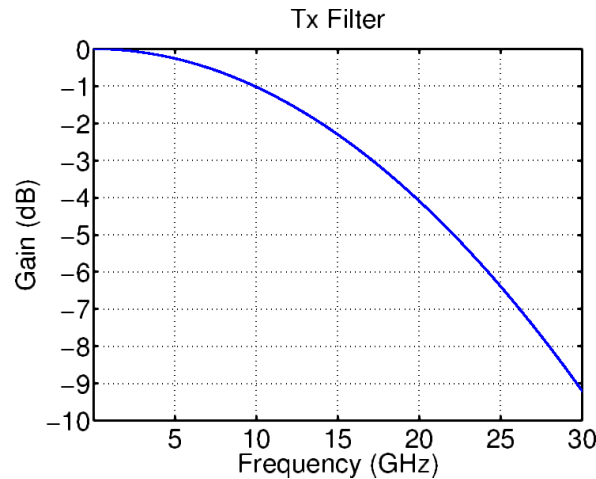


Tx Transition Time Filter

■ Tx Transition Time Filter (per 802.3by) is defined by

$$\blacksquare H_t(f) = \exp(-\beta(\pi f T_r / 1.6832)^2) \quad (93A-46)$$

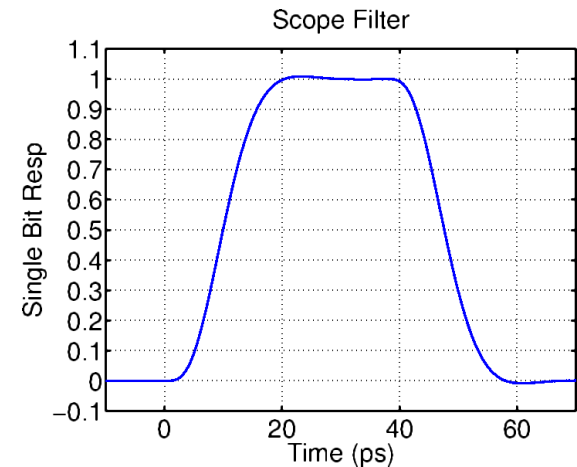
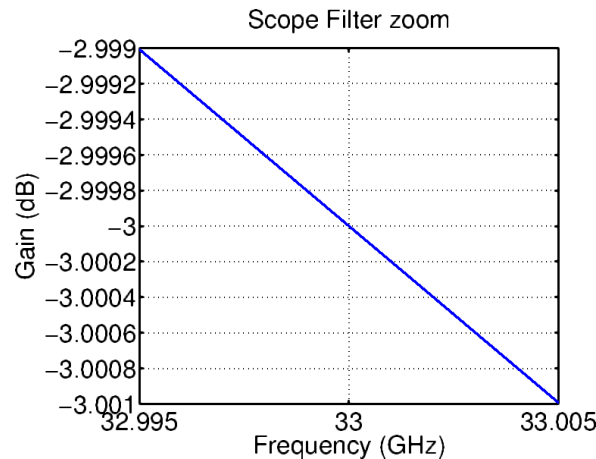
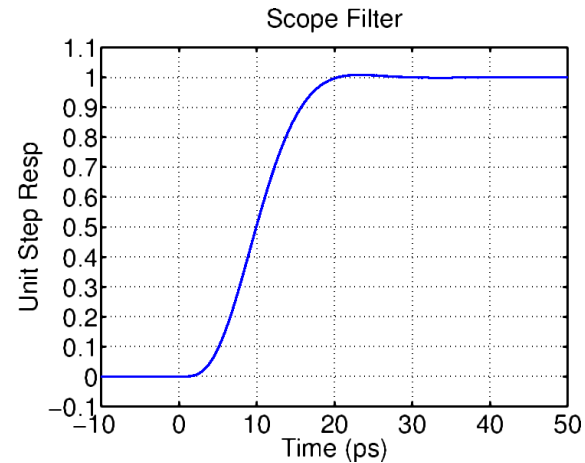
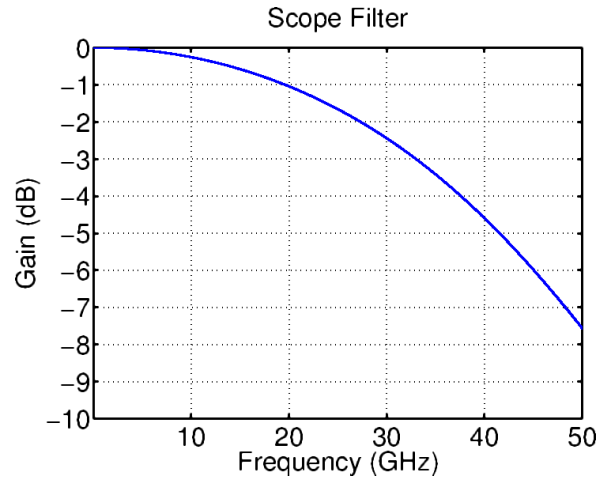
- with $\beta = 2, T_r = 13ps$



Scope Filter (4th-order Bessel-Thomson LPF)

■ A 4th-order BT LPF with 33GHz 3dB Bandwidth is defined by

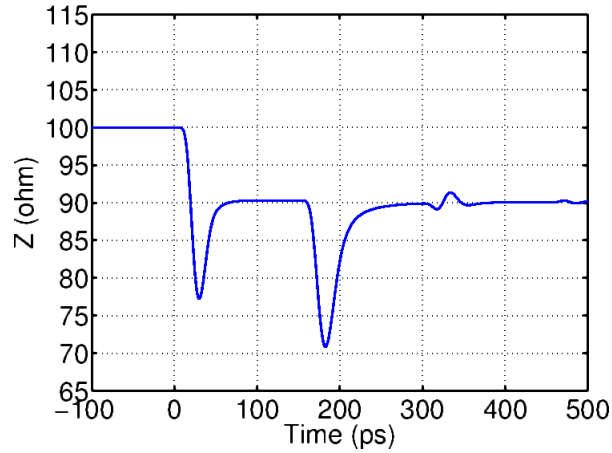
■ $H(s) = \theta_4(0)/\theta_4(s/\omega_0)$ where $\theta_4(s) = s^4 + 10s^3 + 45s^2 + 105s + 105$ and $\omega_0 = 98.28967142447435$ G rad/s



TDR of Entire Path from Scope (zp=12mm)

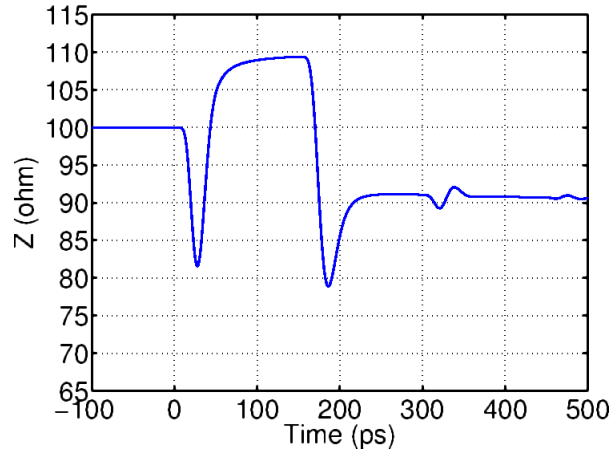
#1: $R_d=45$, $Z_c=90$

zp12 rd45 zc90



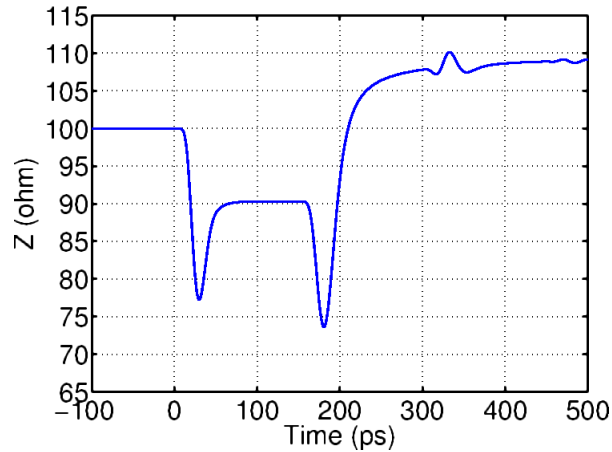
#2: $R_d=45$, $Z_c=110$

zp12 rd45 zc110



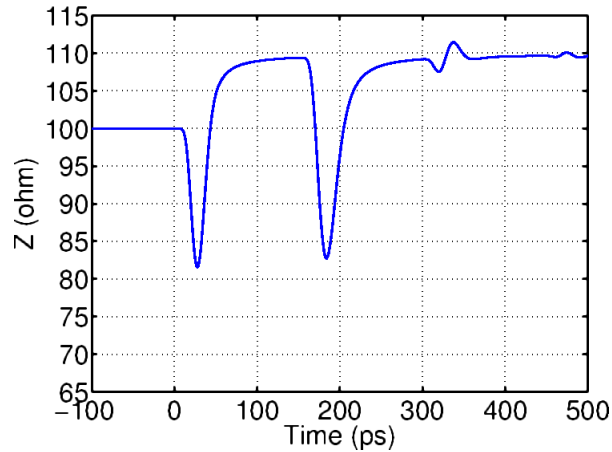
#3: $R_d=55$, $Z_c=90$

zp12 rd55 zc90



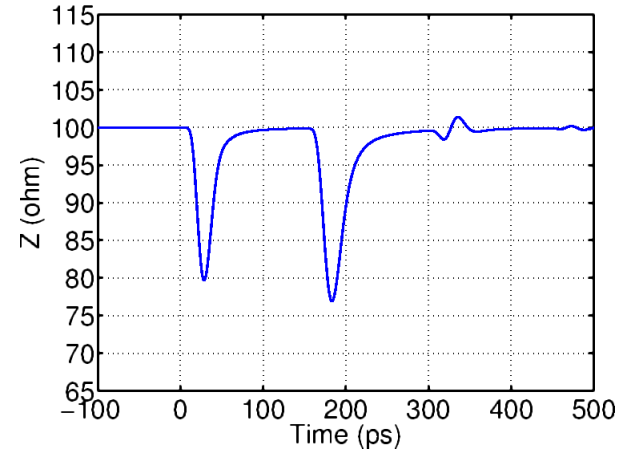
#4: $R_d=55$, $Z_c=110$

zp12 rd55 zc110



#9: $R_d=50$, $Z_c=100$

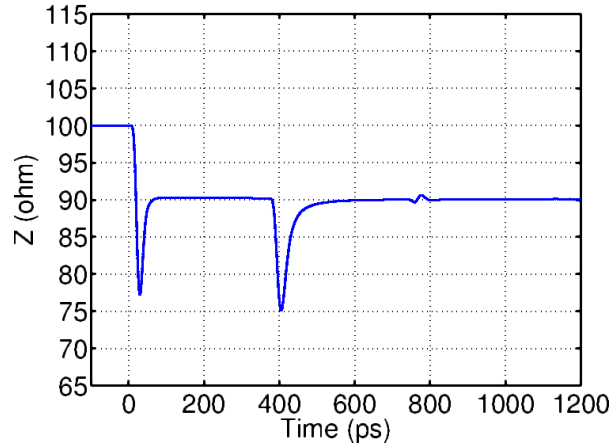
zp12 rd50 zc100



TDR of Entire Path from Scope (zp=30mm)

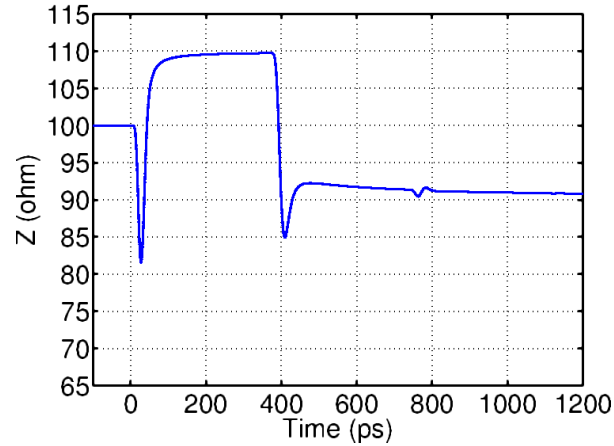
#5: $R_d=45$, $Z_c=90$

zp30 rd45 zc90



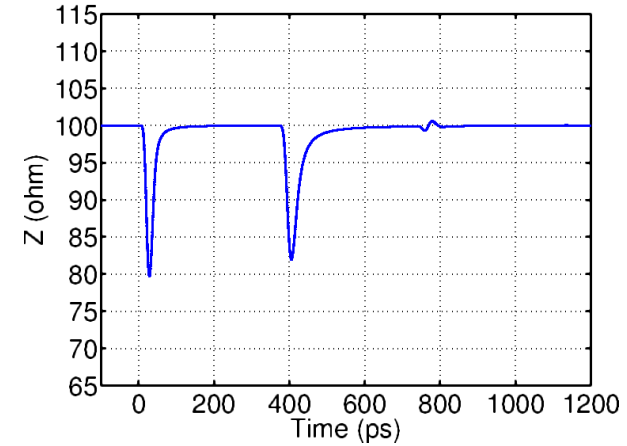
#6: $R_d=45$, $Z_c=110$

zp30 rd45 zc110



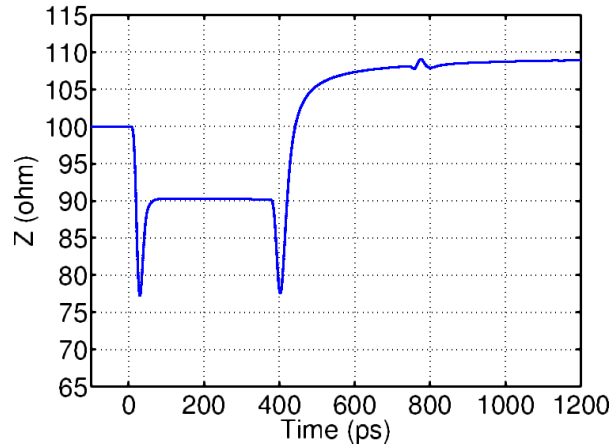
#10: $R_d=50$, $Z_c=100$

zp30 rd50 zc100



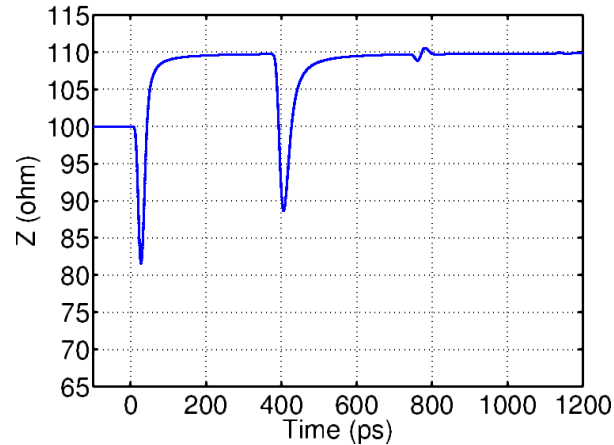
#7: $R_d=55$, $Z_c=90$

zp30 rd55 zc90



#8: $R_d=55$, $Z_c=110$

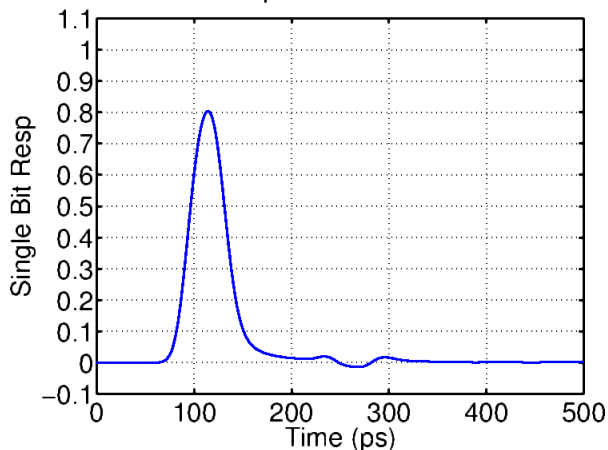
zp30 rd55 zc110



SBR of Entire Path (zp=12mm)

