

A Proposal for MLSE in COM Reference Receiver for KR/CR (AUI?)

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Introduction

- Defining MLSE for COM reference receivers was highlighted as one of the priorities in phase 1 ([lusted_3dj_elec_01_231207.pdf](#))
- MLSE seems necessary for KR/CR receivers
- MLSE may be necessary for AUIs, depending on the loss target (TBD)
- Some options are:
 - 1) Include MLSE COM calculations based on the existing proposal
 - 2) Use MLSE coding gain as a rough estimate (costs accuracy)
 - 3) Further simplify and relax COM margin by a constant amount (costs more accuracy)
 - 4) Find a better replacement for MLSE (currently no clear path)
 - 5) Ignore MLSE for channel compliance (channels need to become better)

History

- A detailed proposal for calculating the MLSE COM improvement using simple equations and compatible with the COM flow was proposed first in November 2022 in the IEEE Plenary ([shakiba_3df_01a_2211.pdf](#))
 - ❖ Calculates real SNR improvement of MLSE over DFE on a channel-by-channel basis
 - ❖ COM flow (Annex 93A) compatible
 - ❖ COM function friendly and fast and only needs few lines of code to post-process COM-generated data
- The proposal was further detailed and presented in January 2023 802.3 Joint Task Force Session ([shakiba_3dj_01_230116.pdf](#)) and in February 2023 802.3 dj Electrical ad hoc Meeting ([shakiba_3dj_elec_01_230223.pdf](#))
- This proposal was implemented in the COM Matlab function ver4.0 in February 2023 ([mellitz_3dj_elec_01a_230223.pdf](#))

History

- Based on the feedback, two updates have been provided since then:

1) April 2023 802.3 dj Electrical ad hoc Meeting ([shakiba_3dj_elec_01_230420.pdf](#)):

- a) COM improvement calculation was updated based on the target detector error ratio (DER0)
- b) A more comprehensive and accurate method for calculating MLSE noise PDF was explained
- c) Effect of noise coloring was analyzed and added

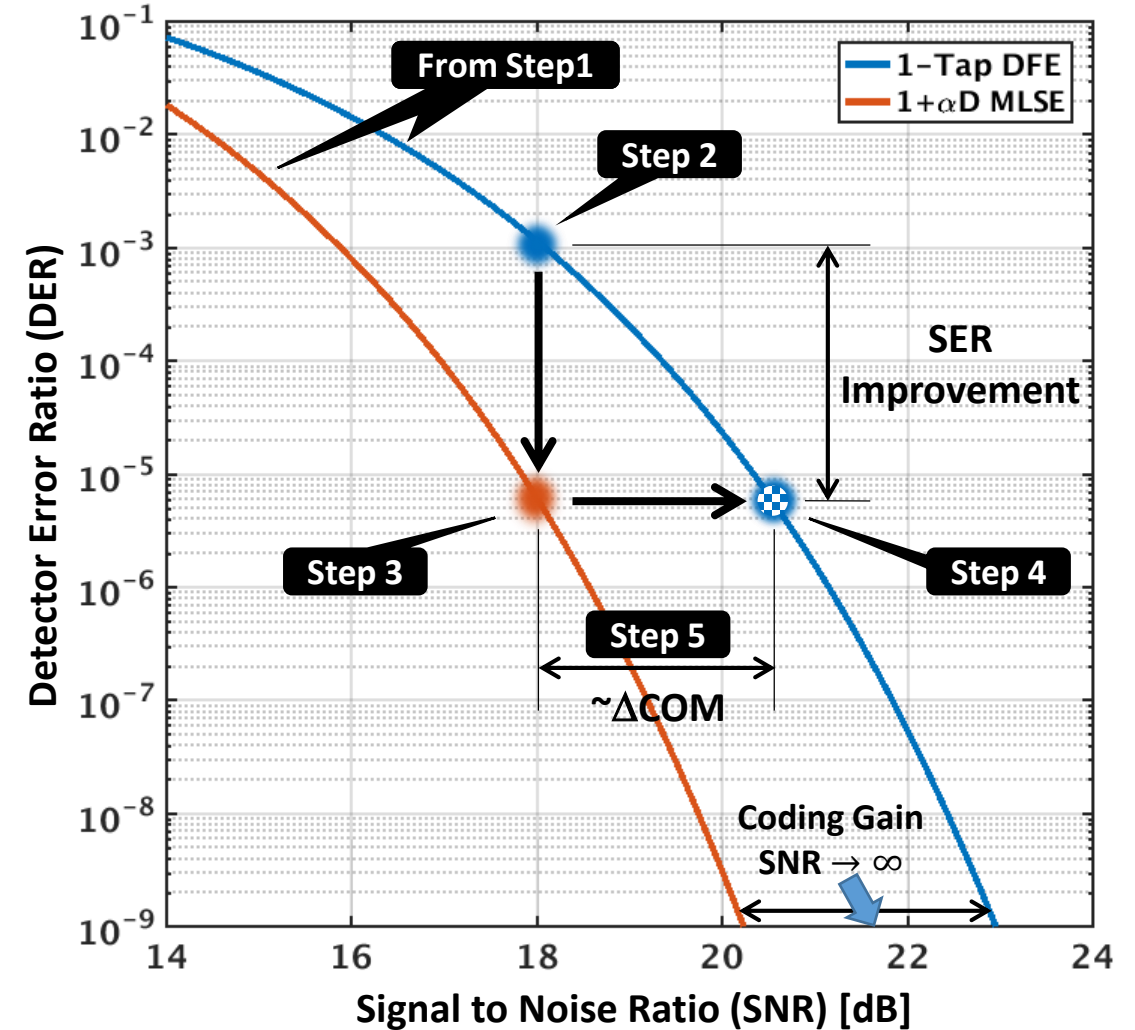
2) April 2023 802.3 dj Electrical ad hoc Meeting ([shakiba_3dj_elec_02_230420.pdf](#)):

- a) Error propagation in MLSE was analyzed and shown to be always better than DFE (approaches DFE as α approaches 1)

Proposal Recap

• The proposal specified following steps:

- 1) Use COM analysis to find DFE tap, α
- 2) From COM data calculate SNR_{DFE}
- 3) Use analysis to calculate DER_{MLSE} at SNR_{DFE}
- 4) Use analysis to calculate $\text{SNR}_{\text{DFE, equivalent}}$ for the same DFE that yields the same DER_{MLSE}
- 5) Increase from SNR_{DFE} to $\text{SNR}_{\text{DFE, equivalent}}$ gives a good estimate of COM improvement of MLSE



What was Added in Matlab COM Function v4.0 Beta1L

● After COM calculation (no change) the following values are passed to the MLSE calculator:

- a) DFE tap value (α)
 - b) Signal amplitude (A_s)
 - c) Total noise PDF and CDF (PDF_{noise} and CDF_{noise})
- } Step 1

● MLSE calculator calculates:

- a) Signal: $main = (L - 1)A_s$ (where $L = 4$ for PAM4)
 - b) Noise: σ_{noise} from noise PDF
 - c) $SNR_{DFE} = \frac{1}{3} \frac{L+1}{L-1} \frac{main^2}{\sigma_{noise}^2}$
- } Step 2

d) $SE_R \approx 2 \sum_{j=1}^{\infty} j \left(\frac{L-1}{L}\right)^j \left(1 - CDF_{noise} \left(\frac{main}{L-1} \sqrt{1 + (j-1)(1-\alpha)^2 + \alpha^2}\right)\right)$

} Step 3

e) $SNR_{DFE, equivalent} \approx \left(\frac{L-1}{main} CDF_{noise}^{-1} \left(1 - \frac{1}{2} SE_{R_{MLSE}} \left(\frac{1}{L-1} + CDF_{noise} \left(\frac{main}{L-1} (1 - 2\alpha) \right) \right) \right) \right)^2 SNR_{DFE}$

} Step 4

f) $\Delta COM \approx 10 \log_{10} \left(\frac{SNR_{DFE, equivalent}}{SNR_{DFE}} \right)$

} Step 5

Updates since then:

- 1) A minor tweak to change SER to DER
- 2) A more comprehensive method to calculate MLSE sequence noise
- 3) A new way to calculate noise to include coloring

