## BASE-AU 980nm/OM3 baseline Reference receiver and

 transmitter and distortion figure of meritRubén Pérez-Aranda, KDPOF

- This contribution proposes a reference receiver and a figure of merit of transmitter and distortion (TDFOM) assessment for the BASE-AU PHY based on 980nm and OM3
- Reference receiver and TDFOM are defined to reflect the most representative receiver implementation, which is consistent with the receiver implementation used in the link budget assessment and the definition of TX/RX characteristics
- Definition of the reference receiver as well as TDFOM has as objective to guarantee the interoperability of different implementations
- TDFOM will be used as part of the transmitter characteristics specification
- TDFOM will be used to define stress receiver sensitivity conditions


## Introduction to reference receivers and signal quality analysis

## Intro to reference RX and analysis - general



- PMD TX generates a pseudo-random periodic pattern with a determined length, modulation format, baseline and clock wander characteristics
- The optical splitter and variable reflector are adjusted so that each transmitter is tested with an optical return loss equal to the max value specified
- A O/E converter is used to receive optical signal generated by PMD TX under test and convert it into electrical domain
- O/E is usually integrated within CRU and oscilloscope equipments
- A CRU (clock recovery unit) is used to generate a low jitter clock locked in phase to PMD TX signal. The CRU OJTF (observed jitter transfer function) needs to be specified according to the communications system specifications
- Pattern triggered oscilloscope is used to capture the full signal pattern with given samples per unit interval
- Equivalent response of O/E plus oscilloscope is specified in terms of a low pass filter type and order as well as its -3dB bandwidth
- It is usual BT4 (Bessel-Thomson 4th order low pass) filters with specified bandwidth, e.g. BW-3dB $\sim 0.7 / T_{s}$, being Ts the nominal symbol period
- BT4 filters are convenient for eye analysis because good tradeoff between rejection and passband linear phase and HW implementation
- Reference receiver and signal quality analysis (e.g. TDEC, TDECQ) is defined to reflect the most representative receiver IC implementation, for sake of interoperability and not precluding different implementations
- Quality analysis determines the amount of noise to be added to the signal so measured BER is equal to the specification limit


## Intro to reference RX and analysis - e.g. TDEC

25GBASE-SR reference RX and analysis is inspired on possible PHY IC RX implementations

Symbol error rate is evaluated with histograms in the 2 sampling times for 1 threshold, i.e. Pave


- At least 2 comparators in the lower and upper side, left and right, for clock recovery

- 1 extra comparator in Pave, for data recovery 2 separate sampling times
needed for clock recovery
- 10 comparisons per symbol


## Intro to reference RX and analysis - e.g. TDECQ

## 50GBASE-SR reference RX and analysis is inspired on possible PHY IC RX implementations



Actually, 2 EQ filters are implemented in IC, one for each sampling time

## Pros:

- FIR filter implementation in analog domain
- Very efficient in terms of speed/power tradeoff


## Cons:

- Tap coefficients adaptation is difficult in IC implementation
- Linear EQ is sub-optimum in terms of channel capacity due to the noise autocorrelation and enhancement produced by the FIR filter (vs capacity approaching MMSE-DFE, u), [1, 2, 3]
- Unable to deal with strong non-linearities


## The reference receiver - e.g. TDECQ vs TDFOM

TDECQ cannot be calculated for the output signal of TDECQ EQ


TDFOM receiver is able to deal with non linear ISI

Comparison of TDECQ equalizer performance vs TDFOM receiver performance, both doing processing of VCSEL signal operating at $\mathrm{T}_{\mathrm{BS}}=125^{\circ} \mathrm{C}, 26.88$ GBd, PAM4

## Specification of BASE-AU 980nm/OM3 reference receiver and analysis

## BASE-AU 980nm/OM3 reference receiver and analysis



## Fiber modelling: BT4 vs Gauss response



- Both filters, Gaussian and BT4, present linear phase response in the passband
- Both filters are compared in magnitude for the same electrical $B W-3 \mathrm{~dB}=16.4 \mathrm{GHz}$

- Considerations for BW calculation:
- $\mathrm{EMB}=945 \mathrm{MHz} \cdot \mathrm{km}$
- $\mathrm{BWcd}=5498 \mathrm{MHz} \cdot \mathrm{km}$
- BWeff $=931 \mathrm{MHz} \cdot \mathrm{km}$
- $931 / 40 /$ sqrt(2) $=16.4 \mathrm{GHz}$ (electrical bandwidth, assuming gaussian response)