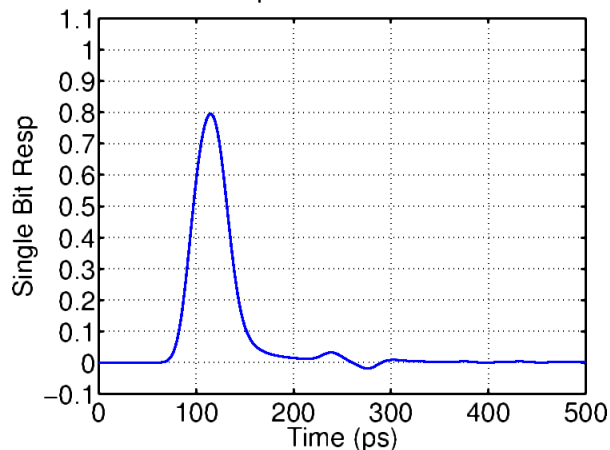
#1: Rd=45, Zc=90

zp12 rd45 zc90



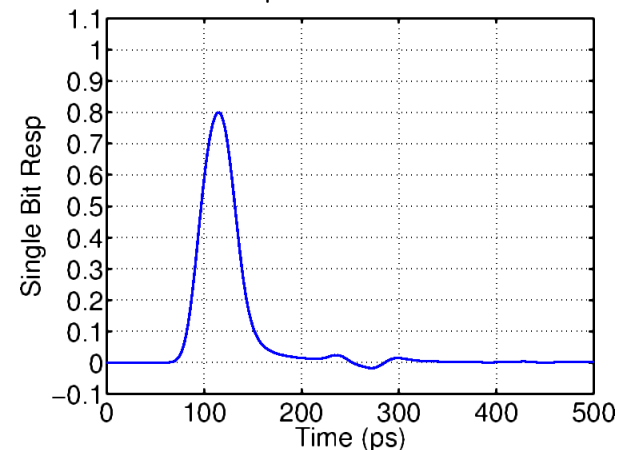
#2: Rd=45, Zc=110

zp12 rd45 zc110



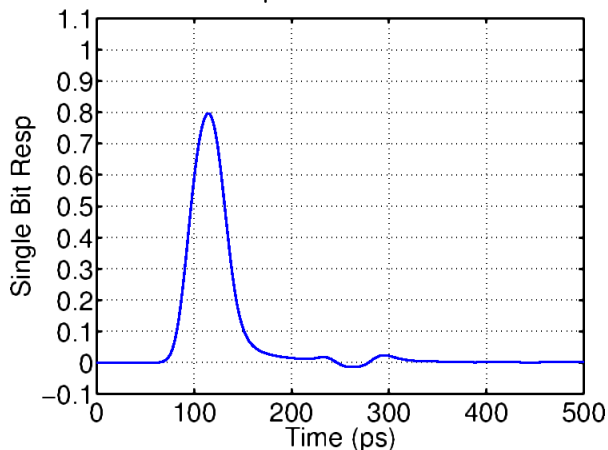
#9: Rd=50, Zc=100

zp12 rd50 zc100



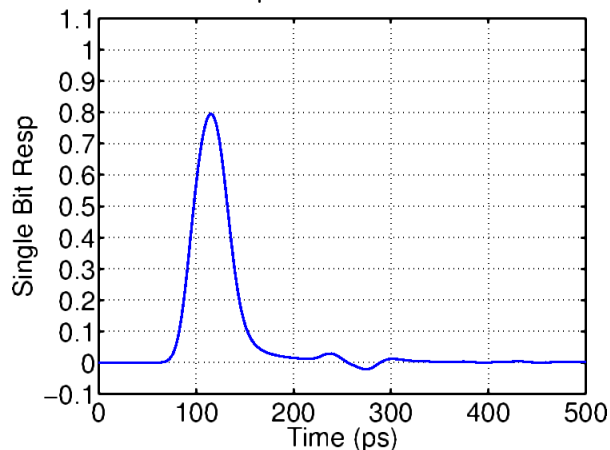
#3: Rd=55, Zc=90

zp12 rd55 zc90



#4: Rd=55, Zc=110

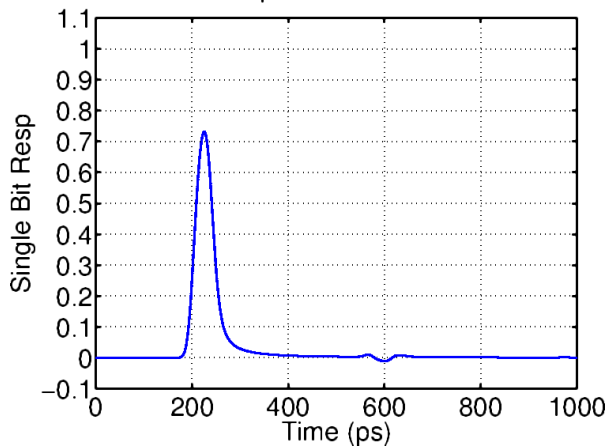
zp12 rd55 zc110



SBR of Entire Path (zp=30mm)

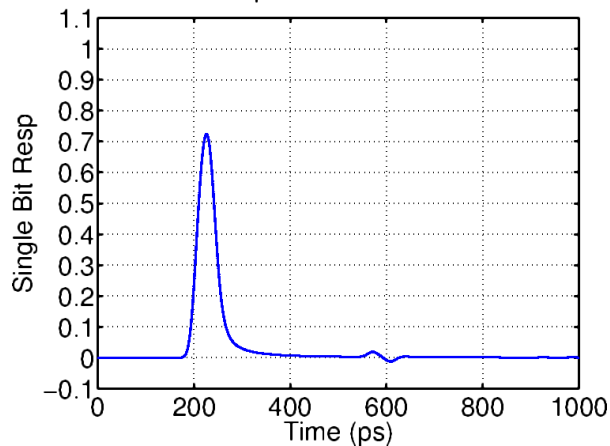
#5: Rd=45, Zc=90

zp30 rd45 zc90



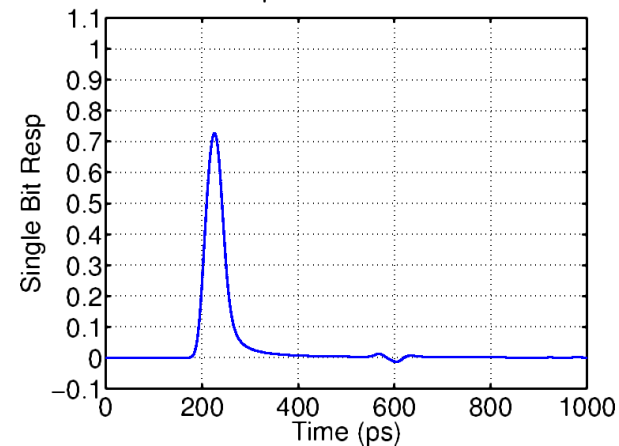
#6: Rd=45, Zc=110

zp30 rd45 zc110



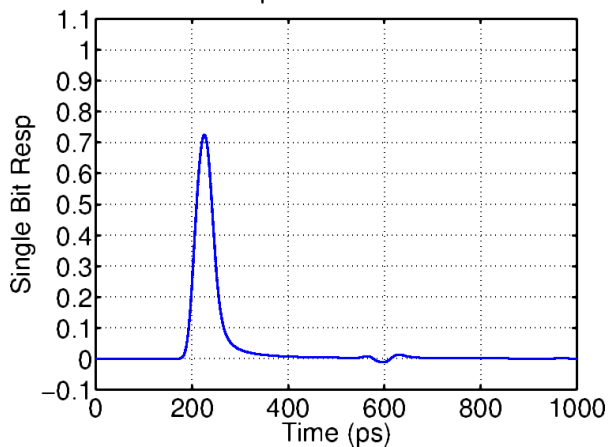
#10: Rd=50, Zc=100

zp30 rd50 zc100



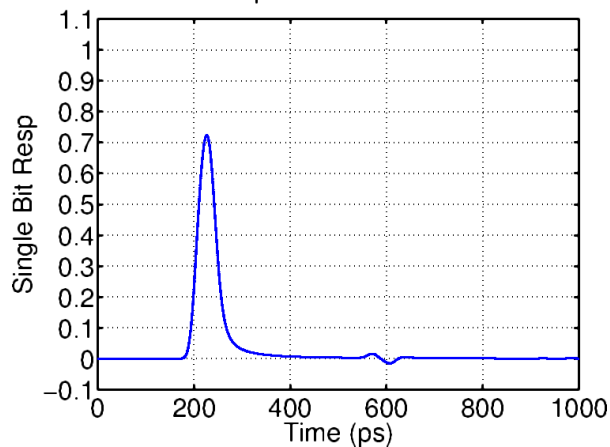
#7: Rd=55, Zc=90

zp30 rd55 zc90



#8: Rd=55, Zc=110

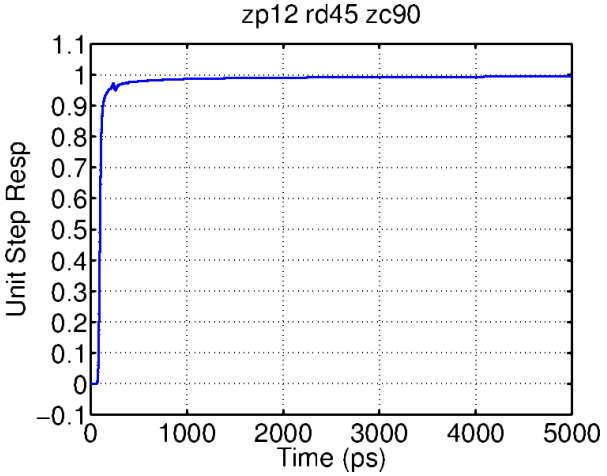
zp30 rd55 zc110



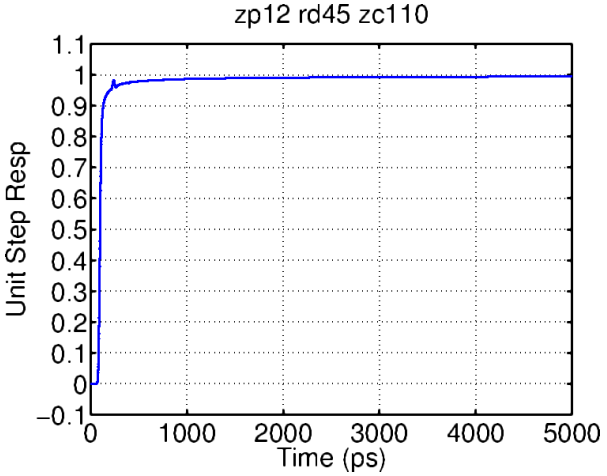
Step Response of Entire Path (zp=12mm)



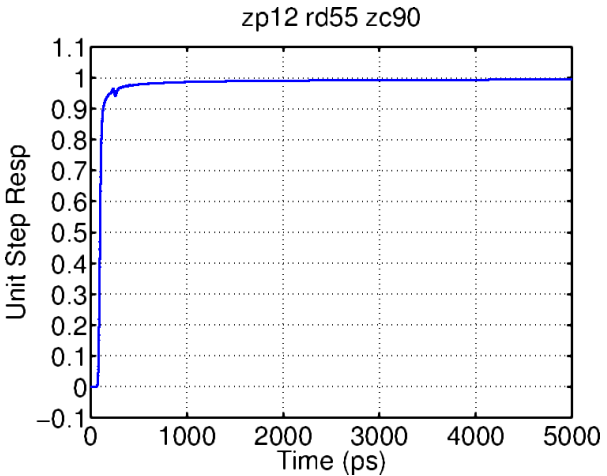
#1: Rd=45, Zc=90



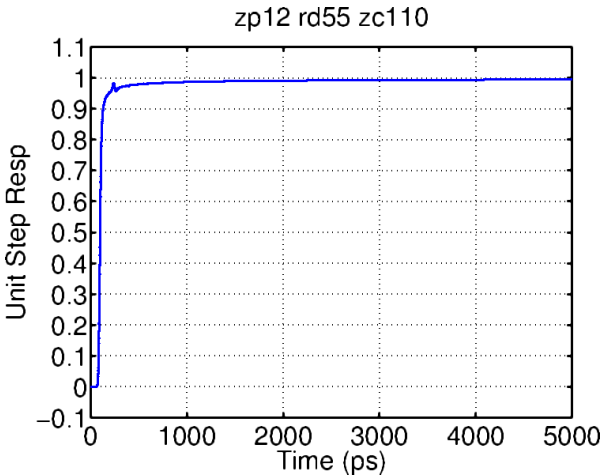
#2: Rd=45, Zc=110



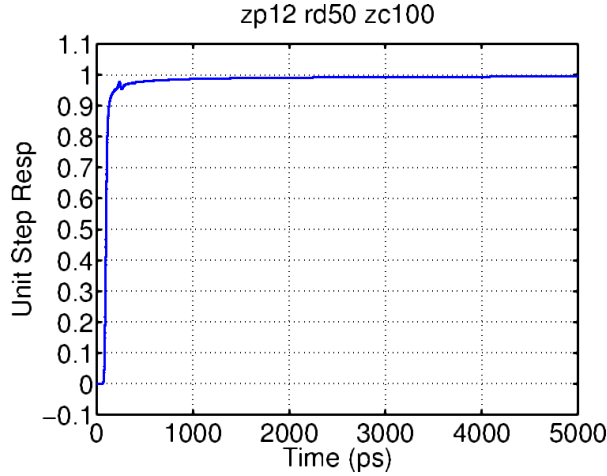
#3: Rd=55, Zc=90



#4: Rd=55, Zc=110



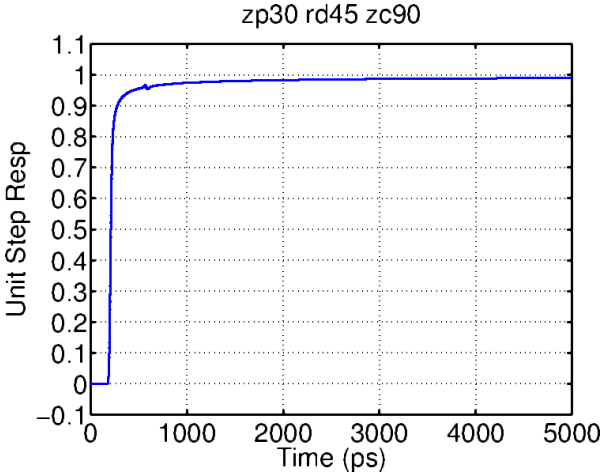
#9: Rd=50, Zc=100



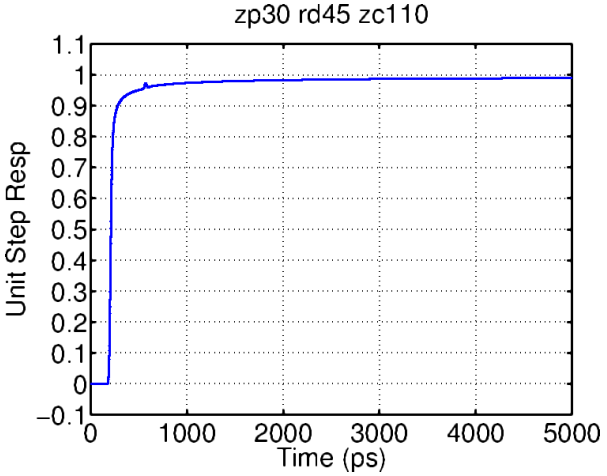
Step Response of Entire Path (zp=30mm)