MLSE Function in the COM Matlab Code (v4.0 Beta1L):

```
1936 function [MLSE_results] = MLSE(param,alpha,A_s,A_ni,PDF,CDF)
1937 % OP.MLSE= 1 ... COM and VEC will be adjusted with MLSE CDF
1938 % OP.MLSE= 2 ... COM and VEC will be adjusted with MLSE Gaussian assumptions
1939 % Based on oif2022.580.00 / IEEE802. shakiba_3dj_01_230116 by Hossein Shakiba
1940
1941 %% step 0
1942 COM_from_matlab=20*log10(A_s/A_ni);
1943 L=param.levels;
1944 DER0=param.specBER;
1945 %% step 1 from slide 6/5
1946 A_peak=(L-1)*A_s; % slide 6 A_s is main in appendix a
1947 main=A_peak;
1948 k_DER=qfuncinv(param.specBER);
1949 sigma_noise=sqrt(sum(PDF.y.*PDF.x.A2));
1950 SNR_dB=10*log10( 1/3*(L+1)/(L-1)*(A_peak^2)/sigma_noise^2 );
1951 COM=SNR_dB-10*log10((LA2-1)/3*k_DER^2);
1952 % sprintf('COM from Matlab %g dB\n COM from slide 6 using Gaussian assumptions %g dB\n', COM_from_matlab ,COM)
1953 if A_s >= A_ni
1954 %% step 2 slide 10/8
1955 SNR_DFE=1/3*(L+1)/(L-1)*(A_peak^2)/sigma_noise^2;
1956 %% step 2 slide 10/8
1957 % DER_DFE= 2/ ( L/(L-1) -qfunc( (1-2*alpha)*main/(L-1)/sigma_noise ) )*(qfunc(main/(L-1)/sigma_noise));
1958 % DER_DFE_CDF=2/ ( L/(L-1)-CDF_ev( (1-2*alpha)*main/(L-1),PDF,CDF ) ) *CDF_ev((main/(L-1)),PDF,CDF);
1959 %% step 3 side 11/9
1960 j=1:200;
1961 DER_MLSE=2*sum( j .* ((L-1)/L).^j .* qfunc( sqrt(1+(j-1)*(1-alpha)^2+alpha^2).* main/((L-1)*sigma_noise ) ));
1962 DER_MLSE_CDF=0; jj=1;
1963 DER_delta = inf;
1964 while DER_delta > .001
1965     last_DER_MLSE_CDF=DER_MLSE_CDF;
1966     DER_MLSE_CDF=2*( jj .* ((L-1)/L).^jj .* CDF_ev( sqrt(1+(jj-1)*(1-alpha)^2+alpha^2).* main/((L-1) ),PDF,CDF )+DER_MLSE_CDF;
1967     DER_delta= 1-last_DER_MLSE_CDF/DER_MLSE_CDF;
1968     jj=jj+1;
1969 end
1970 %% step 4 slide 12/10
1971 SNR_DFE_equivalent=SNR_DFE*(...
1972     (L-1)*sigma_noise/main * qfuncinv(...
1973     1/2 *DER_MLSE*(L/(L-1) - qfunc((1-2*alpha)*main/(L-1)*sigma_noise )) ...
1974     ) ...
1975     )^2;
1976 SNR_DFE_equivalent_CDF=SNR_DFE*(...
1977     (L-1)/main * CDF_inv_ev(...
1978     1/2 *DER_MLSE_CDF*(L/(L-1) - CDF_ev((1-2*alpha)*main/(L-1),PDF,CDF )) ...
1979     ,PDF, CDF ) ...
1980     )^2;
1981 %% step 5 slide 13/11
1982 delta_com=10*log10(SNR_DFE_equivalent/SNR_DFE);
1983 delta_com_CDF=10*log10(SNR_DFE_equivalent_CDF/SNR_DFE);
1984 new_com_CDF=COM_from_matlab+delta_com_CDF;
1985 else
1986     warning('MLSE not applied because there is more noise than signal')
1987     DER_MLSE=[];
1988     DER_MLSE_CDF=[];
1989     SNR_DFE_equivalent=[];
1990     SNR_DFE_equivalent_CDF=[];
1991     new_com_CDF=COM_from_matlab;
1992     delta_com_CDF=0;
1993     delta_com=0;
1994     SNR_DFE=[];
1995 end
```

This fix is needed:
must be placed in brackets
(similar to line 1960)
Only affects calculations with
Gaussian noise assumption

What is Really Being Calculated

- COM code directly followed the steps by which the MLSE COM analysis was conducted and presented
- The interim steps that were purposely included for clarity of the analysis description can be skipped, boiling down the MLSE COM calculation to:

❖ Passing α , A_s , and CDF_{noise} to the MLSE calculator

❖ Calculating:

$$DER_{MLSE} \approx 2 \sum_{j=1}^{\infty} j \left(\frac{3}{4}\right)^j \left(1 - CDF_{noise} \left(A_s \sqrt{1 + (j-1)(1-\alpha)^2 + \alpha^2}\right)\right)$$

$$\Delta COM \approx 20 \log_{10} \left(\frac{1}{A_s} CDF_{noise}^{-1} \left(1 - \frac{1}{2} DER_{MLSE} \left(\frac{1}{3} + CDF_{noise}((1-2\alpha)A_s) \right) \right) \right)$$

This is already implemented in the COM Matlab function. It is simple and costs almost no extra run time.

Presented Updates (1st, Must)

- Change the target error from SER (symbol error rate) to DER (detector error ratio)
- The MLSE COM calculation reduces to:

$$DER_{MLSE} \approx 2 \sum_{j=1}^{\infty} \left(\frac{3}{4}\right)^j \left(1 - CDF_{noise} \left(A_s \sqrt{1 + (j-1)(1-\alpha)^2 + \alpha^2}\right)\right)$$

$$\Delta COM \approx 20 \log_{10} \left(\frac{1}{A_s} CDF_{noise}^{-1} \left(1 - \frac{2}{3} DER_{MLSE} \right) \right)$$

Requires a minor tweak and
in fact simplifies the
implemented calculation.

Presented Updates (2nd, Recommended)

- For some computation overhead, adopt the approach presented in shakiba_3dj_elec_01_230420.pdf to more accurately calculate PDF of the MLSE sequence noise
- The MLSE COM calculation becomes:

$$DER_{MLSE} \approx 2 \sum_{j=1}^{\infty} \left(\frac{3}{4}\right)^j \left(1 - CDF_{noise,jEE}(A_s(1 + (j-1)(1-\alpha)^2 + \alpha^2))\right)$$

where $CDF_{noise,jEE}$ is calculated from $PDF_{noise,jEE}$:

$$PDF_{noise,jEE}(x) = PDF_{noise}(x) * \text{conv}_{i=2}^j PDF_{noise}((1-\alpha)x) * PDF_{noise}(\alpha x)$$

$$\Delta COM \approx 20 \log_{10} \left(\frac{1}{A_s} CDF_{noise}^{-1} \left(1 - \frac{2}{3} DER_{MLSE} \right) \right)$$

Requires j convolutions for each term of the summation.
The extra run time is reasonable and still negligible.

Presented Updates (3rd, Recommended)

- For more computation overhead, adopt the approach presented in shakiba_3dj_elec_01_230420.pdf to include the effect of noise coloring

- The MLSE COM calculation becomes:

$$DER_{MLSE} \approx 2 \sum_{j=1}^{\infty} \left(\frac{3}{4}\right)^j \left(1 - CDF_{noise,jEE} \left(A_s \frac{(\text{trace}(\rho_{noise,jEE}))^{\frac{3}{2}}}{\sqrt{\Sigma_{vertical} \Sigma_{horizontal}(\rho_{noise,jEE})}} \right) \right)$$

where $CDF_{noise,jEE}$ is calculated from $PDF_{noise,jEE}$:

$$PDF_{noise,jEE}(x) = PDF_{noise}(x) * \text{conv}_{i=2}^j PDF_{noise}((1-\alpha)x) * PDF_{noise}(\alpha x)$$

and $\rho_{noise,jEE}$ is calculated from the correlation coefficients of the noise:

$$\rho_{noise,jEE} = \begin{bmatrix} 1 & -(1-\alpha)\rho_1 & +(1-\alpha)\rho_2 & \cdots & (-1)^{j+1}\alpha\rho_j \\ -(1-\alpha)\rho_{-1} & (1-\alpha)^2 & -(1-\alpha)^2\rho_1 & \cdots & (-1)^j\alpha(1-\alpha)\rho_{j-1} \\ +(1-\alpha)\rho_{-2} & -(1-\alpha)^2\rho_{-1} & (1-\alpha)^2 & \cdots & (-1)^{j-1}\alpha(1-\alpha)\rho_{j-2} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ (-1)^{j+1}\alpha\rho_{-j} & (-1)^j\alpha(1-\alpha)\rho_{-(j-1)} & (-1)^{j-1}\alpha(1-\alpha)\rho_{-(j-2)} & \cdots & \alpha^2 \end{bmatrix}$$

Correlation coefficients in **RED** are due to noise coloring.

Presented Updates (3rd, Recommended)

and the correlation coefficients are obtained from inverse Fourier transform of the overall noise PSD (colored):

$$R_{NN}(\tau) = F^{-1}\{PSD_{noise}\}$$

which is obtained as power sum of the individual noise PSDs, each calculated based on their corresponding shaping filters (next slides)

$$PSD_{noise} = PSD_N + PSD_{TX} + PSD_{XT} + PSD_{ISI} + PSD_J$$

and finally:

$$\Delta COM \approx 20 \log_{10} \left(\frac{1}{A_s} CDF_{noise}^{-1} \left(1 - \frac{2}{3} DER_{MLSE} \right) \right)$$

Requires j convolutions and calculation of the correlation matrix for each term of the summation. The extra run time is still reasonable and negligible.

