## 200G/lane PAM4: Error Profile Error Propagation and Error Correction Considerations

## Part2 -Effects of precoding and Inner FEC code

Upen Reddy, Kareti<br>David, Nozadze<br>Cisco Systems Inc.

## Overview

This is continuation of the work presented in kareti 3dj 01a 230116 to further investigate by using Monte Carlo analysis

- The effectiveness of (1+D) precoding, when skip level errors and high level of correlated errors exist
- The effectiveness of Inner FEC code like BCH $(144,136)$ to accommodate higher level of DER_0 in optical sub-link


## Precoding : Link with DER_0 of 1e-4, random errors only cisco ( DFE tap1 =0/a=0)





| DERO=1e-4 | DER | CER (analytical) | Prob of Skipped 2 level symbol <br> errors (analytical) | Skipped 2 level symbol errors <br> (monte-carlo) | Prob of Skipped 2 level <br> symbol errors (monte-carlo) |
| :--- | :---: | :---: | :---: | :---: | :---: |
| average burst length <br> (monte-carlo) |  |  |  |  |  |
| w/ precoder | $2.0 \mathrm{E}-04$ | $9.7 \mathrm{E}-15$ | 0.25 | 135525 |  |
| w/o precoder | $1.0 \mathrm{E}-04$ | $2.7 \mathrm{E}-23$ | N.A. | 2 | N.A. |

[^0]
## Precoding : Link with DER_0 of 1e-4, with correlated errors including skip level errors(DFE tap1 $=1 / \mathrm{a}=0.75$ )





| DERO=1e-4 | DER | CER (analytical) | Prob of Skipped 2 level <br> symbol errors (analytical) | Skipped 2 level symbol errors <br> (monte-carlo) | Prob of Skipped 2 level symbol <br> errors (monte-carlo) | average burst length <br> (monte-carlo) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| w/precoder | $2.0 \mathrm{E}-04$ | $1.47 \mathrm{E}-11$ | NA | 113838 | 0.21 |  |
| w/o precoder | $4.0 \mathrm{E}-04$ | $2.77 \mathrm{E}-08$ | N.A. | N.A. | 2 |  |

## Precoding : Error patterns with and without skip level errors

adjacent level errors only (no skipped level errors)


- Two consecutive symbol errors becomes 2 single symbol errors

- Four consecutive symbol errors can result one two symbols and one single symbol errors

- Single symbol errors
becomes single two symbol error
single skipped error in the beginning of burst

- Two consecutive symbol errors can result 3 single symbol errors

- Single symbol errors
becomes single two symbol error
- After precoder both errors can be skipped error


## Concatenated sub-links

$\qquad$

- Data is received and re-transmitted without error corrections
- Two Monte Carlo models are simulated:

1. At each $R X, D E R O=1 e-4, a=0.75$
2. At each RX, DERO=1e-4, DFE tap1=1

- RS 544 FEC at each sub-link
- 5.44 e 9 symbols simulated



## Concatenated Sub-links: High level of skip level errors --- dfe1/alpha=1- precoding at all TXs and RXs OFF





| DFE1/alpha=1 | precoder | DERO | DER DFE | DER MLSD | CER with DFE (analytical) | extrapolated CER with DFE | extrapolated CER with MLSD | average burst length with DFE (monte-carlo) | average burst length with MLSD (monte-carlo) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| TX1/Rx1 | no/no | 1.00E-04 | 4.0E-04 | 9.0E-05 | 2.8E-08 |  |  | 3.99 | 3.99 |
| TX2/Rx2 | no/no | 1.00E-04 | 8.0E-04 | 1.9E-04 | 5.0E-07 |  |  | 3.99 | 3.99 |
| TX3/Rx3 | no/no | 1.00E-04 | 1.2E-03 | 2.8E-04 | 3.4E-06 |  | 3.4e-9 | 3.99 | 3.99 |


|  | PAM symb \# |
| :--- | :---: |
| Monte Carlo | $5.44 \mathrm{E}+08$ |

## Concatenated Sub-links: High level of skip level errors --- dfe1/alpha=1- precoding at all TXs and RXs ON



Number of symbol errors in RS FEC CW (t count)