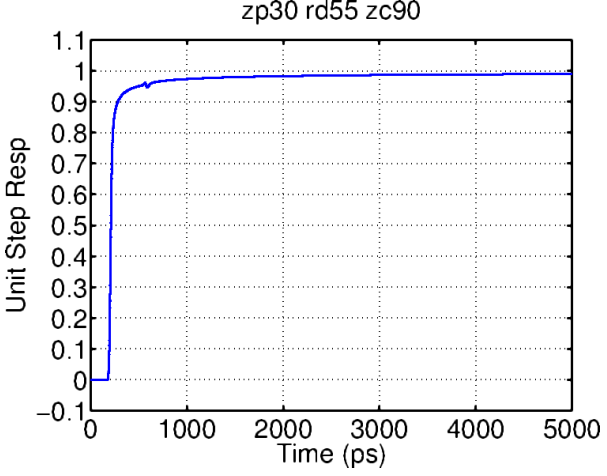
#5: Rd=45, Zc=90



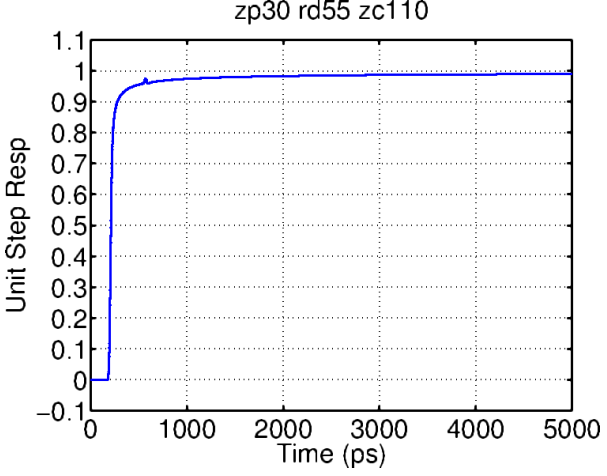
#6: Rd=45, Zc=110



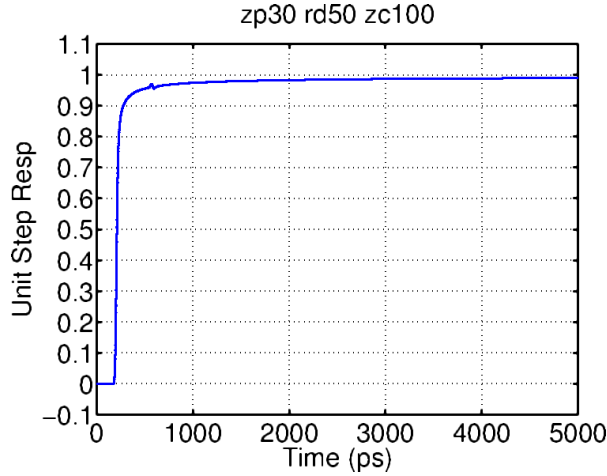
#7: Rd=55, Zc=90



#8: Rd=55, Zc=110



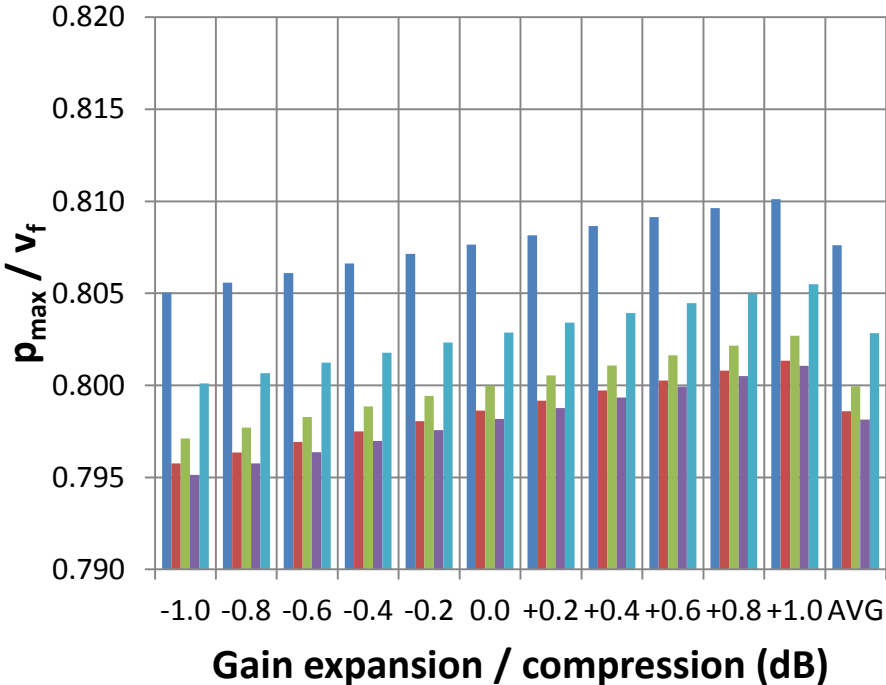
#10: Rd=50, Zc=100



Effect on the Ratio of p_{\max} to v_f ($N_p=200$)

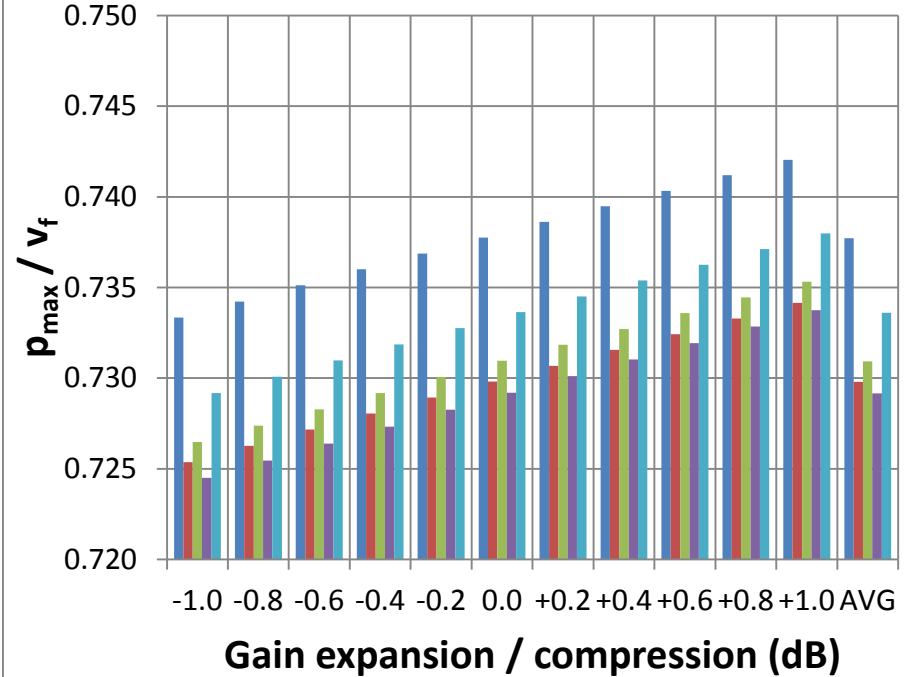
■ Between proposed conditions (#2/3/4, #6/7/8), the effect is rather small

p_{\max} / v_f ($z_p=12\text{mm}$, $N_p=200$)



■ #1 $R_d=45$ $Z_c=90$ ■ #2 $R_d=45$ $Z_c=110$ ■ #3 $R_d=55$ $Z_c=90$
■ #4 $R_d=55$ $Z_c=110$ ■ #9 $R_d=50$ $Z_c=100$

p_{\max} / v_f ($z_p=30\text{mm}$, $N_p=200$)

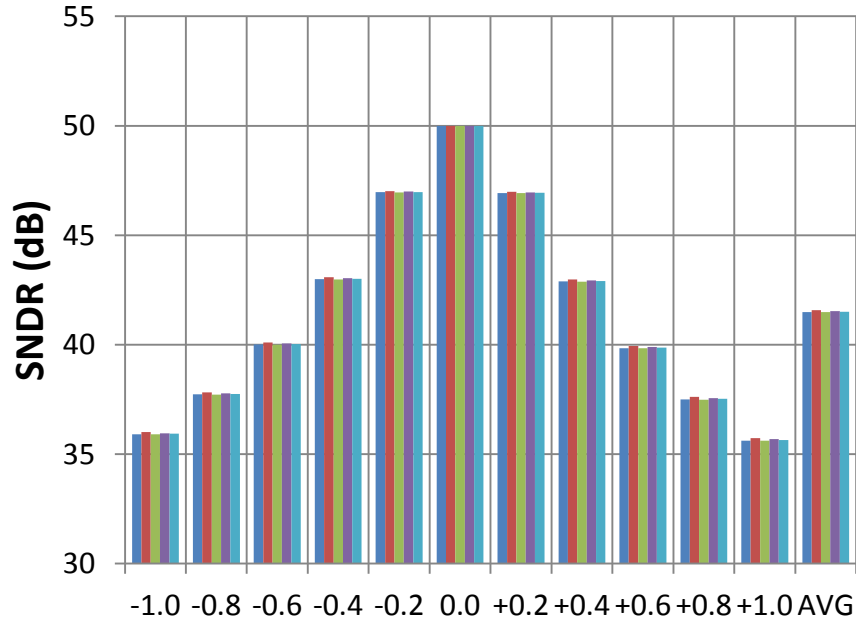


■ #5 $R_d=45$ $Z_c=90$ ■ #6 $R_d=45$ $Z_c=110$ ■ #7 $R_d=55$ $Z_c=90$
■ #8 $R_d=55$ $Z_c=110$ ■ #10 $R_d=50$ $Z_c=100$

Effect on SNDR (Np=200)

■ The effect is very little

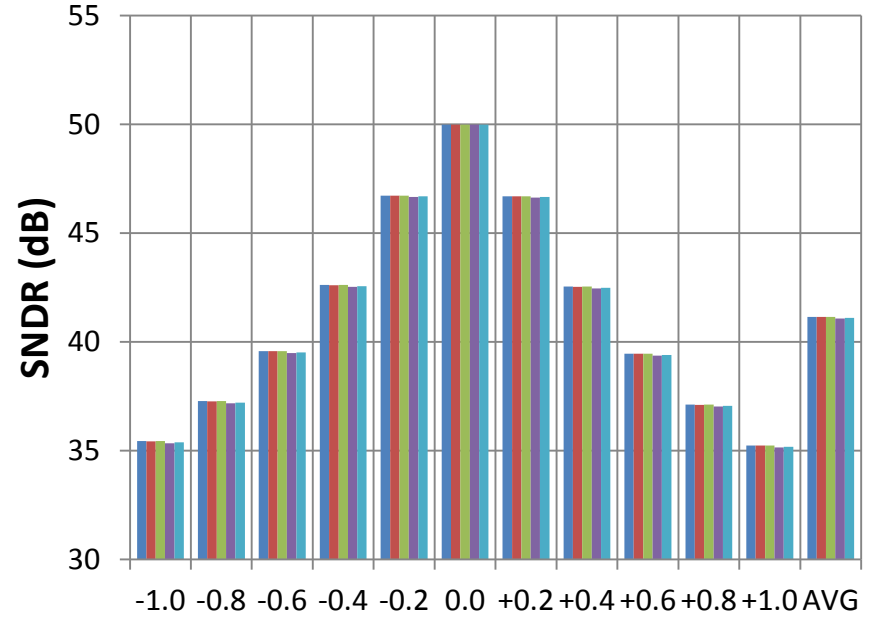
SNDR (z_p=12mm, N_p=200)



Gain expansion / compression (dB)

- #1 Rd=45 Zc=90
- #2 Rd=45 Zc=110
- #3 Rd=55 Zc=90
- #4 Rd=55 Zc=110
- #9 Rd=50 Zc=100

SNDR (z_p=30mm, N_p=200)



Gain expansion / compression (dB)

- #5 Rd=45 Zc=90
- #6 Rd=45 Zc=110
- #7 Rd=55 Zc=90
- #8 Rd=55 Zc=110
- #10 Rd=50 Zc=100

- The effects on the p_{\max} -to- v_f ratio and the SNDR are rather small

Back up Slides

- Linear Fit in 85.8.3.3.5
- Linear Fit Pulse Response $p(k)$ and Error Response $e(k)$
- Results for $N_p=13$
- Results of p_{\max}
- Results of v_f
- Results of σ_e
- Result Value Tables

Linear Fit in 85.8.3.3.5

$$\blacksquare Y = \begin{bmatrix} y(1) & y(M+1) & \cdots & y(M(N-1)+1) \\ y(2) & y(M+2) & \cdots & y(M(N-1)+2) \\ \cdots & \cdots & \cdots & \cdots \\ y(M) & y(2M) & \cdots & y(MN) \end{bmatrix} \quad (85-4)$$

$$\blacksquare x_r = [x(D_p + 1) \quad x(D_p + 2) \quad \cdots \quad x(N) \quad x(1) \quad \cdots \quad x(D_p)] \quad (85-5)$$

$$\blacksquare X = \begin{bmatrix} x_r(1) & x_r(2) & \cdots & x_r(N) \\ x_r(N) & x_r(1) & \cdots & x_r(N-1) \\ \cdots & \cdots & \cdots & \cdots \\ x_r(2) & x_r(3) & \cdots & x_r(1) \end{bmatrix} \quad (85-6)$$

$$\blacksquare X_1 = \begin{bmatrix} X(1:N_p, :) \\ \text{ones}(1, N) \end{bmatrix}$$

$$\blacksquare P = YX_1^T (X_1X_1^T)^{-1} \quad (85-7)$$

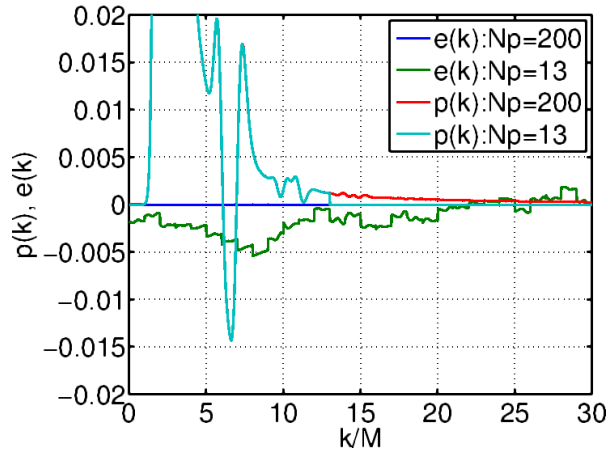
$$\blacksquare E = PX_1 - Y = \begin{bmatrix} e(1) & e(M+1) & \cdots & e(M(N-1)+1) \\ e(2) & e(M+2) & \cdots & e(M(N-1)+2) \\ \cdots & \cdots & \cdots & \cdots \\ e(M) & e(2M) & \cdots & e(MN) \end{bmatrix} \quad (85-8)$$

$$\blacksquare P_1 = P(:, 1:N_p) = \begin{bmatrix} p(1) & p(M+1) & \cdots & p(M(N-1)+1) \\ p(2) & p(M+2) & \cdots & p(M(N-1)+2) \\ \cdots & \cdots & \cdots & \cdots \\ p(M) & p(2M) & \cdots & p(MN) \end{bmatrix} \quad (85-9)$$