- If this method is adopted, it is also recommended that COM Matlab function be modified to import any of the individual input noise PSDs that is already colored

Noise Shaping Filters – eta0

- Appendix 93A:

$$\sigma_N^2 = \eta_0 \int_0^\infty |H_r(f)H_{ctf}(f)|^2 df \quad (93A-35)$$

$$H_r(f) = \frac{1}{1 - 3.414214(f/f_r)^2 + (f/f_r)^4 + j2.613126(f/f_r - (f/f_r)^3)} \quad (93A-20)$$

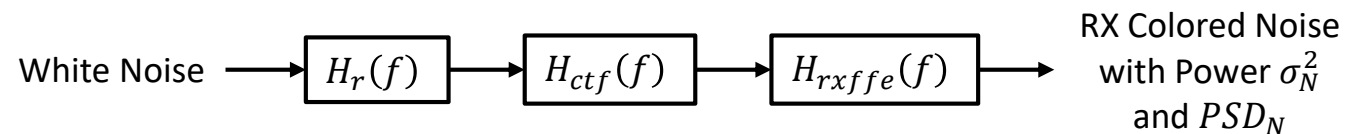
$$H_{ctf}(f) = \frac{\left(10^{\frac{\xi_{DC}}{20}} + j\frac{f}{f_z}\right)\left(10^{\frac{\xi_{DC2}}{20}} + j\frac{f}{f_{LF}}\right)}{\left(1 + j\frac{f}{f_{p1}}\right)\left(1 + j\frac{f}{f_{p2}}\right)\left(1 + j\frac{f}{f_{LF}}\right)} \quad (93A-22)$$

- Now RX FFE should be added, similar to (93A-21) for TX:

$$H_{ffe}(f) = \sum_{i=-1}^1 c(i) \exp(-j2\pi(i+1)(f/f_b)) \quad (93A-21)$$

Need a similar expression for RX FFE

- eta0 noise coloring filter:



Noise Shaping Filters – TX SNR

- Appendix 93A:

$$\sigma_{TX}^2 = [h^{(0)}(t_r)]^2 10^{-SNR_{TX}/10} \tag{93A-30}$$

$$h^{(k)}(t) = \int_{-\infty}^{\infty} X(f)H^{(k)}(f) \exp(j2\pi ft) df \tag{93A-24}$$

$$X(f) = A_r T_b \text{sinc}(fT_b) \tag{93A-23}$$

$$H^{(k)}(f) = H_{ffe}(f)H_t(f)H_{21}^{(k)}(f)H_r(f)H_{ctf}(f) \tag{93A-19}$$

$$H_{ffe}(f) = \sum_{i=-1}^1 c(i) \exp(-j2\pi(i+1)(f/f_b)) \tag{93A-21}$$

$$H_t(f) = \exp(-2(\pi f T_r / 1.6832)^2) \tag{93A-46}$$

$$H_r(f) = \frac{1}{1 - 3.414214(f/f_r)^2 + (f/f_r)^4 + j2.613126(f/f_r - (f/f_r)^3)} \tag{93A-20}$$

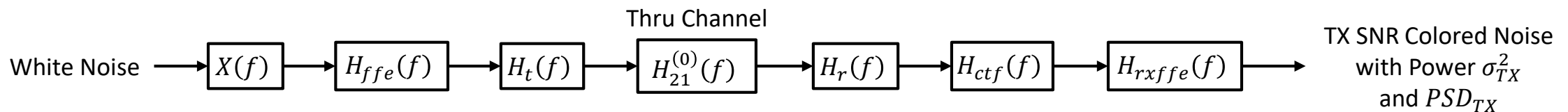
$$H_{ctf}(f) = \frac{\left(10^{\frac{\xi_{DC}}{20}} + j\frac{f}{f_z}\right)\left(10^{\frac{\xi_{DC2}}{20}} + j\frac{f}{f_{LF}}\right)}{\left(1 + j\frac{f}{f_{p1}}\right)\left(1 + j\frac{f}{f_{p2}}\right)\left(1 + j\frac{f}{f_{LF}}\right)} \tag{93A-22}$$

- Now RX FFE should be added, similar to (93A-21) for TX:

$$H_{ffe}(f) = \sum_{i=-1}^1 c(i) \exp(-j2\pi(i+1)(f/f_b)) \tag{93A-21}$$

Need a similar expression for RX FFE

- TX noise coloring filter:



Noise Shaping Filters – Xtalk

- Appendix 93A:

$$\sigma_{XT}^2 = \sum_{k=1}^{K-1} [\sigma_i^{(k)}]^2 \quad (93A-34)$$

$$[\sigma_m^{(k)}]^2 = \sigma_X^2 \sum_n [h^{(k)}((m/M+n)T_b)]^2 \quad (93A-33)$$

$$\sigma_X^2 = \frac{L^2 - 1}{3(L-1)^2} \quad (93A-29)$$

$$h^{(k)}(t) = \int_{-\infty}^{\infty} X(f)H^{(k)}(f) \exp(j2\pi ft) df \quad (93A-24)$$

$$X(f) = A_i T_b \text{sinc}(fT_b) \quad (93A-23)$$

$$H^{(k)}(f) = H_{ffe}(f)H_t(f)H_{21}^{(k)}(f)H_r(f)H_{ctf}(f) \quad (93A-19)$$

$$H_{ffe}(f) = \sum_{i=-1}^1 c(i) \exp(-j2\pi(i+1)(f/f_b)) \quad (93A-21)$$

$$H_t(f) = \exp(-2(\pi f T_r / 1.6832)^2) \quad (93A-46)$$

$$H_r(f) = \frac{1}{1 - 3.414214(f/f_r)^2 + (f/f_r)^4 + j2.613126(f/f_r - (f/f_r)^3)} \quad (93A-20)$$

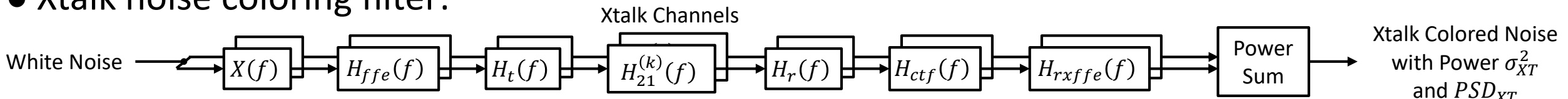
$$H_{ctf}(f) = \frac{\left(10^{\frac{\xi_{DC}}{20}} + j\frac{f}{f_z}\right) \left(10^{\frac{\xi_{DC2}}{20}} + j\frac{f}{f_{LF}}\right)}{\left(1 + j\frac{f}{f_{p1}}\right) \left(1 + j\frac{f}{f_{p2}}\right) \left(1 + j\frac{f}{f_{LF}}\right)} \quad (93A-22)$$

- Now RX FFE should be added, similar to (93A-21) for TX:

$$H_{ffe}(f) = \sum_{i=-1}^1 c(i) \exp(-j2\pi(i+1)(f/f_b)) \quad (93A-21)$$

Need a similar expression for RX FFE

- Xtalk noise coloring filter:



Noise Shaping Filters – ISI and Jitter

- Appendix 93A:

$$\sigma_{ISI}^2 = \sigma_X^2 \sum_n h_{ISI}^2(n) \tag{93A-31}$$

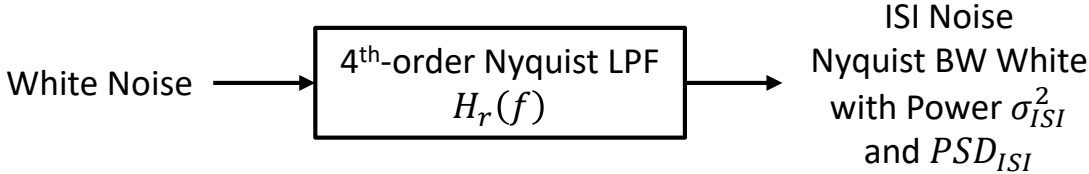
$$\sigma_J^2 = (A_{DD}^2 + \sigma_{RJ}^2) \sigma_X^2 \sum_n h_J^2(n) \tag{93A-32}$$

- ISI and jitter noises are assumed to remain white, but within the Nyquist bandwidth

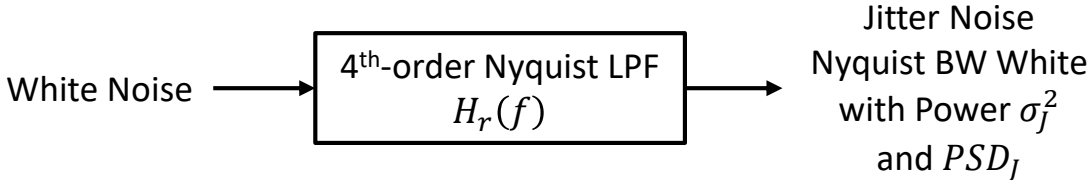
$$H_r(f) = \frac{1}{1 - 3.414214(f/f_r)^2 + (f/f_r)^4 + j2.613126(f/f_r - (f/f_r)^3)} \tag{93A-20}$$

Arbitrary and reasonable choice

- ISI noise filter:



- Jitter noise filter:



Parameters Needed to Be Passed to the MLSE Calculator

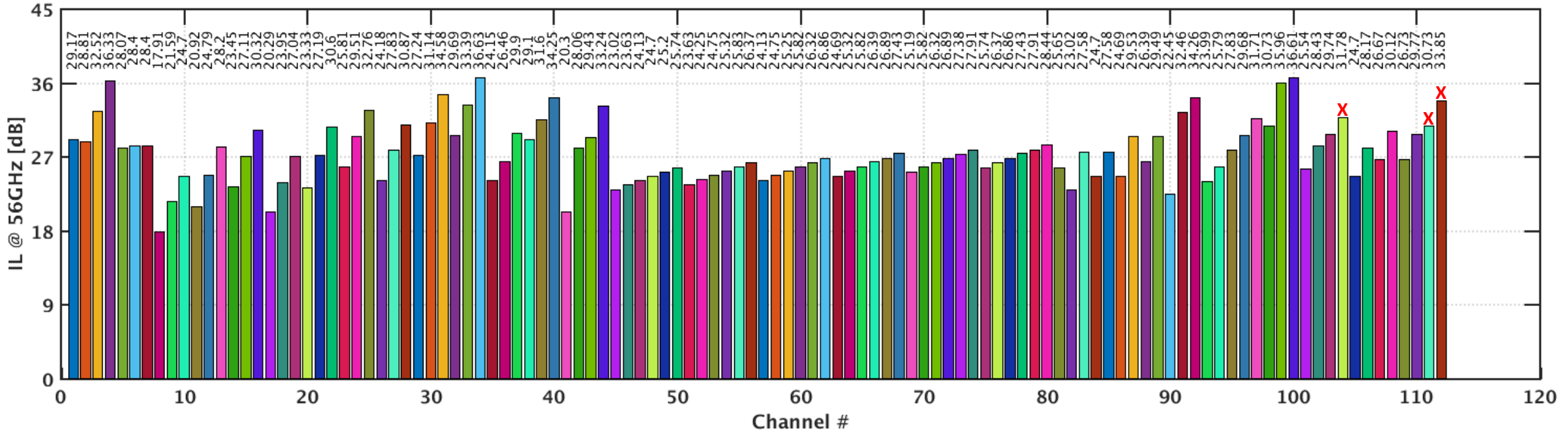
Parameter Description	Annex 93A Parameter Name	COM Matlab Parameter Name
<i>Without including noise coloring effect</i>		
DFE tap	b	DFE_taps
Signal amplitude	A_s	available_signal_after_eq_mV
noise PDF and CDF		PDF, CDF
<i>Additional parameters for including noise coloring effect</i>		
Noise sigma values	$\sigma_N, \sigma_{XT}, \sigma_{TX}, \sigma_{ISI}, \sigma_J$	sgm_N, sgm_TX, sgm_xt, sgm_isi, sgm_rjit, sgm_p_dd
Baud rate	f_b	baud_rate_GHz
Noise filter 3dB cutoff frequency	f_r	f_r
Frequency vector and step	f	faxis, max_freq_step
CTLE DC gains	g_{DC}, g_{DC2}	g_DC_HP, CTLE_DC_gaon_dB
CTLE poles and zeros	$f_{p1}, f_{p2}, f_z, f_{LF}$	CTLE_zero_poles, HP_poles_zero
RX FFE taps and number of pre-taps		RxFFE, ffe_pre_tap_len
TX FFE taps	c	TXLE_taps
TX transition times		transmitter_transition_time
Channel transfer functions	$H_{21}^{(k)}$	sdd21 and sdd21_raw
Termination resistors	R_d	R_diepad
Number of FXET and NEXT channels		num_fext, num_next
Channel s4p file names		filename
Oversampling ratio	M	samples_per_ui

Alternatively, and maybe more efficiently, calculation of noise PSDs can be done within the COM Matlab function. In fact, the filter transfer functions may have already been calculated.

Test Channels

Channel #	Channel Source
1	https://www.ieee802.org/3/dj/public/tools/CR/lim_3dj_03_230629.zip
2	https://www.ieee802.org/3/dj/public/tools/CR/lim_3dj_04_230629.zip
3 – 7	https://www.ieee802.org/3/dj/public/tools/CR/kocsis_3dj_02_2305.zip
8 – 34	https://www.ieee802.org/3/dj/public/tools/KR/mellitz_3dj_02_elec_230504.zip
35 – 40	https://www.ieee802.org/3/dj/public/tools/CR/shanbhag_3dj_01_2305.zip
40 – 44	https://www.ieee802.org/3/dj/public/tools/KR/shanbhag_3dj_02_2305.zip
45 – 80	https://www.ieee802.org/3/dj/public/tools/KR/weaver_3dj_02_2305.zip
80 – 88	https://www.ieee802.org/3/dj/public/tools/KR/weaver_3dj_elec_01_230622.zip
89	https://www.ieee802.org/3/dj/public/tools/CR/lim_3dj_07_2309.zip
90 – 96	https://www.ieee802.org/3/dj/public/tools/KR/akinwale_3dj_01_2310.zip
97 – 100	https://www.ieee802.org/3/dj/public/tools/CR/akinwale_3dj_02_2311.zip
101 – 112	https://www.ieee802.org/3/dj/public/tools/CR/weaver_3dj_02_2311.zip

Test Channels



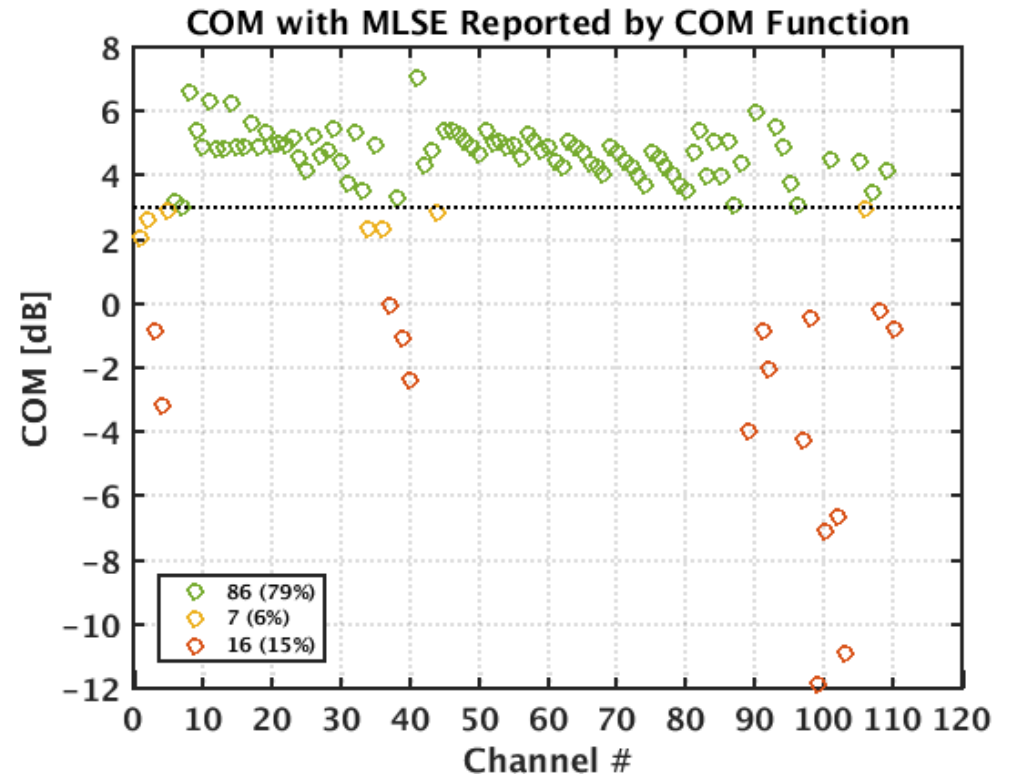
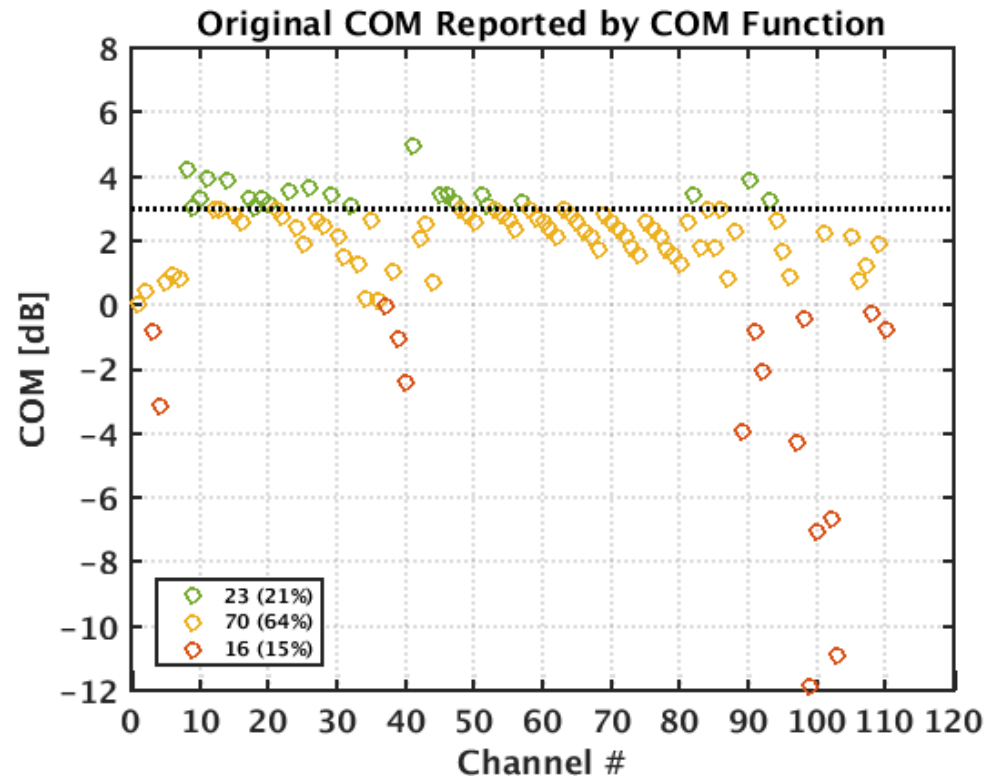
- IL ranges from 17.9dB to 36.6dB (average 27.5dB)
- For channels 104, 111, and 112 the COM function did not converge
 - ❖ Failed to find the floating tap locations (**best_floating_tap_locations**)