## BASE-AU 980nm/OM3 reference receiver and analysis

- The input low pass filter shall be $4^{\text {th }}$ order Bessel-Thomson with BW-3dB $=$ 16.4 GHz
- Acquisition oversampling (samples per unit interval) shall be, Ov > 15
- Waveform averaging shall be enabled to eliminate noise; averaging factor shall be selected high enough to avoid noise affecting the TDFOM analysis (error below 0.05 dB )
- Filters shall be scaled according to symbol period and modulation format as:

$$
\begin{array}{ll}
f_{1}=\frac{1}{10 \cdot T_{S}}+5 \cdot 10^{8}(\mathrm{~Hz}) ; & f_{2}=\left\{\begin{array}{cc}
\frac{1}{5 \cdot T_{S}}, & \mathrm{NRZ} \\
\frac{1}{3 \cdot T_{S}}, & \text { PAM } 4
\end{array} ;\right. \\
f_{3}=\frac{1}{2 \cdot T_{S}} ; & f_{4}=\left\{\begin{array}{cc}
\infty, & \mathrm{NRZ} \\
\frac{1}{2 \cdot T_{S}}, & \text { PAM } 4
\end{array}\right.
\end{array}
$$

## BASE-AU 980nm/OM3 reference receiver and analysis

- MMSE-DFE filters are defined as:

$$
G(z)=\sum_{i=0}^{N_{\sigma^{\sigma}}-1} g_{i} \cdot z^{-i} ; B(z)=1+\sum_{i=1}^{N_{k}-1} b_{i} \cdot z^{-i} ;
$$

- Equalizer DC gain is calculated as:

$$
G_{e q}=\left|\frac{\sum_{i=0}^{N_{G}-1} g_{i}}{1+\sum_{i=1}^{N_{B}-1} b_{i}}\right|
$$

- Number of taps for each filter depends on bit rate:
- For $50 \mathrm{~Gb} / \mathrm{s}: \mathrm{N}_{\mathrm{G}}=8, \mathrm{~N}_{\mathrm{B}}=2$
- For $25 \mathrm{~Gb} / \mathrm{s}: \mathrm{NG}_{\mathrm{G}}=8, \mathrm{~N}_{\mathrm{B}}=3$
- For 2.5, 5, and $10 \mathrm{~Gb} / \mathrm{s}: \mathrm{N}_{\mathrm{G}}=4, \mathrm{~N}_{\mathrm{B}}=3$
- $G(z)$ and $B(z)$ shall be calculated to minimise the mean square error (MMSE) between signals $p$ and $w$, and sampler delay $\phi$ and $G(z)$ delay shall be optimised for minimum BER after equalisation at each value of $\sigma_{n_{i n}}$
- An iterative algorithm shall find the max value of $\sigma_{n_{i n}}$ so measured BER is equal to the specification limit $1.757 \cdot 10^{-4}$ (BER before FEC)
- $\sigma_{n_{i n}}$ is the standard deviation of the white gaussian noise sequence $n_{\text {in }}$
- $p$ is the periodic test pattern, that takes values $\{-1,+1\}$ for NRZ, and $\{-1,-1 / 3,1 / 3,1\}$ for PAM4


## BASE-AU 980nm/OM3 reference receiver and analysis

## - BER calculation:

- Calculate the noise sequence in the output of equaliser as $\mathrm{n}=\mathrm{w}$ - s
- Calculate the standard deviation $\sigma_{n}$
- Define the thresholds vector THv = [0] for NRZ, and THv = [-2/3, 0, +2/3] for PAM4
- Define $\mathrm{N}_{\text {th }}=1$ for NRZ, and $\mathrm{N}_{\text {th }}=3$ for PAM4
- Calculate the histogram of signal $s$, where the value of each bin $h(i)$ is normalised to relative probability, such that $h(i)=c(i) / N_{h}$, where $c(i)$ is the number of elements in the bin centred in $e(i)$ with width $\Delta e$, and $N_{h}$ is the number of elements of signal $s$
- $\Delta e=(\max (s)-\min (s)) / N_{h}$
- $N_{h}$ shall be $\geq 500$
- For each $T H v(k)$ :
- Calculate $i h_{p}$ as the bins that meet $e(i)>T H v(k)$
- Calculate $i h_{n}$ as the bins that meet $e(i) \leq T H v(k)$
- Calculate SER $_{\text {th }}(k)$ as:

$$
S E R_{t h}(k)=\frac{1}{2} \sum_{i=\min \left(i h_{n}\right)}^{\max \left(i h_{n}\right)} h(i) \cdot \operatorname{erfc}\left(\frac{T H v(k)-e(i)}{\sigma_{n} \sqrt{2}}\right)+\frac{1}{2} \sum_{i=\min \left(i h_{p}\right)}^{\max \left(\left(h_{p}\right)\right.} h(i) \cdot \operatorname{erfc}\left(\frac{e(i)-T H v(k)}{\sigma_{n} \sqrt{2}}\right)
$$

where $\operatorname{erfc}(x)$ is the complementary error function defined as:

$$
\operatorname{erfc}(x)=\frac{2}{\sqrt{\pi}} \int_{x}^{\infty} e^{-t^{2}} d t
$$

## BASE-AU 980nm/OM3 reference receiver and analysis

- Calculate the total SER as:

$$
\sum_{k=1}^{N_{k n}} S E R_{t h}(k)
$$

- Calculate BER as:
- BER = SER for NRZ,
- $B E R=S E R / 2$ for PAM4 (Gray mapping as in C/166 is considered)


## BASE-AU 980nm/OM3 reference receiver and analysis

- OMA calculation at EQ output:
- Define OMA eq as the OMA of signal s
- OMA shall be measured using continuous identical digits (CID)
- Search for positive CID as continuous samples of signal s with value $>0$, for NRZ, or with value $>2 / 3$, for PAM4
- Search for negative CID as continuous samples of signal s with value $<0$, for NRZ, or with value $<-2 / 3$, for PAM4
- CID sequence length shall be $\geq 14$ for NRZ, $\geq 7$ for PAM4
- For all the CID sequences that meet length constraint, remove:
- For NRZ: first 6 and last 6 samples
- For PAM4: first 3 and last 2 samples
- For the remaining symbols of all the CID sequences calculate the average value
- For positive CID sequences, we obtain OMAp
- For negative CID sequences, we obtain OMAn
- $\mathrm{OMA}_{\text {eq }}=O M A_{p}-O M A_{n}$
- OMA calculation at EQ input
- Calculate:

$$
O M A_{i n}=\frac{O M A_{e q}}{G_{e q}}
$$

## BASE-AU 980nm/OM3 reference receiver and analysis

- TX DC parameters calculation:
- Calculate transmitter OMA as:

$$
O M A_{t x}=O M A_{i n} \cdot \beta \quad \text { (watts) }
$$

- Calculate transmitter AOP as:

$$
A O P_{t x}=\alpha \quad \text { (watts) }
$$

- Calculate transmitter extinction ratio:

$$
\begin{equation*}
E R_{t x}=10 \log _{10}\left(\frac{O M A_{p} \cdot \beta+G_{e q} \cdot \alpha}{O M A_{n} \cdot \beta+G_{e q} \cdot \alpha}\right) \tag{dB}
\end{equation*}
$$

- Calculate OMA to AOP ratio as:

$$
\Gamma_{t x}=\frac{O M A_{t x}}{A O P_{t x}}=\frac{O M A_{i n} \cdot \beta}{\alpha}
$$

## BASE-AU 980nm/OM3 reference receiver and analysis

- TDFOM calculation
- Define reference Q-factor $Q_{0}$ as:
- $Q_{0}=3.5741$ for NRZ, consistent with $B E R=1.757 \cdot 10^{-4}$
- $Q_{0}=3.4981$ for PAM4, consistent with $B E R=1.757 \cdot 10^{-4}$
- Calculate transmitter and distortion figure of merit (TDFOM) as:

$$
T D F O M=10 \cdot \log _{10}\left(\frac{O M A_{i n} \sqrt{O v}}{2(M-1) \sigma_{n_{i n}} Q_{0}}\right)-\text { TDFOM }_{0}
$$

where $M=2$ for NRZ, and $M=4$ for PAM4.