Linear Fit Pulse & Error (zp=12mm, Linear)

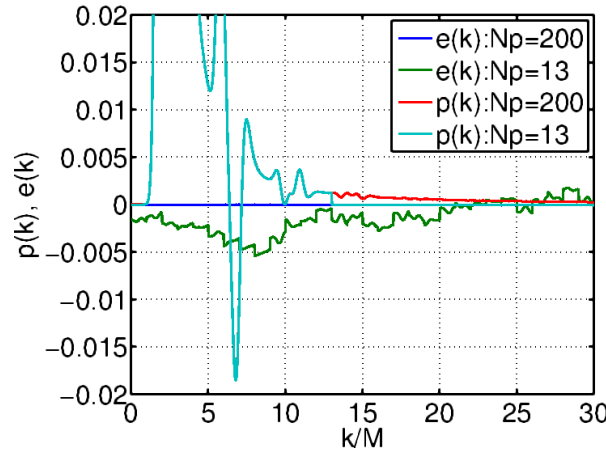
#1: Rd=45, Zc=90

zp12 rd45 zc90 gec0



#2: Rd=45, Zc=110

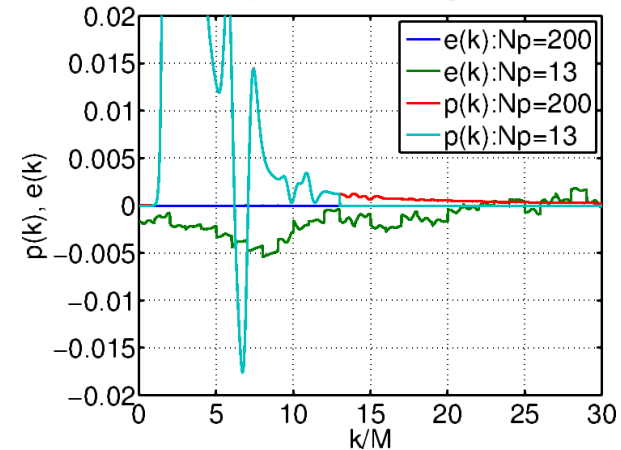
zp12 rd45 zc110 gec0



For Np=200,
e(k) is almost zero

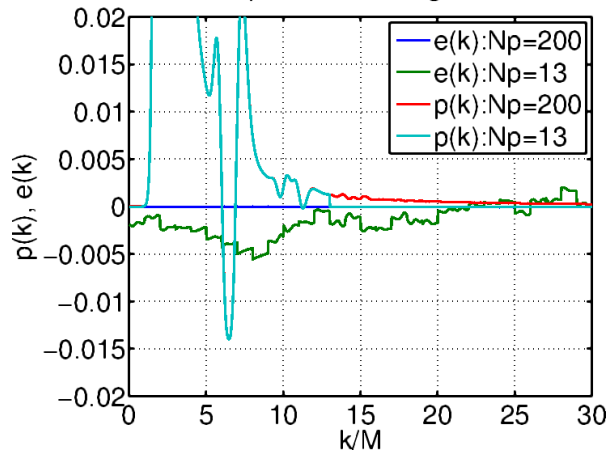
#9: Rd=50, Zc=100

zp12 rd50 zc100 gec0



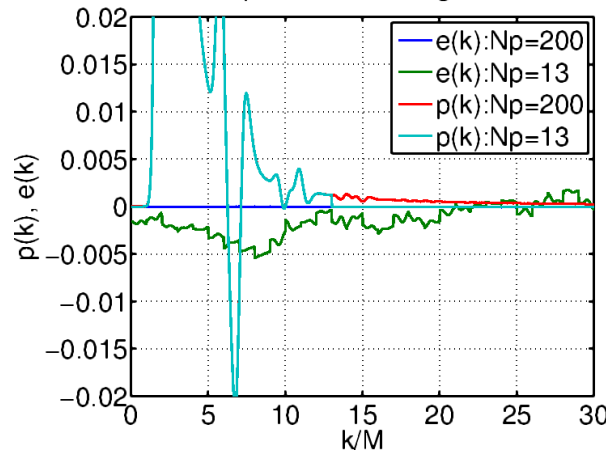
#3: Rd=55, Zc=90

zp12 rd55 zc90 gec0



#4: Rd=55, Zc=110

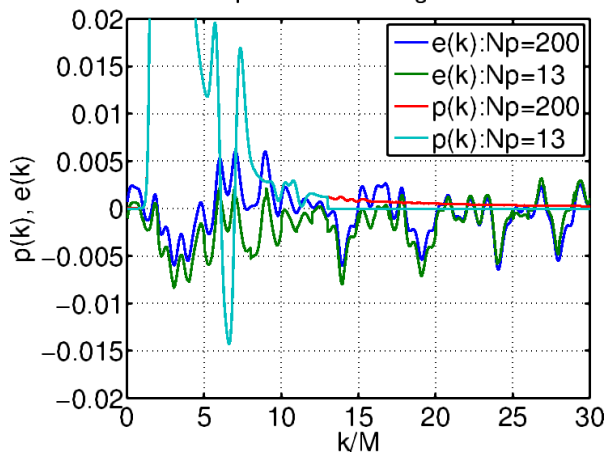
zp12 rd55 zc110 gec0



Linear Fit Pulse & Error (zp=12mm, Non-Linear)

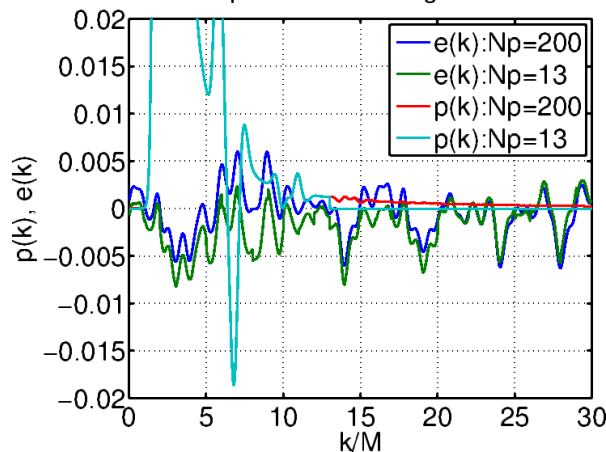
#1: Rd=45, Zc=90

zp12 rd45 zc90 gec0.2



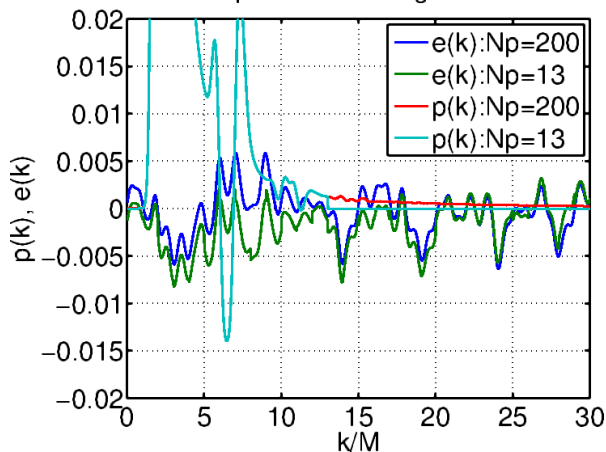
#2: Rd=45, Zc=110

zp12 rd45 zc110 gec0.2



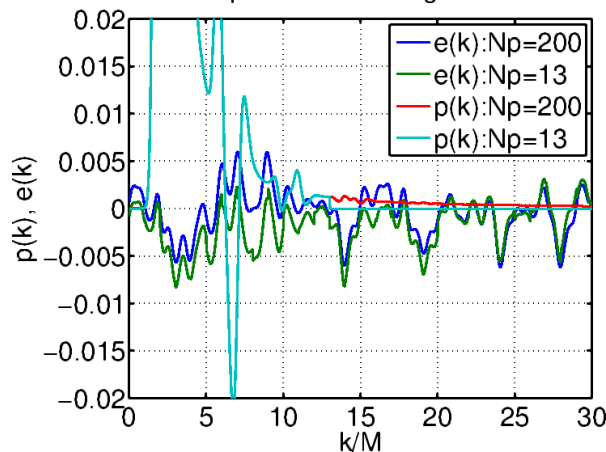
#3: Rd=55, Zc=90

zp12 rd55 zc90 gec0.2



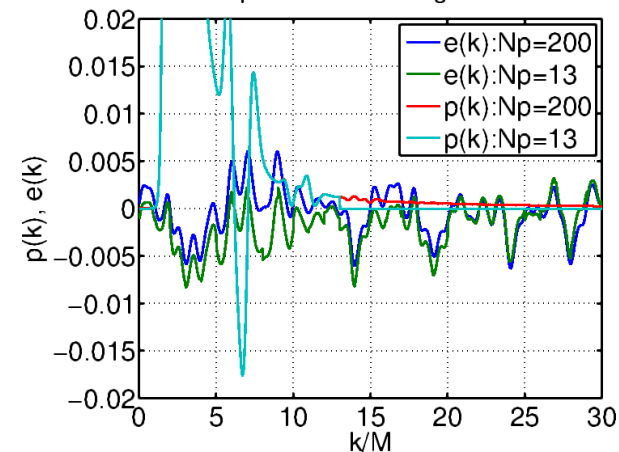
#4: Rd=55, Zc=110

zp12 rd55 zc110 gec0.2



#9: Rd=50, Zc=100

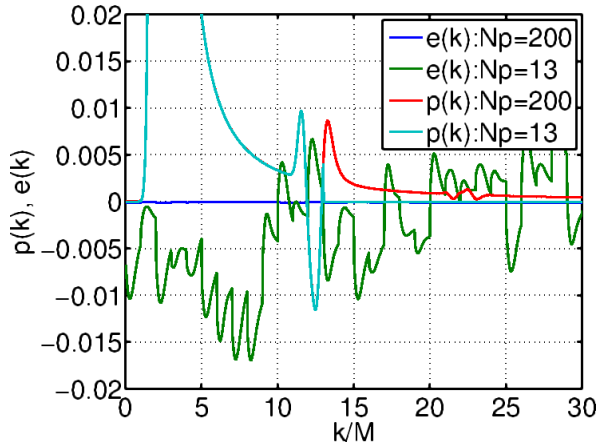
zp12 rd50 zc100 gec0.2



Linear Fit Pulse & Error (zp=30mm, Linear)

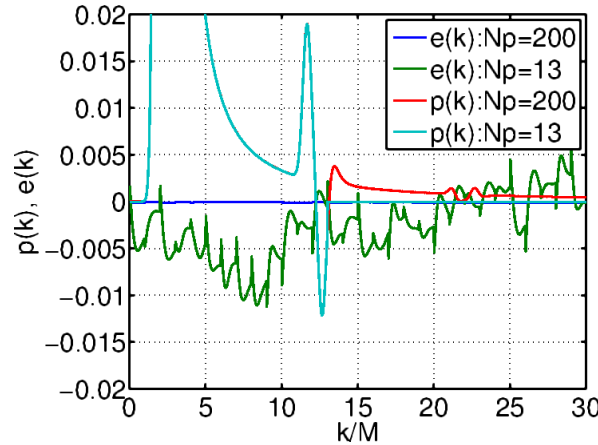
#5: Rd=45, Zc=90

zp30 rd45 zc90 gec0



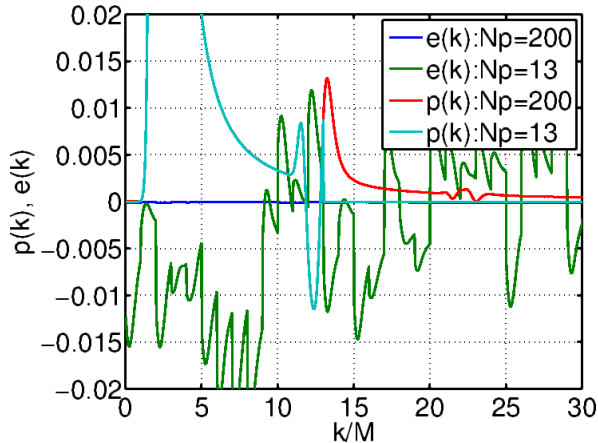
#6: Rd=45, Zc=110

zp30 rd45 zc110 gec0



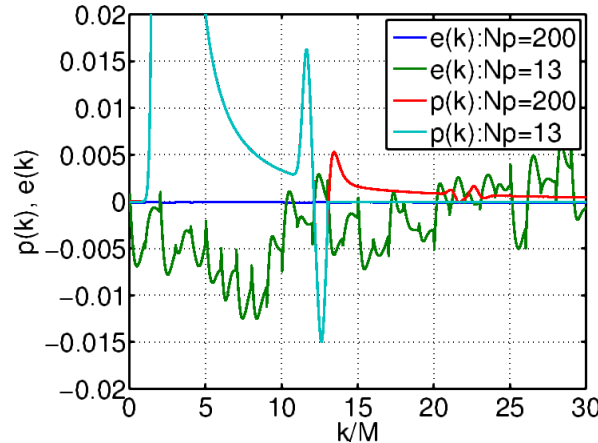
#7: Rd=55, Zc=90

zp30 rd55 zc90 gec0



#8: Rd=55, Zc=110

zp30 rd55 zc110 gec0

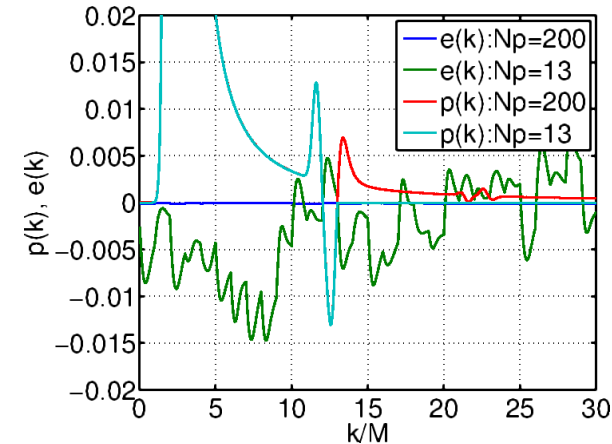


For $N_p=200$,
 $e(k)$ is almost zero

Different shape of reflection
just after 13 UI

#10: Rd=50, Zc=100

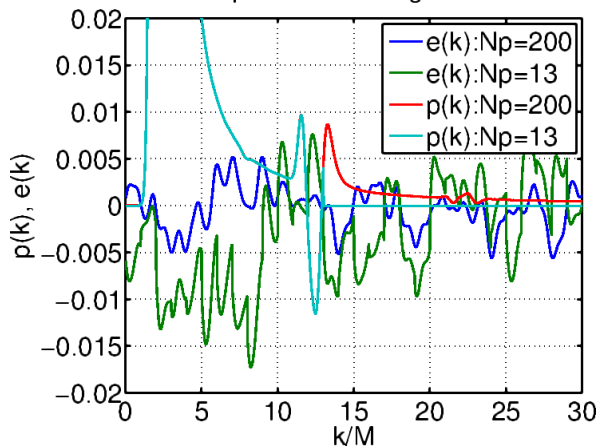
zp30 rd50 zc100 gec0



Linear Fit Pulse & Error (zp=30mm, Non-Linear)