COM Configuration

Table 93A-1 parameters				I/O control			Table 93A-3 parameters		
Parameter	Setting	Units	Information	Parameter	Setting	Units	Parameter	Setting	Units
f_b	112	GBd		DIAGNOSTICS	0	logical	package_ti_gamma0_a1_a2	[0.5E-3 0.89E-3 0.2E-3]	
f_min	0.05	GHz		DISPLAY_WINDOW	0	logical	package_ti_tau	6.141E-03	ns/mm
Delta_f	0.01	GHz		CSV_REPORT	0	logical	package_z_c	[87.5 87.5 ; 92.5 92.5]	Ohm
C_d	[0.4e-4 0.9e-4 1.1e-4 ; 0.4e-4 0.9e-4 1.1e-4]	nF	[TX RX]	RESULT_DIR	\\results\100GEL_KR_{date}\		Table 92-12 parameters		
L_s	[0.13 0.15 0.14 ; 0.13 0.15 0.14]	nH	[TX RX]	SAVE_FIGURES	0	logical	Table 92-12 parameters		
C_b	[0.3e-4 0.3e-4]	nF	[TX RX]	Port Order	[1 3 2 4]		Parameter	Setting	
z_p select	[2]		[test cases to run]	RUNTAG	KR_eval_		board_ti_gamma0_a1_a2	[0.3.8206e-04 9.5909e-05]	
z_p (TX)	[12 33; 1.8 1.8]	mm	[test cases]	COM_CONTRIBUTION	0	logical	board_ti_tau	5.79E-03	ns/mm
z_p (NEXT)	[12 31; 1.8 1.8]	mm	[test cases]	Operational			board_z_c	100	Ohm
z_p (FEXT)	[12 33; 1.8 1.8]	mm	[test cases]	COM Pass Threshold	3	dB	z_bp (TX)	110.3	mm
z_p (RX)	[12 31; 1.8 1.8]	mm	[test cases]	ERL Pass Threshold	8	dB	z_bp (NEXT)	110.3	mm
C_p	[0.4e-4 0.4e-4]	nF	[TX RX]	DER_0	1.00E-04		z_bp (FEXT)	110.3	mm
R_0	50	Ohm		T_r	4.00E-03	ns	z_bp (RX)	110.3	mm
R_d	[46.25 46.25]	Ohm	[TX RX]	FORCE_TR	1	logical	C_0	[0.29E-4]	nF
A_v	0.413	V		Local Search	2		C_1	[0.19E-4]	nF
A_fe	0.413	V		BREAD_CRUMBS	1	logical	Include PCB	0	logical
A_re	0.608	V		SAVE_CONFIG2MAT	1	logical	Floating Tap Control		
AC_CM_RMS	0		[test cases]	PLOT_CM	0		N_bg	4	0 1 2 or 3 groups
L	4			TDR and ERL options			N_bf	5	taps per group
M	32			TDR	1	logical	N_f	60	UI span for floating taps
filter and Eq				ERL	1	logical	bmaxg	0.05	maxDFE value for floating taps
f_r	0.5		*fb	ERL_ONLY	0	logical	B_float_RSS_MAX	0.02	rss tail tap limit
c(0)	0.54		min	TR_TDR	0.01	ns	N_tail_start	25	(UI) start of tail taps limit
c(-1)	[-0.4:0:0.02:0]		[min:step:max]	N	3500		ICN parameters (v2.73+)		
c(-2)	[0:0.02:0:16]		[min:step:max]	rho_x	0.618		f_v	0.528	*Fb
c(-3)	[-0.1:0:0.02:0]		[min:step:max]	fixture delay time	[0 0]	[port1 port2]	f_f	0.528	*Fb
c(-4)	[0:0.02:0:1]		[min:step:max]	TDR_W_TXPKG	0		f_n	0.528	*Fb
c(-5)	0		[min:step:max]	N_bx	21	UI	f_2	80	GHz
c(-6)	0		[min:step:max]	Tukey_Window	1	logical	A_ft	0.6	V
c(1)	[-0.2:0:0.02:0]		[min:step:max]	Noise, Jitter			A_nt	0.6	V
N_b	1	UI		sigma_RJ	0.01	UI	Receiver testing		
b_max(1)	0.85		As/dffe1	A_DD	0.02	UI	RX_CALIBRATION	0.000	logical
b_max(2..N_b)	[0.3 0.2*ones(1,22)]		As/dfe2..N_b	eta_0	5.00E-09	V^2/GHz	Sigma_BBN_step	5.00E-03	V
b_min(1)	0.3		As/dffe1	SNR_TX	33	dB			
b_min(2..N_b)	[-0.3 -0.2*ones(1,22)]		As/dfe2..N_b	R_LM	0.95				
g_DC	[-20:1:0]	dB	[min:step:max]						
f_z	44.8	GHz							
f_p1	44.8	GHz							
f_p2	112	GHz							
g_DC_HP	[-6:1:0]		[min:step:max]						
f_HP_PZ	1.4	GHz							
MLSE	1								
fie_pre_tap_len	6								
fie_post_tap_len	24								
fie_tap_step_size	0								
fie_main_cursor_min	0.7								
fie_pre_tap1_max	0.7								
fie_post_tap1_max	0.7								
fie_tapn_max	0.7								
fie_backoff	0								
fie_float	0		1:FFE float						
fie_bg	4		float FFE groups						
fie_tr	5		taps per group						
fie_Nf	60		float taps range						
LF_PieTap_Ext	10		LF FFE pre-tap ext						
LF_PostTap_Ext	10		LF FFE post-tap ext						

- COM Version: com_ieee8023_93a_420beta3
 - ❖ COM function calculates MLSE ΔCOM (based on SER)
- + Post-COM MLSE Calculator
 - ❖ Calculates MLSE ΔCOM based on SER, DER, with the improved MLSE noise PDF for white and colored noise

Test Results – COM Function

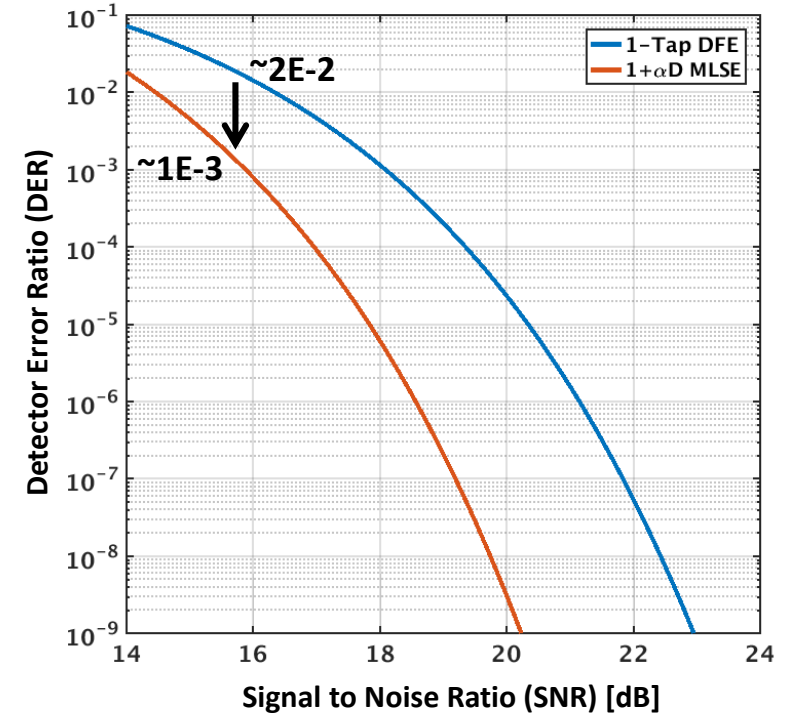


- Currently COM function ignores MLSE and reports $\Delta\text{COM} = 0$ if the original COM is negative
- This was a quick patch to ignore cases with low SNR, where analysis is less accurate
- 16 ignored cases for the current test channels