| DFE1/alpha=1 | precoder | DERO | DER DFE | DER MLSD | CER with DFE (analytical) | extrapolated CER with DFE | extrapolated CER with MLSD | average burst length with DFE (monte-carlo) | average burst length with MLSD (monte-carlo) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| TX1/Rx1 | yes/yes | $1.00 \mathrm{E}-04$ | 2.0E-04 | $4.0 \mathrm{E}-05$ | $1.5 \mathrm{E}-11$ |  |  | 1.14 | 1.14 |
| TX2/Rx2 | yes/yes | $1.00 \mathrm{E}-04$ | 4.0E-04 | $9.0 \mathrm{E}-05$ | $3.8 \mathrm{E}-09$ |  |  | 1.14 | 1.14 |
| TX3/Rx3 | yes/yes | $1.00 \mathrm{E}-04$ | 6.0E-04 | $1.4 \mathrm{E}-04$ | 9.7E-08 |  | $1 \mathrm{e}-11$ | 1.14 | 1.14 |


|  | PAM symb \# |
| :--- | :---: |
| Monte Carlo | $5.44 \mathrm{E}+08$ |

## Concatenated Sub-links: High level of skip level errors --- dfe1/alpha=1





| DFE1/alpha=1 | precoder | DERO | DER DFE | DER MLSD | CER with DFE <br> (analytical) | extrapolated <br> CER with DFE | extrapolated <br> CER with MLSD | average burst length with DFE <br> (monte-carlo) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| TX1/R×1 | yes/no | $1.00 \mathrm{E}-04$ | $2.0 \mathrm{E}-04$ | $4.0 \mathrm{E}-05$ | $1.5 \mathrm{E}-11$ |  |  | 1.14 |
| $\mathrm{TX} / \mathrm{Rx} \times 2$ | no/no | $1.00 \mathrm{E}-04$ | $4.0 \mathrm{E}-04$ | $9.0 \mathrm{E}-05$ | $3.8 \mathrm{E}-09$ |  |  |  |
| $\mathrm{TX} 3 / \mathrm{Rx} 3$ | no/yes | $1.00 \mathrm{E}-04$ | $6.0 \mathrm{E}-04$ | $1.4 \mathrm{E}-04$ | $9.7 \mathrm{E}-08$ |  |  | 1.14 |


|  | PAM symb \# |
| :--- | :---: |
| Monte Carlo | $5.44 \mathrm{E}+08$ |

## Concatenated sub-links : Inner BCH Code

- Data is received and re-transmitted without error corrections
- End2End RS 544 FEC
- Inner FEC at middle sub-link $\operatorname{BCH}(144,136,1)$
- 5.44 e 9 symbols simulated



## Concatenated sub-links: w/o vs w/ BCH correction at RX2---Precoding off at all TX/RX

RX1/RX3 DFE=0.7, RX2 DFE=0.2




|  | DFE | precoder | DER0 | extrapolated CER with <br> DFE for case 1 | extrapolated CER with <br> DFE for case 2 | average burst length <br> with DFE (w/ BCH) | average burst length <br> with DFE (w/o BCH) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| TX1/Rx1 | 0.7 | no/no | $1.00 \mathrm{E}-05$ |  |  | 3.50 |  |
| TX2/Rx2 | 0.2 | no/no | $2.40 \mathrm{E}-04$ |  |  | 2.72 |  |
| TX3/Rx3 | 0.7 | no/no | $1.00 \mathrm{E}-05$ | $3.8 \mathrm{E}-10$ |  | $1.0 \mathrm{E}-11$ | 3.04 |


| PAM symbols | $5.44 \mathrm{E}+08$ |
| :---: | :---: |
| total number of BCH blocks | $8.00 \mathrm{E}+06$ |

[^1]| bits error per BCH block | dfe1 at $\mathrm{RX2}=0.2$ |
| :---: | :---: |
| 1 | 136500 |
| 2 | 2646 |
| 3 | 51 |
| 4 | 0 |
| 5 | 0 |