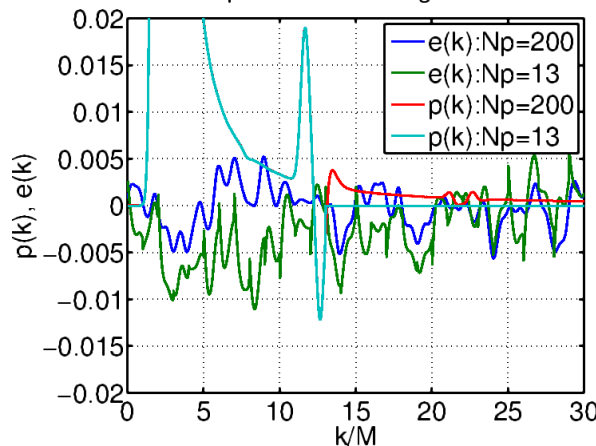
#5: Rd=45, Zc=90

zp30 rd45 zc90 gec0.2



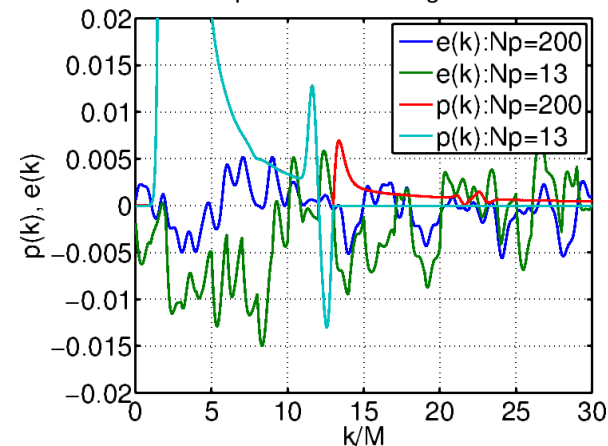
#6: Rd=45, Zc=110

zp30 rd45 zc110 gec0.2



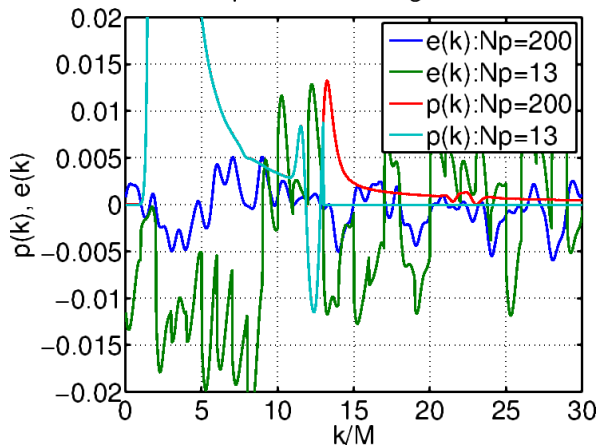
#10: Rd=50, Zc=100

zp30 rd50 zc100 gec0.2



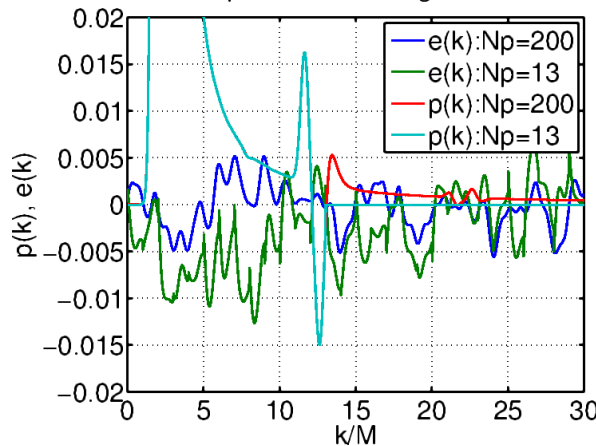
#7: Rd=55, Zc=90

zp30 rd55 zc90 gec0.2



#8: Rd=55, Zc=110

zp30 rd55 zc110 gec0.2

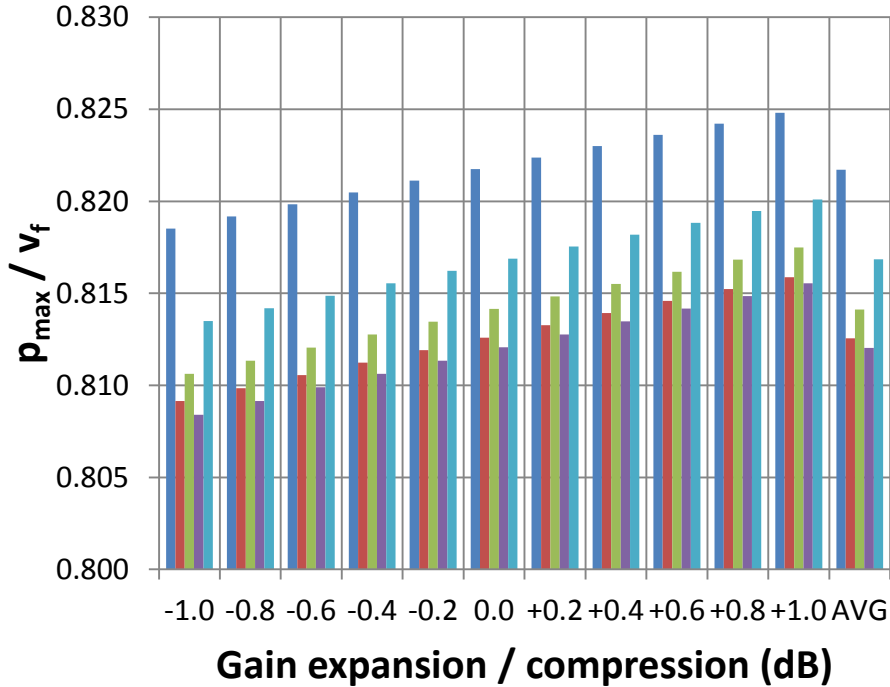


Effect on the Ratio of p_{\max} to v_f ($N_p=13$)

■ The effect gets larger with $z_p=30\text{mm}$ (right graph)

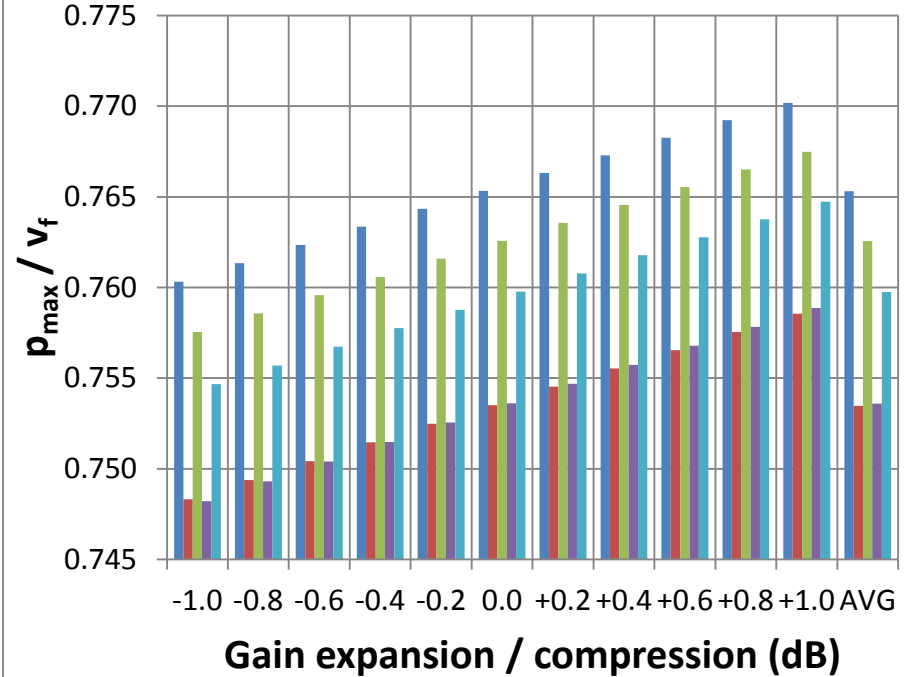
■ The ratio of p_{\max} to v_f is lower with $Z_c=110\Omega$ (#6,#8) than $Z_c=90\Omega$ (#7)

p_{\max} / v_f ($z_p=12\text{mm}, N_p=13$)



#1 Rd=45 Zc=90 #2 Rd=45 Zc=110 #3 Rd=55 Zc=90
#4 Rd=55 Zc=110 #9 Rd=50 Zc=100

p_{\max} / v_f ($z_p=30\text{mm}, N_p=13$)

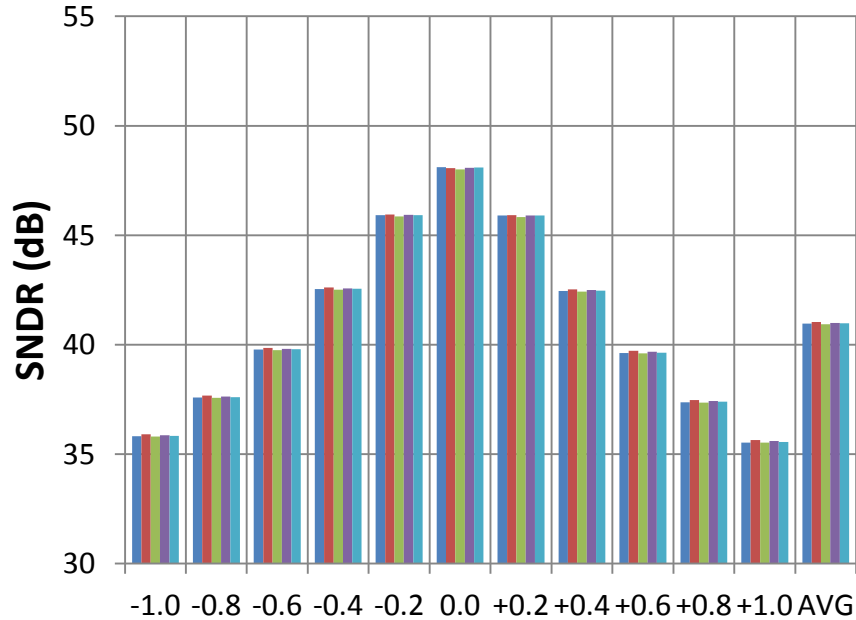


#5 Rd=45 Zc=90 #6 Rd=45 Zc=110 #7 Rd=55 Zc=90
#8 Rd=55 Zc=110 #10 Rd=50 Zc=100

Effect on SNDR (Np=13)

- The effect gets larger with $z_p=30\text{mm}$ (right graph)
 - SNDR is higher with $Z_c=110\Omega$ (#6,#8) than $Z_c=90\Omega$ (#7)

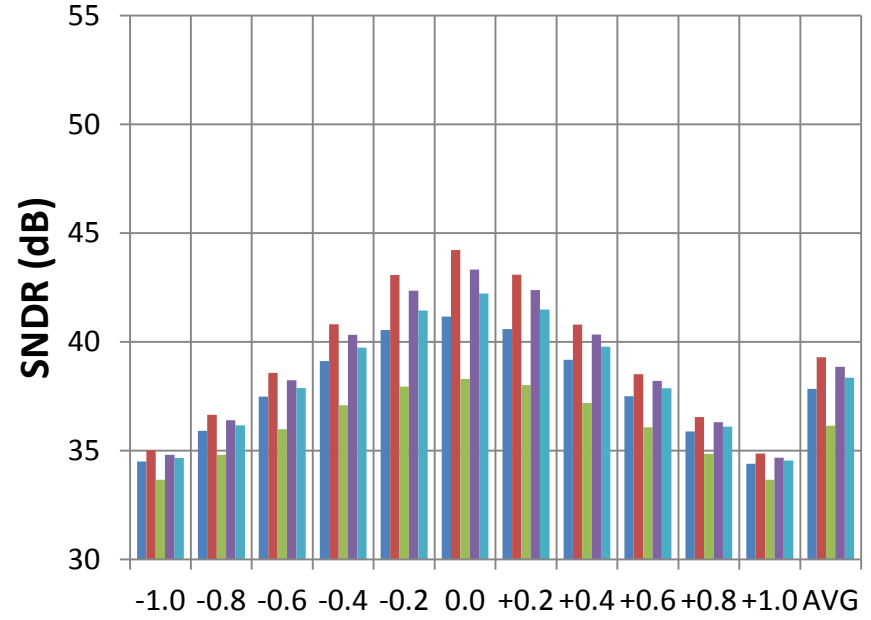
SNDR ($z_p=12\text{mm}$, $N_p=13$)



Gain expansion / compression (dB)

■ #1 Rd=45 Zc=90 ■ #2 Rd=45 Zc=110 ■ #3 Rd=55 Zc=90
■ #4 Rd=55 Zc=110 ■ #9 Rd=50 Zc=100

SNDR ($z_p=30\text{mm}$, $N_p=13$)



Gain expansion / compression (dB)

■ #5 Rd=45 Zc=90 ■ #6 Rd=45 Zc=110 ■ #7 Rd=55 Zc=90
■ #8 Rd=55 Zc=110 ■ #10 Rd=50 Zc=100

Result Table for the Ratio of p_{\max} to v_f

Ratio of Linear Fit Pulse Peak p_{\max} to Steady-State Voltage v_f (Dp=2, Np=200)											
Case	#1	#2	#3	#4	#5	#6	#7	#8	#9	#10	
zp	12				30				12	30	
Rd	45		55		45		55		50	50	
Zc	90	110	90	110	90	110	90	110	100	100	
Gain expansion / compression (dB)	-1.0	0.8050	0.7958	0.7971	0.7951	0.7333	0.7254	0.7265	0.7245	0.8001	0.7292
	-0.8	0.8056	0.7963	0.7977	0.7957	0.7342	0.7263	0.7274	0.7255	0.8007	0.7301
	-0.6	0.8061	0.7969	0.7983	0.7964	0.7351	0.7272	0.7283	0.7264	0.8012	0.7310
	-0.4	0.8066	0.7975	0.7989	0.7970	0.7360	0.7280	0.7292	0.7273	0.8018	0.7319
	-0.2	0.8071	0.7981	0.7994	0.7976	0.7369	0.7289	0.7301	0.7283	0.8023	0.7328
	0.0	0.8076	0.7986	0.8000	0.7982	0.7377	0.7298	0.7309	0.7292	0.8029	0.7336
	0.2	0.8082	0.7992	0.8005	0.7988	0.7386	0.7307	0.7318	0.7301	0.8034	0.7345
	0.4	0.8086	0.7997	0.8011	0.7993	0.7395	0.7316	0.7327	0.7310	0.8039	0.7354
	0.6	0.8091	0.8003	0.8016	0.7999	0.7403	0.7324	0.7336	0.7319	0.8045	0.7363
	0.8	0.8096	0.8008	0.8022	0.8005	0.7412	0.7333	0.7345	0.7328	0.8050	0.7371
1.0	0.8101	0.8013	0.8027	0.8011	0.7420	0.7341	0.7353	0.7338	0.8055	0.7380	
Average	0.8076	0.7986	0.7999	0.7981	0.7377	0.7298	0.7309	0.7292	0.8028	0.7336	