Cases to Ignore

- A better option is to, instead of ignoring based on COM, ignore cases with DER threshold value more than a reasonable level, say $2E-2$
- DER is a more direct indication of the error performance
- DER threshold is DER at COM = 0 and is already reported by the COM function
- In either case, these are cases that most likely fail even with MLSE
- Nevertheless, it is still good to see the failing margin

Channels Ignored	Channel #
COM < 0	3, 4, 37, 39, 40, 89, 91, 92, 97, 98, 99, 100, 102, 103, 108, 110 (16 Channels)
DER Threshold > $2E-2$	4, 40, 89, 97, 99, 100, 102, 103 (8 Channels)

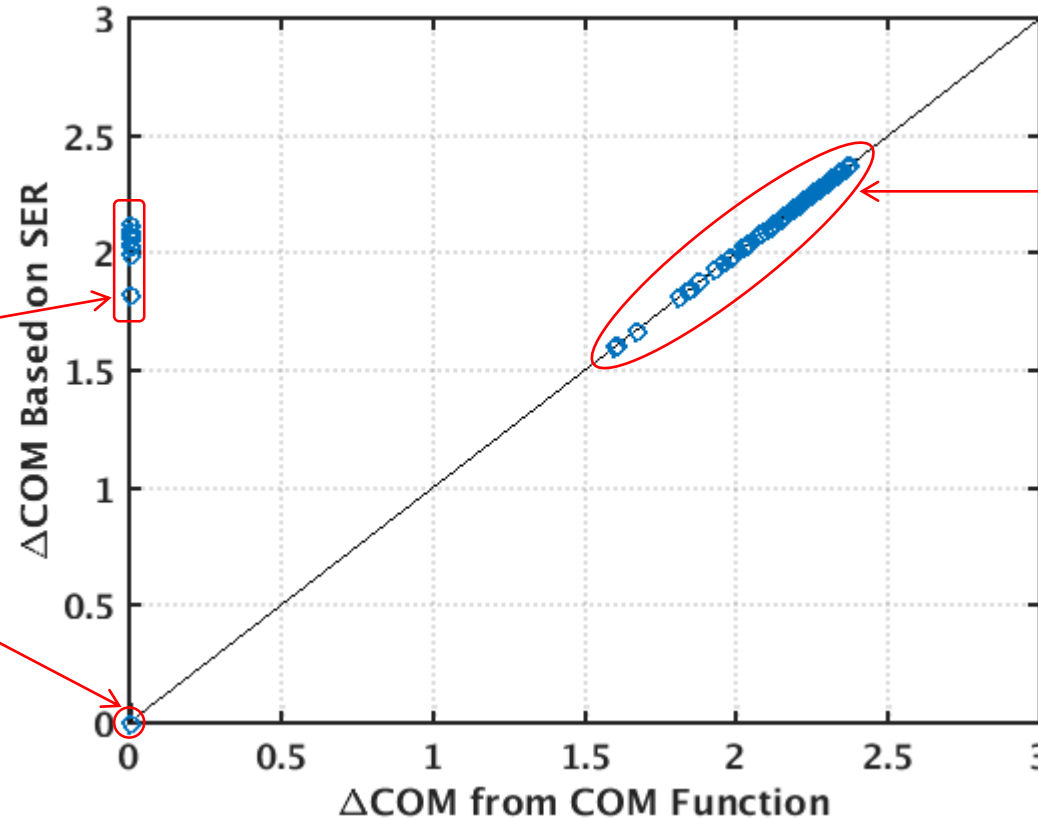


Test Results – Compare to COM Function

16 cases have $COM < 0$

8 of the 16 cases pass DER threshold of $2E-2$ and can be added back to MLSE calculations

8 of the 16 cases have DER threshold above $2E-2$



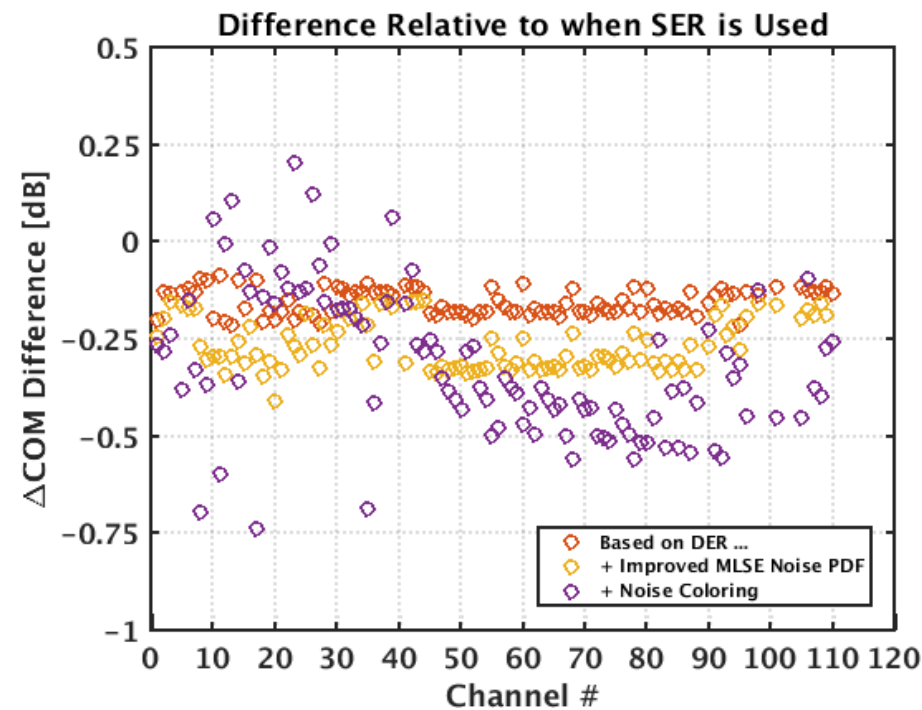
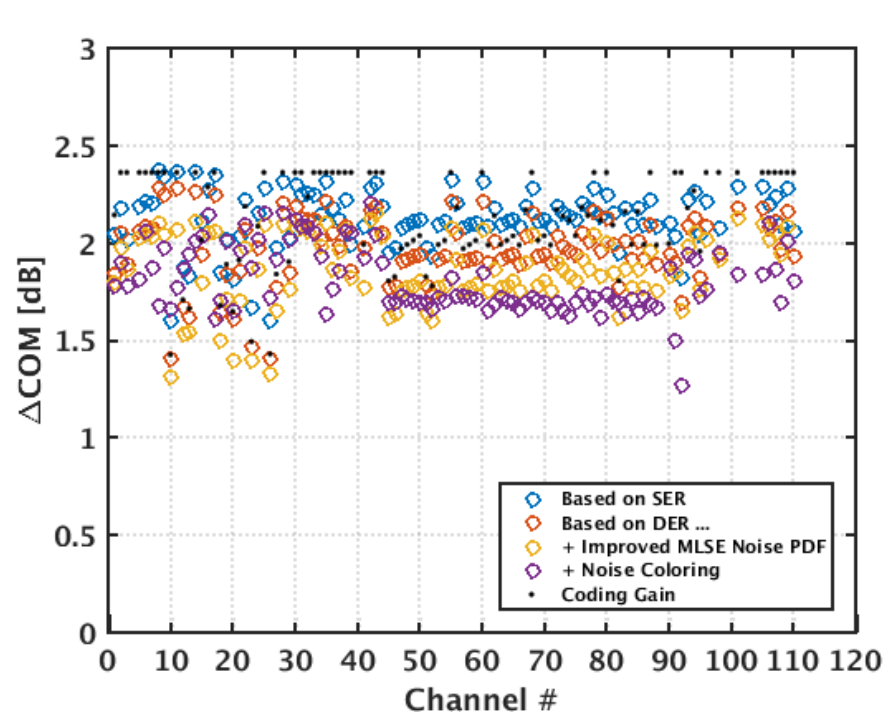
100% correlation for 93 other cases

Total # of Channels	# of Channels for which COM Function Calculated COM	# of Channels for which COM Function Calculated ΔCOM	# of Channels for which COM Calculator Calculated ΔCOM
112	109	93	101