- TDFOM is calculated to get TDFOM $=0 \mathrm{~dB}$ when an ideal transmitter (square pulse) is connected to the reference receiver
- It depends on bit-rate:
- For $50 \mathrm{~Gb} / \mathrm{s}$ : TDFOM $_{0}=4.47 \mathrm{~dB}$
- For $25 \mathrm{~Gb} / \mathrm{s}$ : $\mathrm{TDFOM}_{0}=4.27 \mathrm{~dB}$
- For $10 \mathrm{~Gb} / \mathrm{s}:$ TDFOM $_{0}=3.29 \mathrm{~dB}$
- For $5 \mathrm{~Gb} / \mathrm{s}: \mathrm{TDFOM}_{0}=2.59 \mathrm{~dB}$
- For $2.5 \mathrm{~Gb} / \mathrm{s}$ : $\mathrm{TDFOM}_{0}=1.84 \mathrm{~dB}$
- TDFOM ${ }_{0}$ values are obtained by simulation connecting a square pulse transmitter to the reference receiver input


## BASE-AU 980nm/OM3 reference receiver and analysis

-Why $\sqrt{o_{v}}$ factor?

- Noise $\mathrm{n}_{\text {in }}$ is added in a point of the signal processing path were signal is sampled a rate of $\frac{O v}{T_{s}}$
- The noise added is gaussian and white. Therefore, $\sigma_{n_{m}}^{2}=S_{n_{m}}^{2} \frac{O v}{2 \cdot T_{s}}$, where time domain power $\sigma_{n_{m}}^{2}$ relates with the single-sideband power spectral density $S_{n_{m}}^{2}$ by means of the sampling frequency $\frac{O v}{T_{s}}$
- After noise addition, $\mathrm{H}_{2}, \mathrm{H}_{3}$ and $\mathrm{H}_{4}$ filter the signal and noise low pass before sampler operating at $\frac{1}{T_{s}}$, so the noise and signal power spectral densities in the low pass band are preserved
- Therefore, in order to make TDFOM independent of oversampling factor, normalization of standard deviation is introduced as $\frac{\sigma_{n_{n}}}{\sqrt{O v}}$
- How $Q_{0}$ is calculated?
- For NRZ, $Q_{0}=\sqrt{2} \cdot \operatorname{erfc}^{-1}(2 \cdot B E R)$
- For PAM4, $Q_{0}=\sqrt{2} \cdot \mathrm{erfc}^{-1}\left(\frac{4}{3} \cdot 2 \cdot B E R\right)$


## Illustrative examples for $25 \mathrm{~Gb} / \mathrm{s}$ (980nm VCSEL)

AC PSD, from 0 to $3 / \mathrm{T}_{\mathrm{s}}$


AC PSD, from 0 to Nyquist


TDFOM = 0 dB (reference)


TDFOM = 1.2 dB (will produce worse sensitivity)


TDFOM = -0.7 dB (will produce better RX sensitivity)


## Shannon capacity illustration for $25 \mathrm{~Gb} / \mathrm{s}$



## TDFOM vs. RX sensitivity

Fitting: $O M A T P 4=T D F O M+K$


$10 \mathrm{~Gb} / \mathrm{s}$
2 VCSEL driver designs
Tbs $=-40,25$ and $125^{\circ} \mathrm{C}$
1 RX design at $125^{\circ} \mathrm{C}$

## Conclusion

- Reference receiver and TDFOM measurement method have been defined for transmitter characteristics specification and stress receiver sensitivity conditions of BASE-AU 980nm/OM3 PHY
- Reference receiver and TDFOM are defined to reflect the most representative receiver implementation, for sake of interoperability, but not precluding different implementations
- Reference receiver and TDFOM are proposed to be included in the BASE-AU 980nm/OM3 PMD baseline


## References

- [1] John M. Cioffi et al., "MMSE Decision-Feedback Equalizers and CodingPart I: Equalization Results," October 1995, IEEE Transactions on Communications, Vol. 43, No. 10
- [2] John M. Cioffi et al., "MMSE Decision-Feedback Equalizers and CodingPart II: Coding Results," October 1995, IEEE Transactions on Communications, Vol. 43, No. 10
- [3] John M. Cioffi, "Equalization", Course EE379A: Digital Communications Signal Processing, Chapter 3, Stanford University, [Online], Available: https:// cioffi-group.stanford.edu/doc/book/chap3.pdf


## Thank you