Ratio of Linear Fit Pulse Peak p_{\max} to Steady-State Voltage v_f (Dp=2, Np=13)											
Case	#1	#2	#3	#4	#5	#6	#7	#8	#9	#10	
zp	12				30				12	30	
Rd	45		55		45		55		50	50	
Zc	90	110	90	110	90	110	90	110	100	100	
Gain expansion / compression (dB)	-1.0	0.8185	0.8091	0.8106	0.8084	0.7603	0.7483	0.7575	0.7482	0.8135	0.7547
	-0.8	0.8192	0.8098	0.8113	0.8092	0.7613	0.7494	0.7586	0.7493	0.8142	0.7557
	-0.6	0.8198	0.8105	0.8121	0.8099	0.7623	0.7504	0.7596	0.7504	0.8149	0.7567
	-0.4	0.8205	0.8112	0.8128	0.8106	0.7634	0.7515	0.7606	0.7515	0.8155	0.7578
	-0.2	0.8211	0.8119	0.8135	0.8113	0.7643	0.7525	0.7616	0.7525	0.8162	0.7588
	0.0	0.8218	0.8126	0.8141	0.8121	0.7653	0.7535	0.7626	0.7536	0.8169	0.7598
	0.2	0.8224	0.8133	0.8148	0.8128	0.7663	0.7545	0.7636	0.7547	0.8175	0.7608
	0.4	0.8230	0.8139	0.8155	0.8135	0.7673	0.7555	0.7646	0.7557	0.8182	0.7618
	0.6	0.8236	0.8146	0.8162	0.8142	0.7683	0.7565	0.7655	0.7568	0.8188	0.7628
	0.8	0.8242	0.8152	0.8168	0.8149	0.7692	0.7575	0.7665	0.7578	0.8195	0.7638
1.0	0.8248	0.8159	0.8175	0.8155	0.7702	0.7585	0.7675	0.7589	0.8201	0.7647	
Average	0.8217	0.8126	0.8141	0.8120	0.7653	0.7535	0.7626	0.7536	0.8168	0.7597	

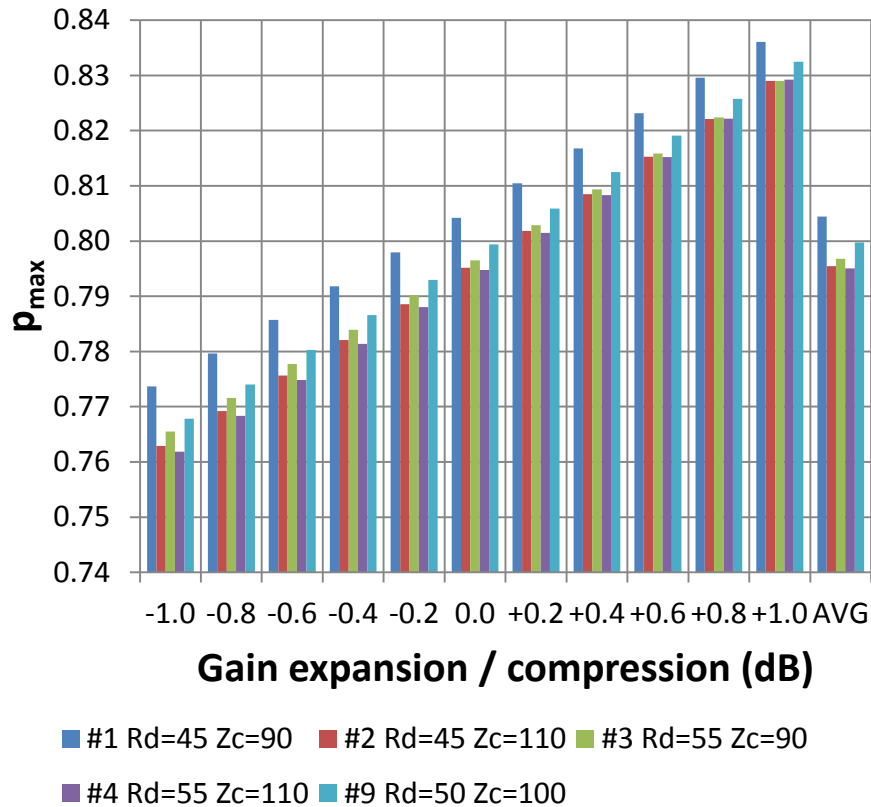
Result Table for SNDR

SNDR (Dp=2, Np=200)											
Case	#1	#2	#3	#4	#5	#6	#7	#8	#9	#10	
zp	12				30				12	30	
Rd	45		55		45		55		50	50	
Zc	90	110	90	110	90	110	90	110	100	100	
Gain expansion / compression (dB)	-1.0	35.91	36.01	35.90	35.95	35.44	35.43	35.44	35.33	35.93	35.37
	-0.8	37.73	37.83	37.72	37.77	37.27	37.26	37.27	37.17	37.75	37.21
	-0.6	40.01	40.10	40.00	40.05	39.58	39.57	39.58	39.48	40.02	39.52
	-0.4	42.99	43.08	42.98	43.03	42.62	42.61	42.61	42.53	43.01	42.56
	-0.2	46.96	47.02	46.96	46.99	46.72	46.72	46.72	46.67	46.98	46.69
	0.0	50.00	49.99	49.99	49.99	49.98	49.98	49.98	49.98	50.00	49.98
	0.2	46.92	46.98	46.92	46.96	46.69	46.69	46.69	46.64	46.94	46.66
	0.4	42.89	42.98	42.88	42.94	42.54	42.53	42.54	42.46	42.91	42.49
	0.6	39.83	39.94	39.83	39.90	39.46	39.45	39.46	39.37	39.86	39.40
	0.8	37.49	37.61	37.49	37.56	37.11	37.11	37.11	37.02	37.52	37.05
1.0	35.61	35.74	35.61	35.69	35.23	35.23	35.24	35.14	35.65	35.18	
Average	41.49	41.57	41.48	41.53	41.15	41.14	41.15	41.07	41.51	41.10	

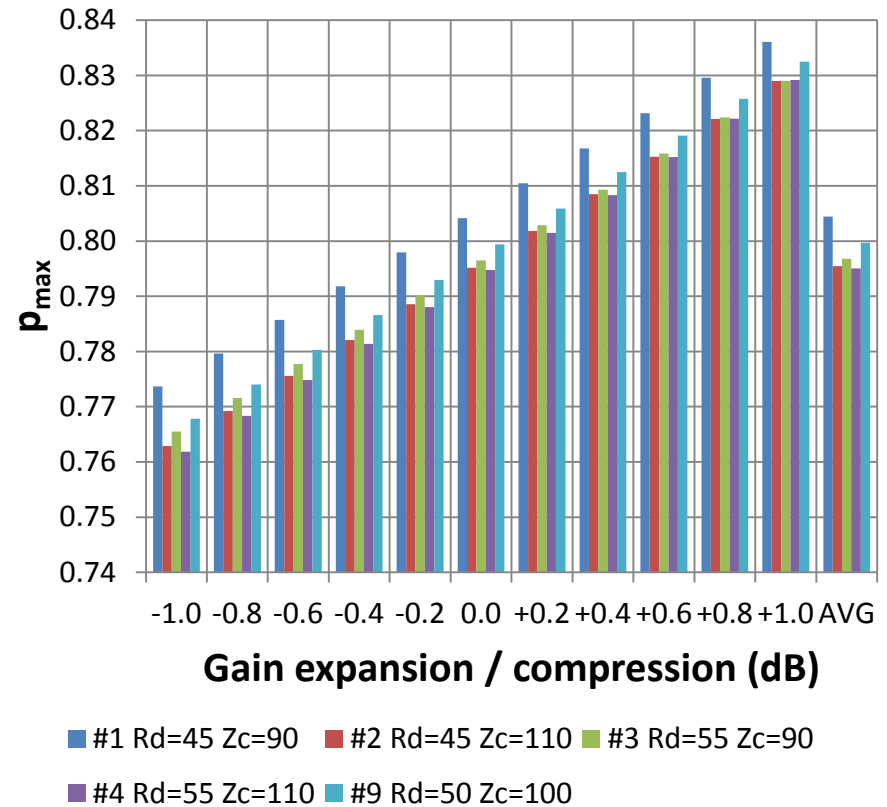
SNDR (Dp=2, Np=13)											
Case	#1	#2	#3	#4	#5	#6	#7	#8	#9	#10	
zp	12				30				12	30	
Rd	45		55		45		55		50	50	
Zc	90	110	90	110	90	110	90	110	100	100	
Gain expansion / compression (dB)	-1.0	35.82	35.91	35.80	35.86	34.49	35.01	33.65	34.80	35.83	34.66
	-0.8	37.59	37.68	37.57	37.63	35.91	36.65	34.80	36.39	37.60	36.17
	-0.6	39.77	39.86	39.75	39.81	37.48	38.57	35.98	38.24	39.79	37.88
	-0.4	42.54	42.61	42.51	42.57	39.12	40.81	37.09	40.32	42.55	39.74
	-0.2	45.92	45.94	45.86	45.92	40.54	43.08	37.94	42.35	45.92	41.44
	0.0	48.11	48.07	48.01	48.08	41.17	44.22	38.29	43.33	48.09	42.23
	0.2	45.90	45.92	45.84	45.90	40.59	43.10	38.01	42.38	45.90	41.49
	0.4	42.45	42.53	42.42	42.49	39.18	40.80	37.19	40.33	42.47	39.77
	0.6	39.62	39.71	39.60	39.67	37.50	38.52	36.07	38.21	39.64	37.87
	0.8	37.36	37.47	37.36	37.43	35.88	36.54	34.85	36.31	37.39	36.11
1.0	35.53	35.65	35.52	35.60	34.40	34.86	33.66	34.68	35.56	34.54	
Average	40.96	41.03	40.93	41.00	37.84	39.29	36.14	38.85	40.98	38.35	

Result of p_{\max} (zp=12mm)

p_{\max} (zp=12mm, Np=200)

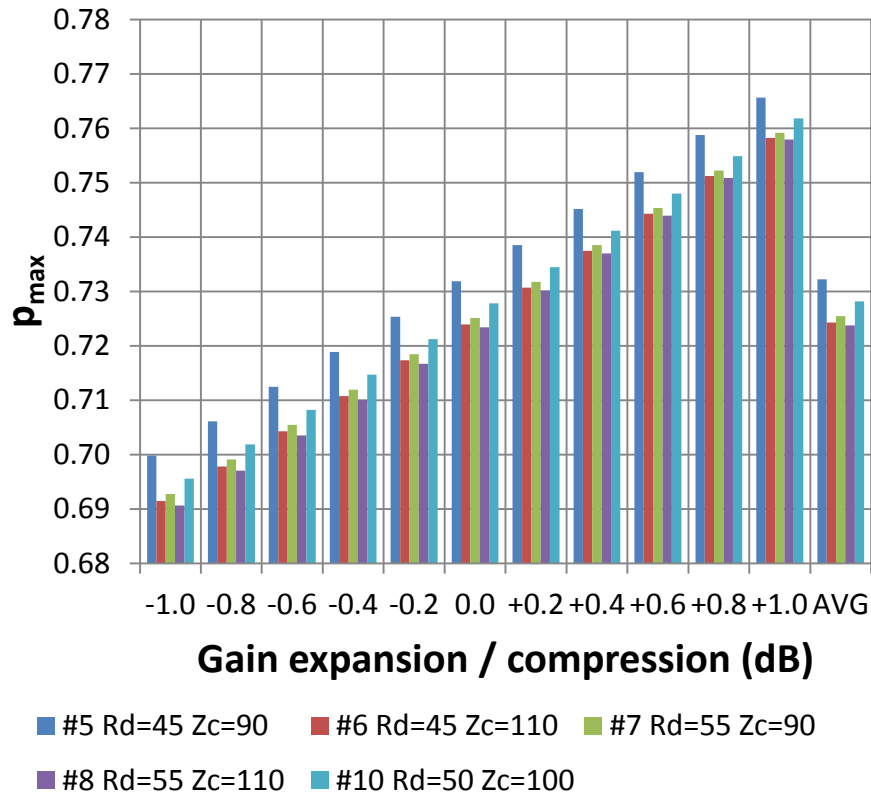


p_{\max} (zp=12mm, Np=13)

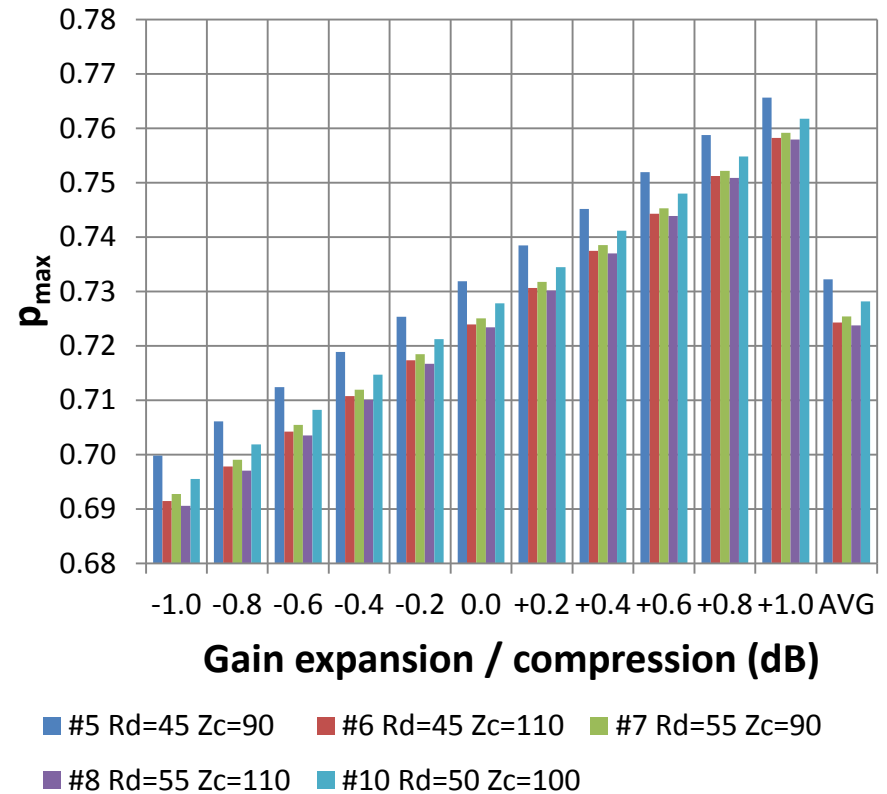


Result of p_{\max} ($z_p=30\text{mm}$)

p_{\max} ($z_p=30\text{mm}$, $N_p=200$)



p_{\max} ($z_p=30\text{mm}$, $N_p=13$)