Test Results – Latest Updates

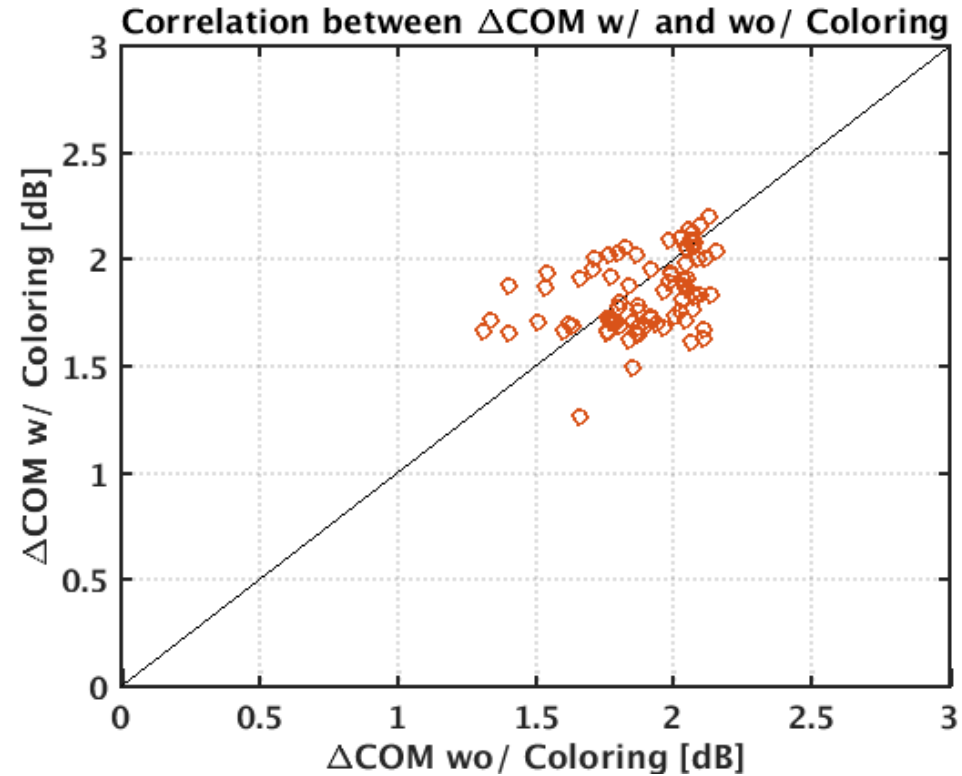
- Recent updates of the MLSE proposal on average predict a little less ΔCOM

- 1) Change of SER to DER
- 2) + more comprehensive calculation method for MLSE noise PDF
- 3) + inclusion of noise coloring



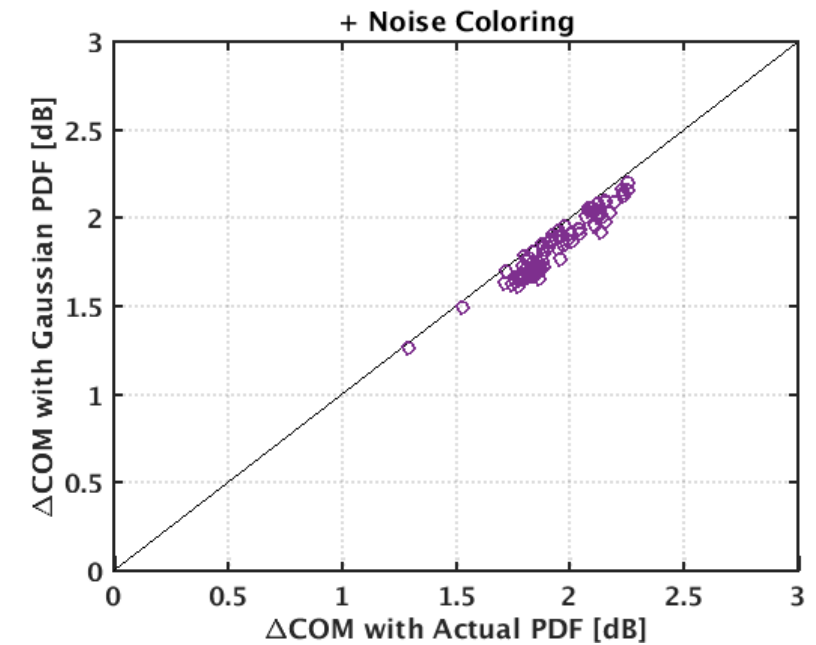
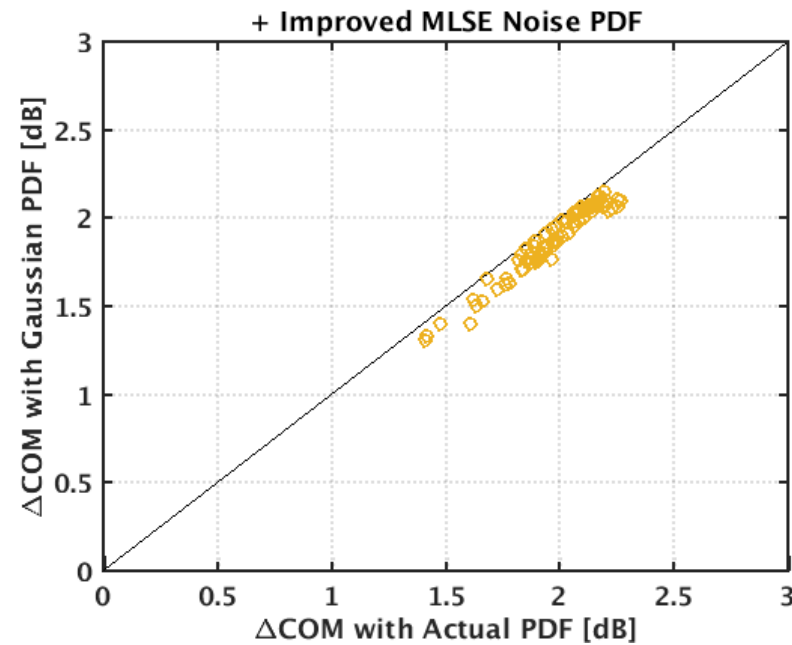
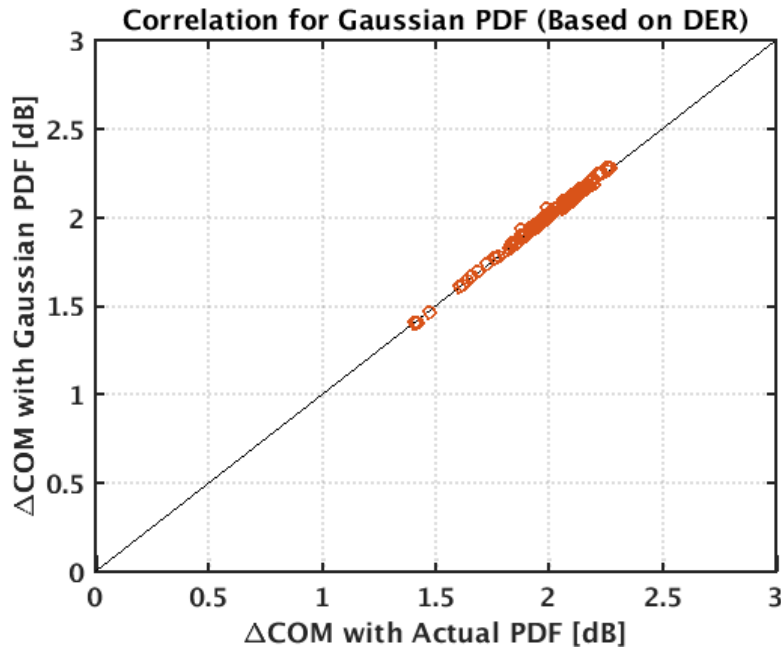
[dB]	Based on SER (as Currently Reported by the COM Function)	Based on DER ("Must" Change)	Improved MLSE Noise PDF, White ("Nice to " Update)	Improved MLSE Noise PDF, Color ("Nice to " Update)
ΔCOM (ave)	2.13	1.98	1.86	1.81
Difference (ave)	0	-0.15	-0.27	-0.32

Test Results – White or Colored Noise?