## Concatenated sub-links: w/o vs w/ BCH correction at RX2---Precoding off at all TX/RX

RX1/RX3 DFE=0.7, RX2 DFE=0.5




|  | DFE | precoder | DER0 | extrapolated CER with <br> DFE for case 1 | extrapolated CER with <br> DFE for case 2 | average burst length <br> with DFE (w/ BCH) | average burst length <br> with DFE (w/o BCH) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| TX1/Rx1 | 0.7 | no/no | $1.00 \mathrm{E}-05$ |  |  | 3.58 |  |
| TX2/Rx2 | 0.5 | no/no | $2.40 \mathrm{E}-04$ |  |  | 2.64 | 1.54 |
| TX3/Rx3 | 0.7 | no/no | $1.00 \mathrm{E}-05$ | $2.5 \mathrm{E}-09$ |  | 2.73 |  |


| PAM symbols | $5.44 \mathrm{E}+08$ |
| :---: | :---: |
| total number of BCH blocks | $8.00 \mathrm{E}+06$ |

Case1--- no BCH correction
Case2--- $\mathrm{BCH}(144,136,1)$ correction at RX2

| bits error per BCH block | dfe1 at $\mathrm{RX2}=0.5$ |
| :---: | :---: |
| 1 | 88409 |
| 2 | 31558 |
| 3 | 12041 |
| 4 | 4443 |
| 5 | 1664 |

## Concatenated sub-links: link w/o vs w/ BCH correction at RX2---Precoding off at all TX/RX

RX1/RX3 DFE=0.7, RX2 DFE=0.9




|  | DFE | precoder | DER0 | extrapolated CER with <br> DFE for case 1 | extrapolated CER with <br> DFE for case 2 | average burst length <br> with DFE (w/ BCH) | average burst length <br> with DFE (w/o BCH) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| TX1/Rx1 | 0.7 | no/no | $1.00 \mathrm{E}-05$ |  |  | 3.56 | 3.59 |
| TX2/Rx2 | 0.9 | no/no | $2.40 \mathrm{E}-04$ |  |  | 4.68 | 3.94 |
| TX3/Rx3 | 0.7 | no/no | $1.00 \mathrm{E}-05$ | $1.6 \mathrm{E}-06$ | $2.4 \mathrm{E}-06$ | 3.40 | 3.92 |


| PAM symbols | $5.44 \mathrm{E}+08$ |
| :---: | :---: |
| total number of BCH blocks | $8.00 \mathrm{E}+06$ |

Case1--- no BCH correction
Case2--- $\mathrm{BCH}(144,136,1)$ correction at RX2

| bits error per BCH block | dfe1 at $R \times 2=0.9$ |
| :---: | :---: |
| 1 | 39022 |
| 2 | 26224 |
| 3 | 19373 |
| 4 | 14174 |
| 5 | 10604 |

## Concatenated sub-links:

RX1/RX3 DFE=0.9, DFE=0.2




|  | DFE | precoder | DER0 | extrapolated CER with <br> DFE for case 1 | extrapolated CER with <br> DFE for case 2 | average burst length <br> with DFE (w/ BCH) | average burst length <br> with DFE (w/o BCH) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| TX1/Rx1 | 0.9 | no/no | $1.00 \mathrm{E}-05$ |  |  | 3.94 | 4.03 |
| TX2/Rx2 | 0.2 | no/no | $2.40 \mathrm{E}-04$ |  |  | 2.97 | 1.15 |
| TX3/Rx3 | 0.9 | no/no | $1.00 \mathrm{E}-05$ | $1.4 \mathrm{E}-09$ | $1.9 \mathrm{E}-10$ | 3.35 | 1.27 |


| bits error per BCH block | dfe1 at RX2=0.2 |
| :---: | :---: |
| 1 | 136463 |
| 2 | 2618 |
| 3 | 51 |
| 4 | 1 |
| 5 | 0 |


| PAM symbols | $5.44 \mathrm{E}+08$ |
| :---: | :--- |
| total number of BCH blocks | $8.00 \mathrm{E}+06$ |