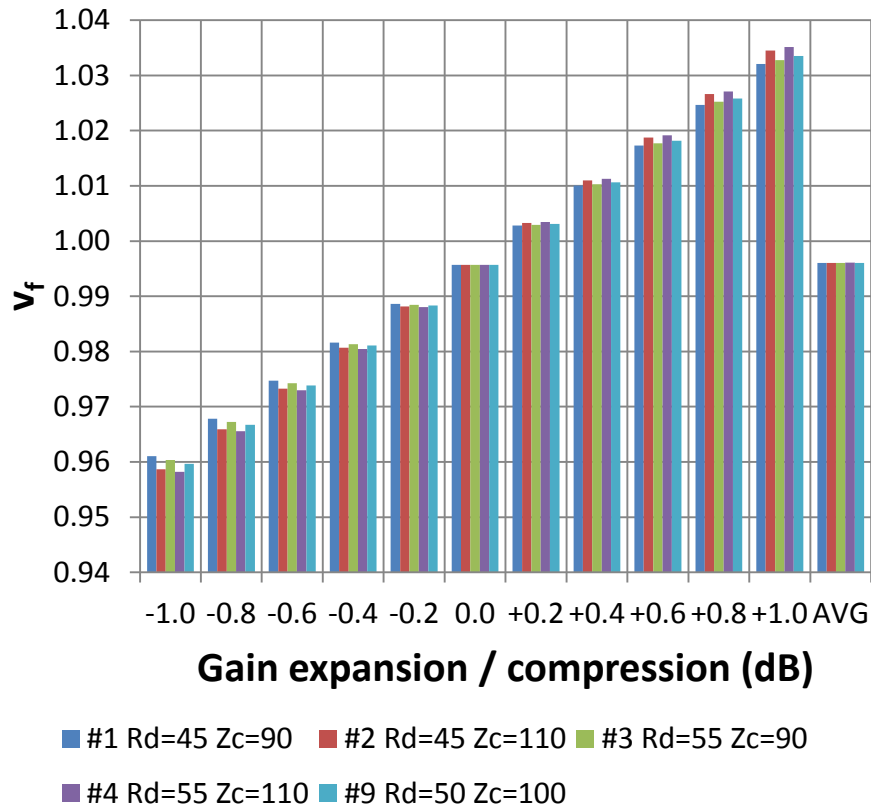
Result Table for p_{\max}

Linear Fit Pulse Peak p_{\max} (Dp=2, Np=200)											
Case	#1	#2	#3	#4	#5	#6	#7	#8	#9	#10	
zp	12				30				12	30	
Rd	45		55		45		55		50	50	
Zc	90	110	90	110	90	110	90	110	100	100	
Gain expansion / compression (dB)	-1.0	0.7737	0.7629	0.7655	0.7619	0.6998	0.6915	0.6928	0.6906	0.7678	0.6956
	-0.8	0.7797	0.7692	0.7716	0.7683	0.7061	0.6978	0.6991	0.6970	0.7740	0.7019
	-0.6	0.7857	0.7756	0.7777	0.7748	0.7124	0.7043	0.7055	0.7035	0.7803	0.7083
	-0.4	0.7918	0.7821	0.7839	0.7814	0.7189	0.7108	0.7120	0.7101	0.7866	0.7147
	-0.2	0.7980	0.7886	0.7902	0.7880	0.7253	0.7173	0.7185	0.7167	0.7930	0.7212
	0.0	0.8042	0.7952	0.7965	0.7947	0.7319	0.7240	0.7251	0.7234	0.7994	0.7278
	0.2	0.8105	0.8018	0.8029	0.8015	0.7385	0.7307	0.7318	0.7302	0.8059	0.7345
	0.4	0.8168	0.8085	0.8093	0.8083	0.7452	0.7375	0.7385	0.7370	0.8125	0.7412
	0.6	0.8232	0.8153	0.8158	0.8152	0.7519	0.7443	0.7453	0.7439	0.8191	0.7480
	0.8	0.8296	0.8221	0.8224	0.8222	0.7588	0.7512	0.7522	0.7509	0.8258	0.7549
1.0	0.8361	0.8290	0.8290	0.8292	0.7657	0.7582	0.7592	0.7580	0.8325	0.7618	
Average	0.8045	0.7955	0.7968	0.7951	0.7322	0.7243	0.7254	0.7238	0.7997	0.7282	

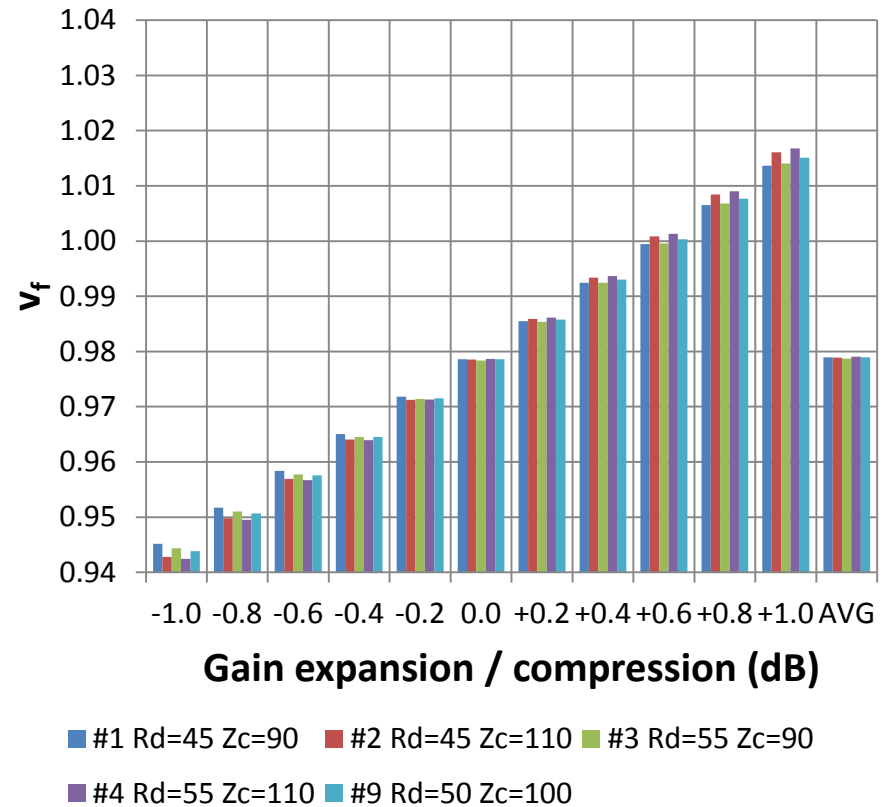
Linear Fit Pulse Peak p_{\max} (Dp=2, Np=13)											
Case	#1	#2	#3	#4	#5	#6	#7	#8	#9	#10	
zp	12				30				12	30	
Rd	45		55		45		55		50	50	
Zc	90	110	90	110	90	110	90	110	100	100	
Gain expansion / compression (dB)	-1.0	0.7737	0.7629	0.7655	0.7619	0.6998	0.6915	0.6927	0.6906	0.7678	0.6955
	-0.8	0.7797	0.7692	0.7716	0.7683	0.7061	0.6978	0.6991	0.6970	0.7740	0.7019
	-0.6	0.7857	0.7756	0.7777	0.7748	0.7124	0.7043	0.7055	0.7035	0.7803	0.7082
	-0.4	0.7918	0.7821	0.7839	0.7814	0.7189	0.7108	0.7119	0.7101	0.7866	0.7147
	-0.2	0.7980	0.7886	0.7902	0.7880	0.7253	0.7173	0.7185	0.7167	0.7930	0.7212
	0.0	0.8042	0.7952	0.7965	0.7947	0.7319	0.7240	0.7251	0.7234	0.7994	0.7278
	0.2	0.8104	0.8018	0.8029	0.8015	0.7385	0.7307	0.7318	0.7302	0.8059	0.7345
	0.4	0.8168	0.8085	0.8093	0.8083	0.7452	0.7375	0.7385	0.7370	0.8125	0.7412
	0.6	0.8232	0.8153	0.8158	0.8152	0.7519	0.7443	0.7453	0.7439	0.8191	0.7480
	0.8	0.8296	0.8221	0.8224	0.8222	0.7588	0.7512	0.7522	0.7509	0.8258	0.7549
1.0	0.8361	0.8290	0.8290	0.8292	0.7657	0.7582	0.7592	0.7580	0.8325	0.7618	
Average	0.8045	0.7955	0.7968	0.7951	0.7322	0.7243	0.7254	0.7237	0.7997	0.7281	

Result of v_f ($z_p=12\text{mm}$)

v_f ($z_p=12\text{mm}$, $N_p=200$)

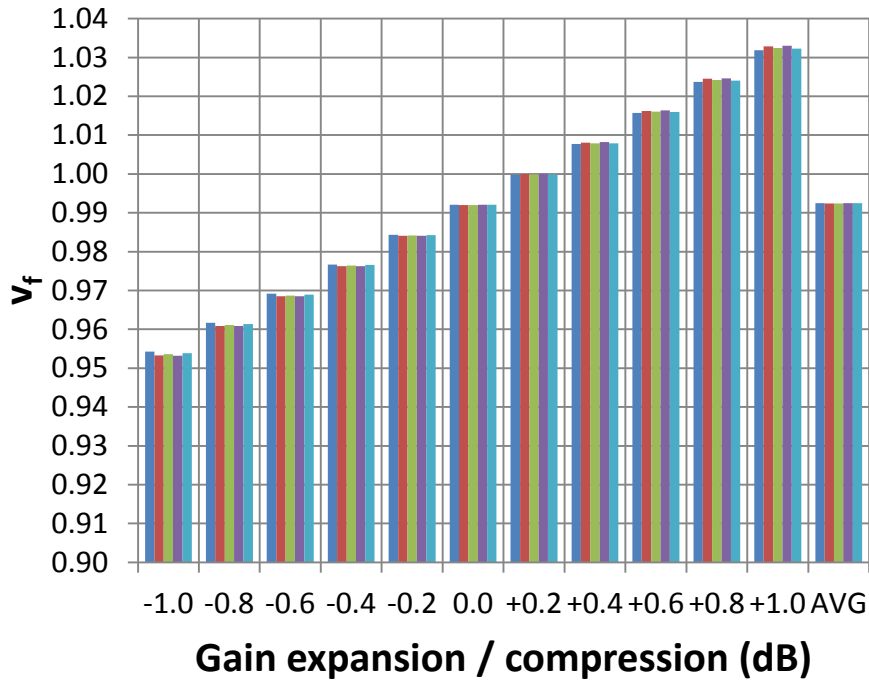


v_f ($z_p=12\text{mm}$, $N_p=13$)



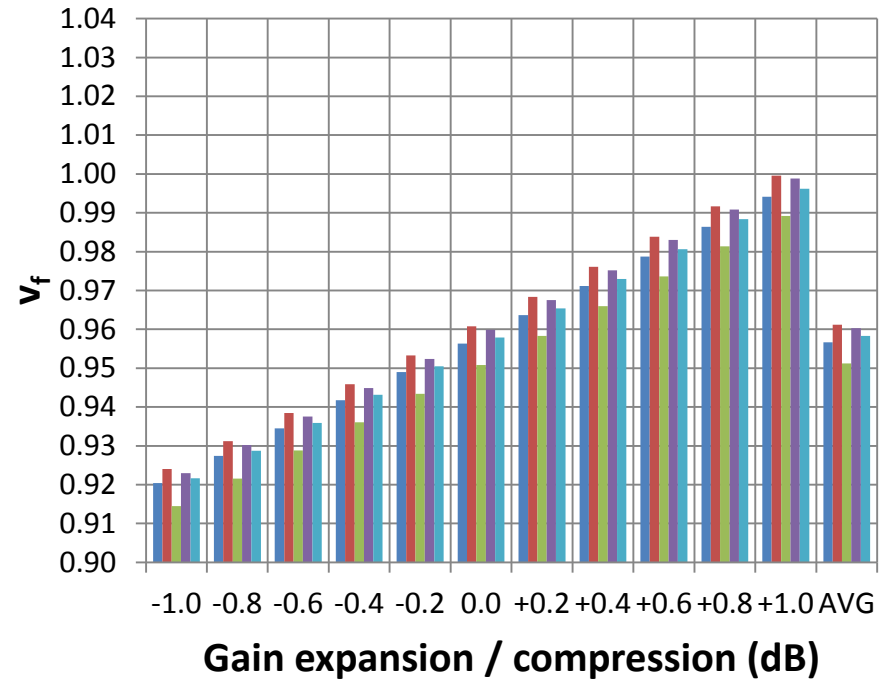
Result of v_f ($z_p=30\text{mm}$)

v_f ($z_p=30\text{mm}$, $N_p=200$)



■ #5 Rd=45 Zc=90 ■ #6 Rd=45 Zc=110 ■ #7 Rd=55 Zc=90
■ #8 Rd=55 Zc=110 ■ #10 Rd=50 Zc=100

v_f ($z_p=30\text{mm}$, $N_p=13$)



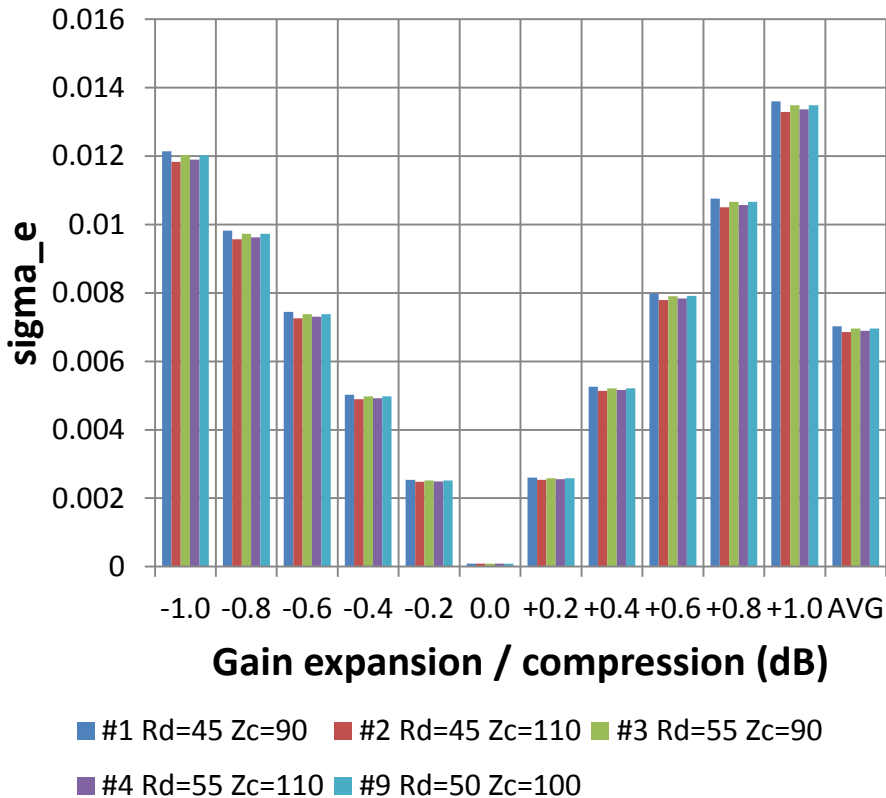
■ #5 Rd=45 Zc=90 ■ #6 Rd=45 Zc=110 ■ #7 Rd=55 Zc=90
■ #8 Rd=55 Zc=110 ■ #10 Rd=50 Zc=100