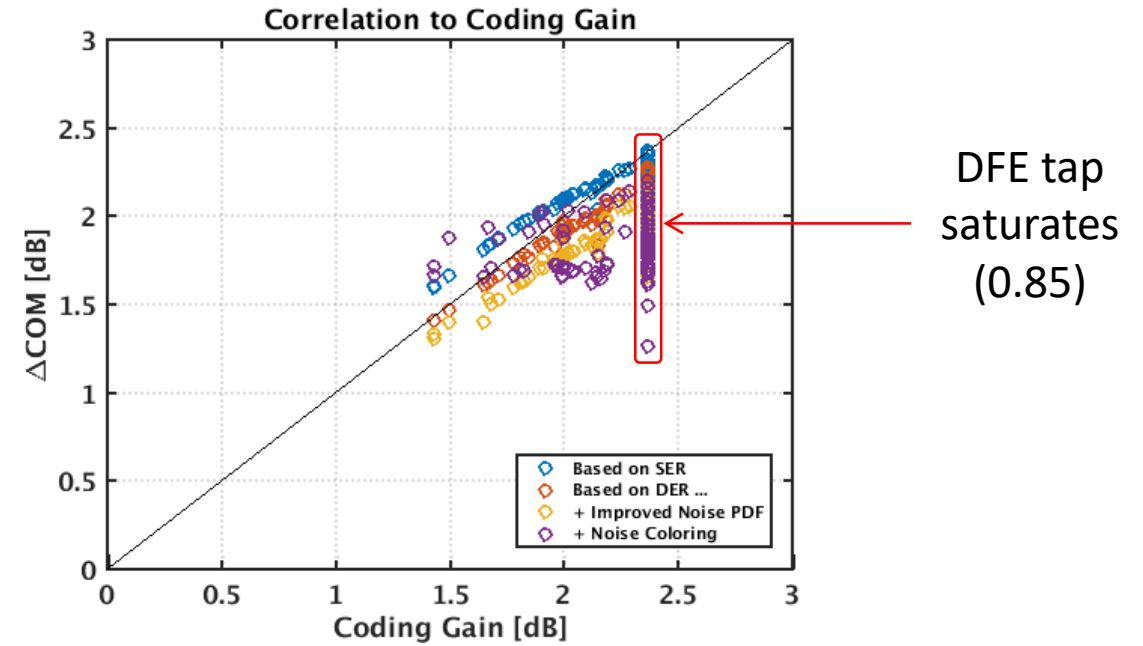
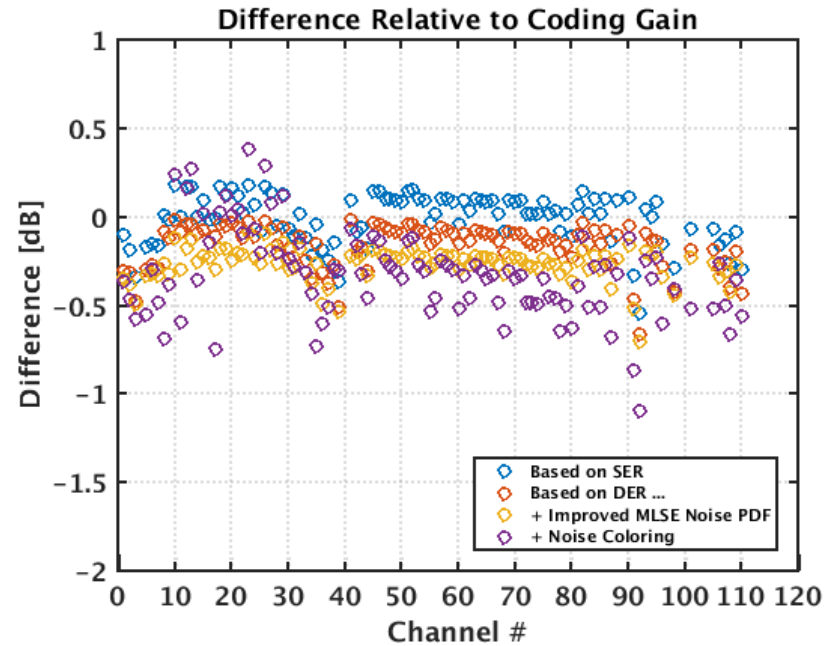
- The correlation between ΔCOM calculated with and without noise coloring is weak
- It is a good idea to include the effect of noise coloring

Test Results – Actual or Gaussian Noise Distribution?



- Using the actual noise PDF (as calculated by the COM function) instead of assuming it is Gaussian makes more sense as the accuracy of the MLSE calculator improves

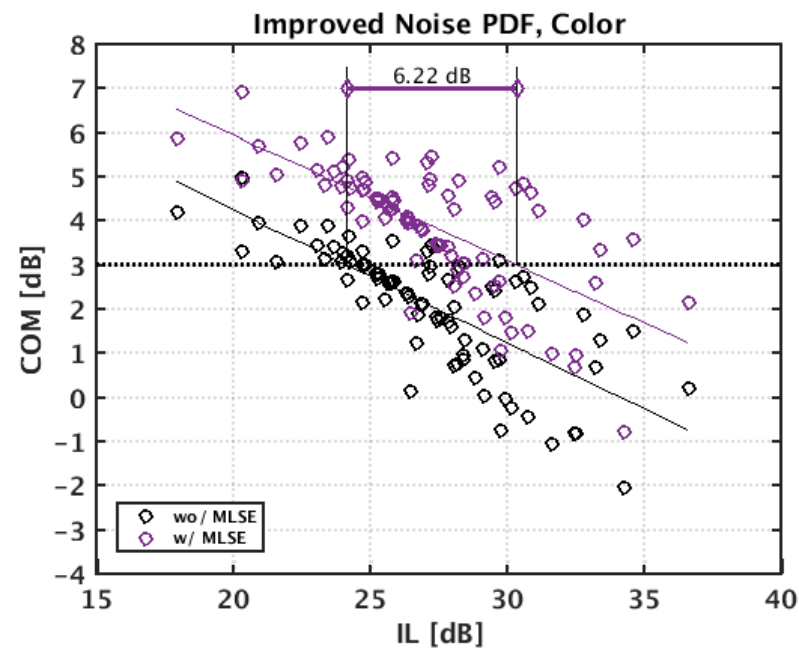
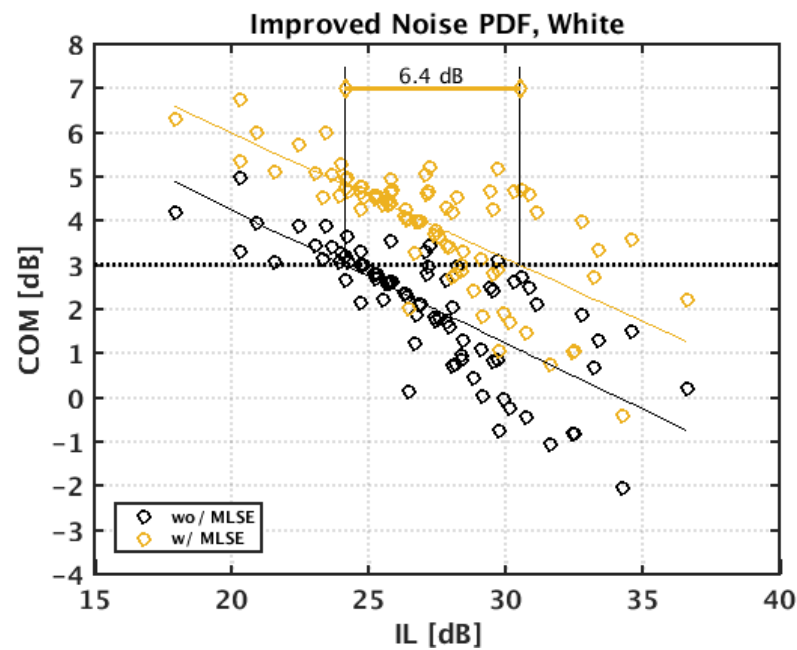
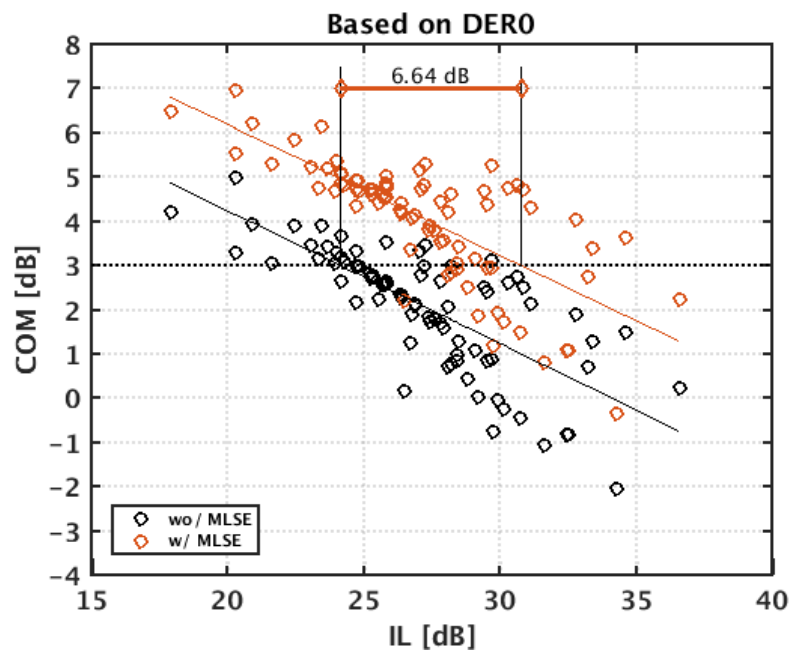
Test Results – Δ COM or Coding Gain?



- Coding gain correlation to Δ COM weakens as Δ COM calculation becomes more accurate
- Coding gain is not a representative of MLSE COM advantage when DFE tap saturates

[dB]	Coding Gain ($10 \log_{10}(1 + \alpha^2)$)	Based on SER (as Currently Reported by the COM Function)	Based on DER ("Must" Change)	Improved MLSE Noise PDF, White ("Nice to " Update)	Improved MLSE Noise PDF, Color ("Nice to " Update)
Δ COM (ave)	2.14	2.13	1.98	1.86	1.81
Difference (ave)	0	-0.01	-0.16	-0.27	-0.33

Test Results – IL Improvement



[dB]	Based on DER ("Must" Change)	Improved MLSE Noise PDF, White ("Nice to " Update)	Improved MLSE Noise PDF, Color ("Nice to " Update)
IL Improvement with MLSE	6.64	6.40	6.22

- Note that this is only a rough average estimate based a linear fit to the scattered data

Summary and Conclusions

- MLSE seems necessary for KR/CR and maybe for AUIs
- This presentation summarized a proposal for inclusion of MLSE in COM flow (Annex 93A and COM Matlab function)
- Other options such as ignoring MLSE, allowing a fix COM margin, or using MLSE coding gain are far less accurate and non-realistic
- Currently, this proposal is the most accurate and realistic option to include MLSE for channel compliance
- A simple calculator can post-process data generated by the COM Matlab function
- Effects of actual noise distribution and coloring were quantified and included in the proposal
- MLSE Δ COM results for additional 112 test channel cases were presented