## An Executive Summary of the MLSE Proposal

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## Introduction

- Defining MLSE for COM reference receivers was highlighted as one of the priorities in phase 1 (lusted 3dj elec 01 231207.pdf)
- MLSE seems necessary for KR/CR receivers
- MLSE may be necessary for C2M/C2C, depending on the loss target (TBD)
- $1^{\text {st }}$ priority is to agree if MLSE is needed to be a part of the reference receiver
- $2^{\text {nd }}$ priority is to find the best practical approach to achieve this
- Some options are:
A. Include MLSE COM calculations based on the existing proposal
B. Use MLSE coding gain as a rough estimate (costs accuracy)
C. Further simplify and relax COM margin by a constant amount (costs more accuracy)
D. Find a better replacement for MLSE (currently no clear path)
E. Ignore MLSE for channel compliance (channels need to become better)


## History

| Date | Content | Reference Contribution |
| :--- | :--- | :--- |
| November 2022 | Original Proposal | shakiba 3df 01a 2211.pdf |
| January 2023 | Further Details | shakiba_3dj_01_230116.pdf |
| February 2023 | Recap | shakiba 3dj_elec 01 230223.pdf |
| February 2023 | First COM Matlab Code | mellitz_3dj_elec_01a_230223.pdf |
| April 2023 | First Update (U1.a, U1.b, U1.c) | shakiba_3dj_elec 01_230420.pdf |
| April 2023 | MLSE Error Propagation | shakiba 3dj elec 02 230420.pdf |
| January 2024 | Recap and Test Data | shakiba_3dj_elec 01a_240104.pdf |

- Considering an MLSE implementation penalty was suggested in shakiba_3df 01a 2211.pdf as a later step (amount TBD)
- This presentation suggests making this explicit and as the last step of the proposal


## Proposal Recap

- The proposal specified following steps:

1) Use COM analysis to find DFE tap, $\alpha$
2) From COM data calculate $\operatorname{SNR}_{\text {DFE }}$
3) Use analysis to calculate $\operatorname{DER}_{\text {MLSE }}$ at $S N R_{\text {DFE }}$
4) Use analysis to calculate $S_{\text {D }}^{\text {DFE, equivalent }}$ for the same DFE that yields the same DER $_{\text {MLSE }}$
5) Increase from $S N R_{\text {DFE }}$ to $S N R_{\text {DFE, equivalent }}$ gives a good estimate of COM advantage of MLSE ( $\triangle C O M$ )

* 6) Consider an MLSE implementation penalty (TBD) to be subtracted from $\triangle C O M$



## Summary of $\Delta$ COM Equations

- The original equation (currently coded in COM Matlab function) includes error propagation and should be disregarded and updated moving forward
- The following updated equations are all based on DER and exclude error propagation

|  | Intermediate Equation | MLSE $\triangle$ COM Equation | Comment |
| :---: | :---: | :---: | :---: |
| U1.a | $D E R_{M L S E} \approx 2 \sum_{j=1}^{\infty}\left(\frac{3}{4}\right)^{j}\left(1-C D F_{\text {noise }}\left(A_{s} \sqrt{1+(j-1)(1-\alpha)^{2}+\alpha^{2}}\right)\right)$ | $\Delta C O M \approx 20 \log _{10}\left(\frac{1}{A_{s}} C D F_{\text {noise }}^{-1}\left(1-\frac{2}{3} D E R_{\text {MLSE }}\right)\right)-\text { Implementation Penalty }$ | Excludes Error Propagation |
| U1.b | $\begin{gathered} D E R_{\text {MLSE }} \approx 2 \sum_{j=1}^{\infty}\left(\frac{3}{4}\right)^{j}\left(1-C D F_{\text {noise }, j E E}\left(A_{s}\left(1+(j-1)(1-\alpha)^{2}+\alpha^{2}\right)\right)\right) \\ P D F_{\text {noise }, j E E}(x)=P D F_{\text {noise }}(x) * \operatorname{conv}_{i=2}^{j} P D F_{\text {noise }}(x /(1-\alpha)) * P D F_{\text {noise }}(x / \alpha) \end{gathered}$ |  | U1.a <br> + <br> Improved MLSE <br> Noise Calculation |
| U1.C | $\begin{aligned} & D E R_{\text {MLSE }} \approx 2 \sum_{j=1}^{\infty}\left(\frac{3}{4}\right)^{j}\left(1-C D F_{\text {noise }, j E E}\left(A_{s} \frac{\left(\operatorname{trace}\left(\rho_{\text {noise }, j E E}\right)\right)^{\frac{3}{2}}}{\sqrt{\sum_{\text {vertical }} \sum_{\text {horizental }}\left(\rho_{\text {noise }, j E E}\right.}}\right)\right) \\ & P D F_{\text {noise }, j E E}(x)=P D F_{\text {noise }}(x) * \operatorname{conv}_{i=2}^{j} P D F_{\text {noise }}(x /(1-\alpha)) * P D F_{\text {noise }}(x / \alpha) \end{aligned}$ <br> For calculating the correlation matrix ( $\rho_{\text {noise }, j E E}$ ) from the colored noise PSD, see shakiba 3dj elec 01a 240104.pdf |  | U1.b <br> $+$ <br> Noise Coloring Effect |

- For analysis details and derivation of these equations refer to the previous contributions


## Test Results (See Backup Slide for Test Channels)

Option A


Option B


Option C


- Implementation penalty is not included
- As updated equations kick in, $\triangle$ COM reduces and becomes more channel dependent
- Coding gain is not a representative of MLSE COM advantage when DFE tap saturates
- For the test channels:
* The difference between $\triangle C O M$ and coding gain could be as much as $+0.4 \mathrm{~dB} /-1.1 \mathrm{~dB}$
$*$ The difference between $\triangle C O M$ and its fix average value could be as much as $+0.4 \mathrm{~dB} /-0.6 \mathrm{~dB}$
- At $200+G$ every dB (or even a fraction of a dB) counts and must be meaningful to close the link


## Backup Slide - Test Channels

| Channel \# | Channel Source |
| :---: | :---: |
| 1 | https://www.ieee802.org/3/dj/public/tools/CR/lim 3dj 03 230629.zip |
| 2 | https://www.ieee802.org/3/dj/public/tools/CR/lim 3dj 04 230629.zip |
| 3-7 | https://www.ieee802.org/3/di/public/tools/CR/kocsis 3di 02 2305.zip |
| 8-34 | https://www.ieee802.org/3/dj/public/tools/KR/mellitz 3dj 02 elec 230504.zip |
| 35-40 | https://www.ieee802.org/3/dj/public/tools/CR/shanbhag 3dj 01 2305.zip |
| 40-44 | https://www.ieee802.org/3/dj/public/tools/KR/shanbhag 3dj 02 2305.zip |
| 45-80 | https://www.ieee802.org/3/di/public/tools/KR/weaver 3dj 02 2305.zip |
| 80-88 | https://www.ieee802.org/3/dj/public/tools/KR/weaver 3dj elec 01 230622.zip |
| 89 | https://www.ieee802.org/3/dj/public/tools/CR/lim 3dj 07 2309.zip |
| 90-96 | https://www.ieee802.org/3/dj/public/tools/KR/akinwale 3dj 01 2310.zip |
| 97-100 | https://www.ieee802.org/3/dj/public/tools/CR/akinwale 3dj 02 2311.zip |
| 101-112 | https://www.ieee802.org/3/di/public/tools/CR/weaver 3dj_02 2311.zip |