Result Table for v_f

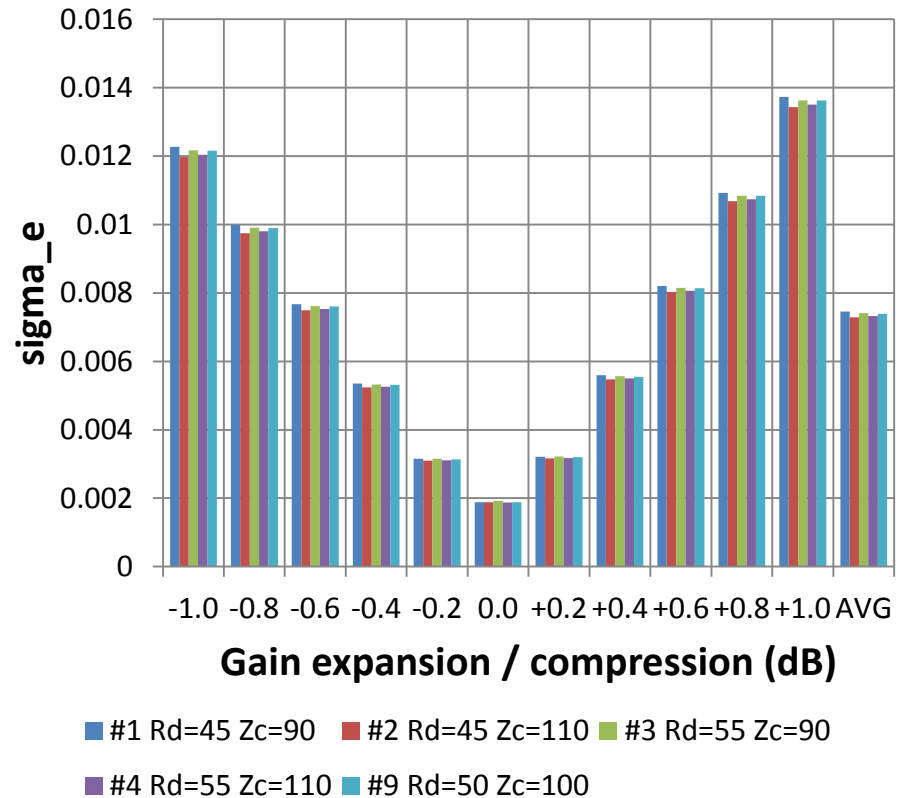
Steady-State Voltage v_f (Dp=2, Np=200)												
Case	#1	#2	#3	#4	#5	#6	#7	#8	#9	#10		
zp	12				30				12	30		
Rd	45		55		45		55		50	50		
Zc	90	110	90	110	90	110	90	110	100	100		
Gain expansion / compression (dB)	-1.0	0.9610	0.9587	0.9603	0.9582	0.9543	0.9533	0.9536	0.9532	0.9597	0.9539	
	-0.8	0.9678	0.9659	0.9673	0.9655	0.9617	0.9608	0.9611	0.9608	0.9667	0.9614	
	-0.6	0.9747	0.9733	0.9743	0.9730	0.9692	0.9685	0.9687	0.9685	0.9739	0.9689	
	-0.4	0.9816	0.9807	0.9813	0.9805	0.9767	0.9763	0.9764	0.9763	0.9811	0.9765	
	-0.2	0.9886	0.9881	0.9885	0.9881	0.9843	0.9841	0.9841	0.9841	0.9884	0.9843	
	0.0	0.9957	0.9957	0.9957	0.9957	0.9921	0.9920	0.9920	0.9920	0.9921	0.9957	0.9921
	0.2	1.0028	1.0033	1.0030	1.0034	0.9999	1.0000	0.9999	1.0001	1.0031	0.9999	
	0.4	1.0101	1.0110	1.0103	1.0112	1.0077	1.0081	1.0079	1.0082	1.0106	1.0079	
	0.6	1.0173	1.0188	1.0177	1.0191	1.0157	1.0162	1.0160	1.0164	1.0182	1.0159	
	0.8	1.0247	1.0266	1.0252	1.0271	1.0237	1.0245	1.0242	1.0246	1.0258	1.0241	
1.0	1.0321	1.0345	1.0328	1.0351	1.0318	1.0328	1.0324	1.0330	1.0335	1.0323		
Average	0.9960	0.9961	0.9960	0.9961	0.9925	0.9924	0.9924	0.9925	0.9961	0.9925		
Steady-State Voltage v_f (Dp=2, Np=13)												
Case	#1	#2	#3	#4	#5	#6	#7	#8	#9	#10		
zp	12				30				12	30		
Rd	45		55		45		55		50	50		
Zc	90	110	90	110	90	110	90	110	100	100		
Gain expansion / compression (dB)	-1.0	0.9452	0.9428	0.9443	0.9424	0.9204	0.9240	0.9145	0.9230	0.9439	0.9217	
	-0.8	0.9517	0.9498	0.9510	0.9495	0.9274	0.9312	0.9216	0.9302	0.9507	0.9288	
	-0.6	0.9584	0.9569	0.9577	0.9567	0.9345	0.9385	0.9288	0.9375	0.9576	0.9359	
	-0.4	0.9650	0.9640	0.9645	0.9640	0.9417	0.9458	0.9361	0.9449	0.9645	0.9432	
	-0.2	0.9718	0.9713	0.9714	0.9713	0.9490	0.9533	0.9434	0.9523	0.9715	0.9505	
	0.0	0.9786	0.9786	0.9784	0.9787	0.9563	0.9608	0.9508	0.9599	0.9786	0.9579	
	0.2	0.9855	0.9859	0.9854	0.9861	0.9637	0.9684	0.9583	0.9675	0.9858	0.9654	
	0.4	0.9924	0.9934	0.9924	0.9937	0.9712	0.9761	0.9659	0.9752	0.9930	0.9730	
	0.6	0.9994	1.0009	0.9996	1.0013	0.9788	0.9838	0.9736	0.9830	1.0003	0.9806	
	0.8	1.0065	1.0084	1.0068	1.0090	0.9864	0.9917	0.9813	0.9909	1.0077	0.9883	
1.0	1.0137	1.0161	1.0141	1.0168	0.9941	0.9996	0.9892	0.9988	1.0151	0.9962		
Average	0.9789	0.9789	0.9787	0.9790	0.9567	0.9612	0.9512	0.9603	0.9790	0.9583		

Result of σ_e (zp=12mm)

sigma_e (zp=12mm, Np=200)

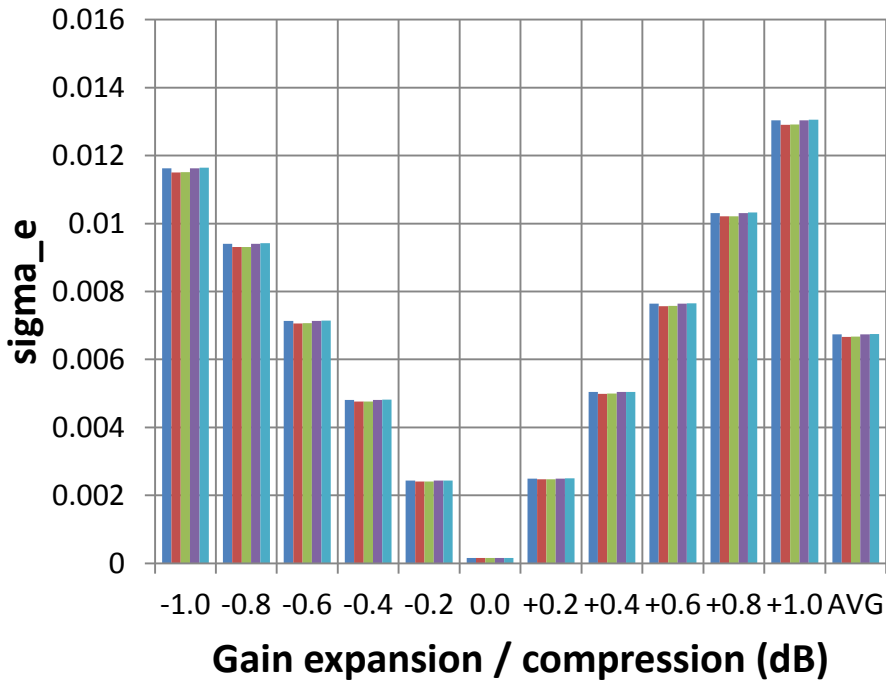


sigma_e (zp=12mm, Np=13)



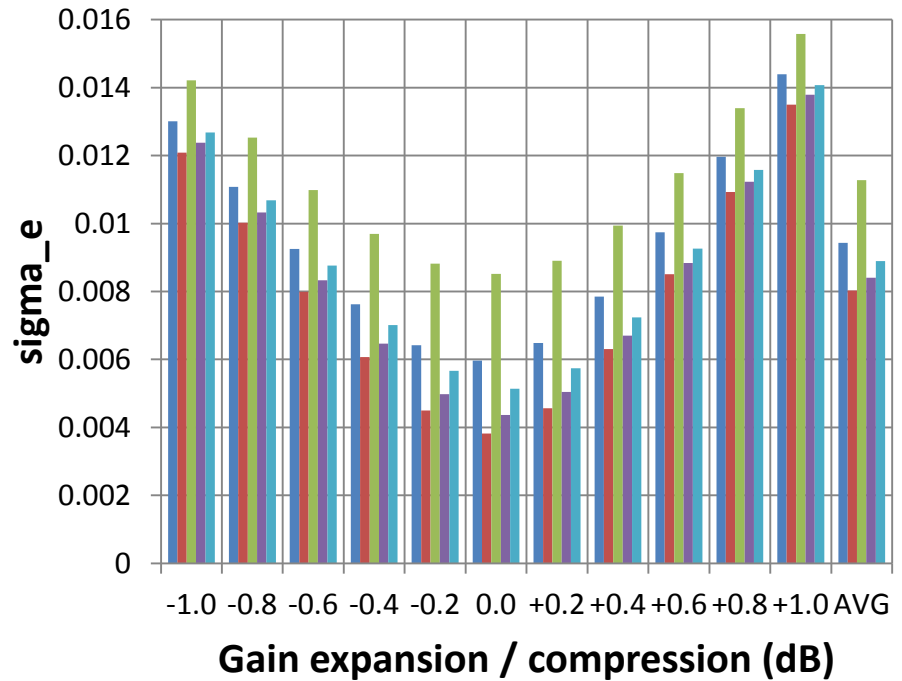
Result of σ_e (zp=30mm)

sigma_e (zp=30mm, Np=200)



#5 Rd=45 Zc=90 #6 Rd=45 Zc=110 #7 Rd=55 Zc=90
 #8 Rd=55 Zc=110 #10 Rd=50 Zc=100

sigma_e (zp=30mm, Np=13)



#5 Rd=45 Zc=90 #6 Rd=45 Zc=110 #7 Rd=55 Zc=90
 #8 Rd=55 Zc=110 #10 Rd=50 Zc=100

Result Table for σ_e

sigma_e (Dp=2, Np=200)											
Case	#1	#2	#3	#4	#5	#6	#7	#8	#9	#10	
zp	12				30				12	30	
Rd	45		55		45		55		50	50	
Zc	90	110	90	110	90	110	90	110	100	100	
Gain expansion / compression (dB)	-1.0	1.21E-02	1.18E-02	1.20E-02	1.19E-02	1.16E-02	1.15E-02	1.15E-02	1.16E-02	1.20E-02	1.16E-02
	-0.8	9.82E-03	9.57E-03	9.73E-03	9.63E-03	9.40E-03	9.31E-03	9.31E-03	9.40E-03	9.73E-03	9.42E-03
	-0.6	7.45E-03	7.26E-03	7.38E-03	7.30E-03	7.13E-03	7.06E-03	7.06E-03	7.13E-03	7.38E-03	7.14E-03
	-0.4	5.02E-03	4.90E-03	4.98E-03	4.93E-03	4.81E-03	4.76E-03	4.76E-03	4.81E-03	4.98E-03	4.82E-03
	-0.2	2.54E-03	2.48E-03	2.52E-03	2.49E-03	2.43E-03	2.41E-03	2.41E-03	2.43E-03	2.52E-03	2.44E-03
	0.0	8.56E-05	8.61E-05	8.62E-05	8.56E-05	1.54E-04	1.56E-04	1.56E-04	1.54E-04	8.56E-05	1.54E-04
	0.2	2.60E-03	2.54E-03	2.58E-03	2.55E-03	2.50E-03	2.47E-03	2.47E-03	2.50E-03	2.58E-03	2.50E-03
	0.4	5.26E-03	5.13E-03	5.21E-03	5.16E-03	5.04E-03	4.99E-03	4.99E-03	5.04E-03	5.21E-03	5.05E-03
	0.6	7.98E-03	7.79E-03	7.91E-03	7.84E-03	7.64E-03	7.57E-03	7.57E-03	7.65E-03	7.91E-03	7.66E-03
	0.8	1.08E-02	1.05E-02	1.07E-02	1.06E-02	1.03E-02	1.02E-02	1.02E-02	1.03E-02	1.07E-02	1.03E-02
1.0	1.36E-02	1.33E-02	1.35E-02	1.34E-02	1.30E-02	1.29E-02	1.29E-02	1.30E-02	1.35E-02	1.31E-02	
Average	7.02E-03	6.85E-03	6.96E-03	6.89E-03	6.73E-03	6.67E-03	6.67E-03	6.73E-03	6.96E-03	6.74E-03	

sigma_e (Dp=2, Np=13)											
Case	#1	#2	#3	#4	#5	#6	#7	#8	#9	#10	
zp	12				30				12	30	
Rd	45		55		45		55		50	50	
Zc	90	110	90	110	90	110	90	110	100	100	
Gain expansion / compression (dB)	-1.0	1.23E-02	1.20E-02	1.22E-02	1.20E-02	1.30E-02	1.21E-02	1.42E-02	1.24E-02	1.22E-02	1.27E-02
	-0.8	9.99E-03	9.75E-03	9.91E-03	9.80E-03	1.11E-02	1.00E-02	1.25E-02	1.03E-02	9.90E-03	1.07E-02
	-0.6	7.67E-03	7.49E-03	7.62E-03	7.53E-03	9.25E-03	7.99E-03	1.10E-02	8.33E-03	7.61E-03	8.76E-03
	-0.4	5.35E-03	5.24E-03	5.32E-03	5.26E-03	7.62E-03	6.07E-03	9.70E-03	6.47E-03	5.31E-03	7.01E-03
	-0.2	3.15E-03	3.10E-03	3.16E-03	3.11E-03	6.42E-03	4.49E-03	8.82E-03	4.98E-03	3.13E-03	5.67E-03
	0.0	1.88E-03	1.88E-03	1.92E-03	1.87E-03	5.97E-03	3.82E-03	8.52E-03	4.37E-03	1.88E-03	5.14E-03
	0.2	3.21E-03	3.17E-03	3.22E-03	3.17E-03	6.49E-03	4.56E-03	8.91E-03	5.05E-03	3.20E-03	5.74E-03
	0.4	5.59E-03	5.48E-03	5.56E-03	5.50E-03	7.85E-03	6.31E-03	9.94E-03	6.70E-03	5.55E-03	7.24E-03
	0.6	8.20E-03	8.02E-03	8.14E-03	8.06E-03	9.74E-03	8.51E-03	1.15E-02	8.84E-03	8.14E-03	9.26E-03
	0.8	1.09E-02	1.07E-02	1.08E-02	1.07E-02	1.20E-02	1.09E-02	1.34E-02	1.12E-02	1.08E-02	1.16E-02
1.0	1.37E-02	1.34E-02	1.36E-02	1.35E-02	1.44E-02	1.35E-02	1.56E-02	1.38E-02	1.36E-02	1.41E-02	
Average	7.45E-03	7.29E-03	7.41E-03	7.33E-03	9.43E-03	8.03E-03	1.13E-02	8.40E-03	7.39E-03	8.89E-03	

Thank you