## Concatenated sub-links: w/o vs w/ BCH correction at RX2---Precoding off at all TX/RX

RX1/RX3 DFE=0.9, RX2 DFE=0.5




|  | DFE | precoder | DER0 | extrapolated CER with <br> DFE for case 1 | extrapolated CER with <br> DFE for case 2 | average burst length <br> with DFE (w/ BCH) | average burst length <br> with DFE (w/o BCH) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| TX1/Rx1 | 0.9 | no/no | $1.00 \mathrm{E}-05$ |  |  | 4.04 |  |
| TX2/Rx2 | 0.5 | no/no | $2.40 \mathrm{E}-04$ |  |  | 2.68 | 4.08 |
| TX3/Rx3 | 0.9 | no/no | $1.00 \mathrm{E}-05$ | $7.7 \mathrm{E}-09$ |  | $2.2 \mathrm{E}-10$ | 1.71 |


| PAM symbols | $5.44 \mathrm{E}+08$ |
| :---: | :---: |
| total number of BCH blocks | $8.00 \mathrm{E}+06$ |

Case1--- no BCH correction
Case2--- $\mathrm{BCH}(144,136,1)$ correction at RX2

| bits error per $B C H$ block | dfe1 at $\mathrm{RX2}=0.5$ |
| :---: | :---: |
| 1 | 88510 |
| 2 | 31655 |
| 3 | 12029 |
| 4 | 4542 |
| 5 | 1614 |

## Concatenated sub-links: w/o vs w/ BCH correction at RX2---Precoding off at all TX/RX

RX1/RX3 DFE=0.9, RX2 DFE=0.9




|  | DFE | precoder | DER0 | extrapolated CER with <br> DFE for case 1 | extrapolated CER with <br> DFE for case 2 | average burst length <br> with DFE (w/ BCH) | average burst length <br> with DFE (w/o BCH) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| TX1/Rx1 | 0.9 | no/no | $1.00 \mathrm{E}-05$ |  |  | 3.95 |  |
| TX2/Rx2 | 0.9 | no/no | $2.40 \mathrm{E}-04$ |  |  | 4.71 |  |
| TX3/Rx3 | 0.9 | no/no | $1.00 \mathrm{E}-05$ | $3.7 \mathrm{E}-06$ |  | 4.96 |  |


| bits error per BCH block | dfe1 at RX2=0.9 |
| :---: | :---: |
| 1 | 38956 |
| 2 | 26259 |
| 3 | 19327 |
| 4 | 14558 |
| 5 | 10532 |


| PAM symbols | $5.44 \mathrm{E}+08$ |
| :---: | :---: |
| total number of BCH blocks | $8.00 \mathrm{E}+06$ |

Case1--- no BCH correction
Case2--- $\mathrm{BCH}(144,136,1)$ correction at RX2

- Data is received and re-transmitted without


## Concatenated sub-links : Inner BCH Code

 error corrections- End2End RS 544 FEC
- Inner FEC at middle sub-link $\operatorname{BCH}(144,136,1)$
- 5.44 e 9 symbols simulated



## Concatenated sub-links: -Precoding off at all sub-links and $\mathrm{CI}(4)$ Off


#### Abstract




## Concatenated sub-links: -Precoding on at AUI sub-links and $\mathrm{Cl}(4)$ Off



Concatenated sub-links: -Precoding on at AUI sub-links and $\mathrm{CI}(4)$


## Summary

- Precoding When Skip level error present
- After decoding pre-code, the data stream have higher bit errors compared to when there are no skip level errors
- No significant impact to error rate as skip level errors are relatively a few even for DFE tap1 = 1
- Inner FEC code ( BCH $(144,136, \mathrm{t})$ :
- Shown how many BCH bit error corrections are needed for various levels of correlated errors and Optical link target DER_Os (2.4e-4, 3.3e-3, 4.6e-3)
- Precoding on AUI links and 4 Codeword RSFEC interleave are very helpful


## Next steps

Look into Multipart links : 2 AUI sub-links on both sides of Optical sub-link for find solution space for different FEC strategies

- End2End RS 544 FEC
- Segmented FEC
- Concatenated FEC - End2End FEC with optical sub-link with Inner FEC code like BCH(144,136,t)


[^0]:    PAM symb \#

    | Monte Carlo | $2.72 \mathrm{E}+09$ |
    | :--- | :--- |

[^1]:    Case1--- no BCH correction
    Case2--- BCH $(144,136,1)$ correction at RX2

